

Lecture 10

2017/2018

Microwave Devices and Circuits for Radiocommunications

Materials

- RF-OPTO
 - <http://rf-opto.etti.tuiasi.ro>
- **David Pozar, “Microwave Engineering”,**
Wiley; 4th edition , 2011
 - 1 exam problem ← Pozar
- Photos
 - sent by email: rdamian@etti.tuiasi.ro
 - used at lectures/laboratory

Software

- ADS ~~2016~~ **2017**
- EmPro ~~2015~~ **2017**
- based on IP from outside university or campus



Date:

Grupa	5601 (2017/2018)
Specializarea	Master Retele de Comunicatii
Marca	857

[Acceseaza ca acest student](#) | [Cere acces la licente](#)

Note obtinute

Disciplina	Tip	Data	Descriere	Nota	Puncte	Obs.
TMPAW			Tehnici moderne de proiectare a aplicatiilor web			
	N	29/05/2017	Nota finala	10	-	

Nume

Email

Cod de verificare

Trimite

Software

Advanced Design System Premier High-Frequency and High Speed Design Platform

2017

 **KEYSIGHT**
TECHNOLOGIES

Advanced Design System Premier High-Frequency and High Speed Design Platform

2016.01

 **KEYSIGHT**
TECHNOLOGIES

© Keysight Technologies 1985-2016

Advanced Design System

Select a product license

You have more than one product license available.

Description

▶ **ADS Inclusive**

▶ **GoldenGate All In**

Update Availability

Legend:  **License available**  License in use or not available

ADS Inclusive

▶ **License is available**

Number of licenses: 50

Used: 3

Version: 2018.07

Expires: 30-jul-

License Setup Wizard for Advanced Design System 2016.01

Specify Remote License Server

Enter the name of the network license server you wish to add or replace.

Advanced Design System 2016.01

Enter the network license server name (e.g., 27001 or host_name.t_number@host_name)

Network license server name

(e.g., 27001)

[What is a network license server?](#)

[How do I know which network license server to use?](#)

[How do I specify a network license server name?](#)

[Can I find out the network license server name from the license file?](#)

Examining your license server...



Cancel

Clear

Details

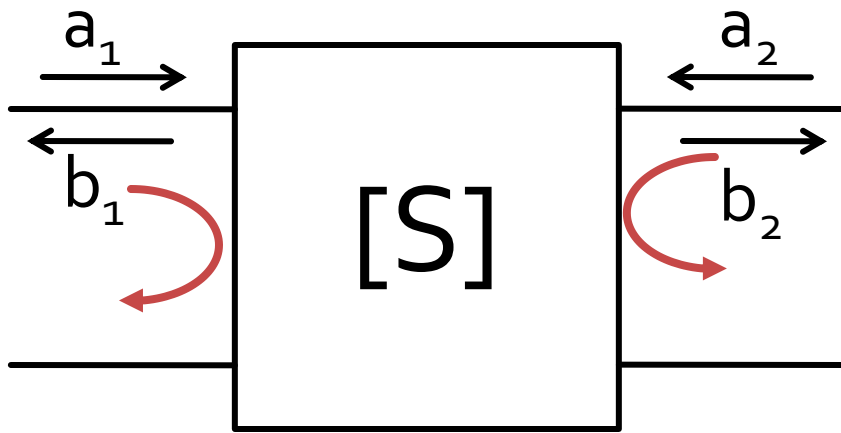
< Back

Next >

Exit

Microwave Network Analysis

Scattering matrix – S

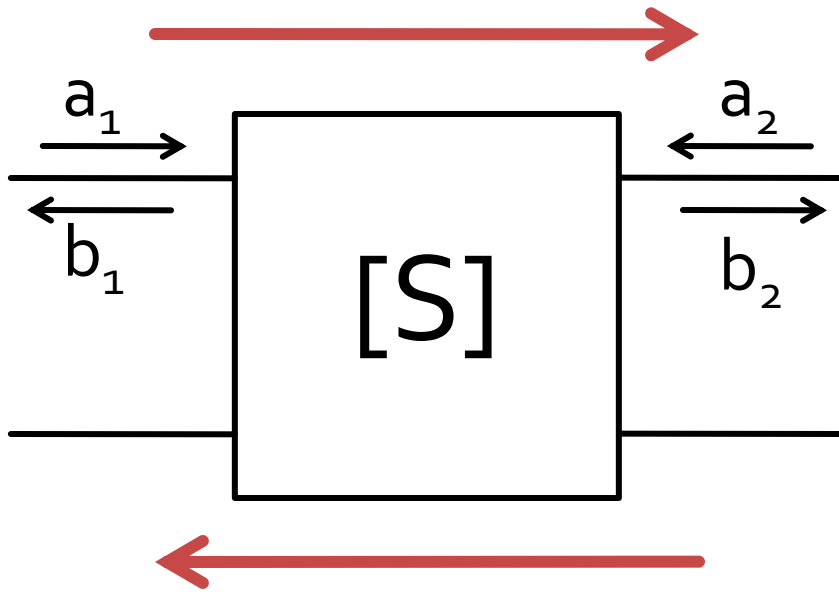


$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$S_{11} = \left. \frac{b_1}{a_1} \right|_{a_2=0} \quad S_{22} = \left. \frac{b_2}{a_2} \right|_{a_1=0}$$

- S_{11} and S_{22} are reflection coefficients at ports 1 and 2 when the other port is matched

Scattering matrix – S

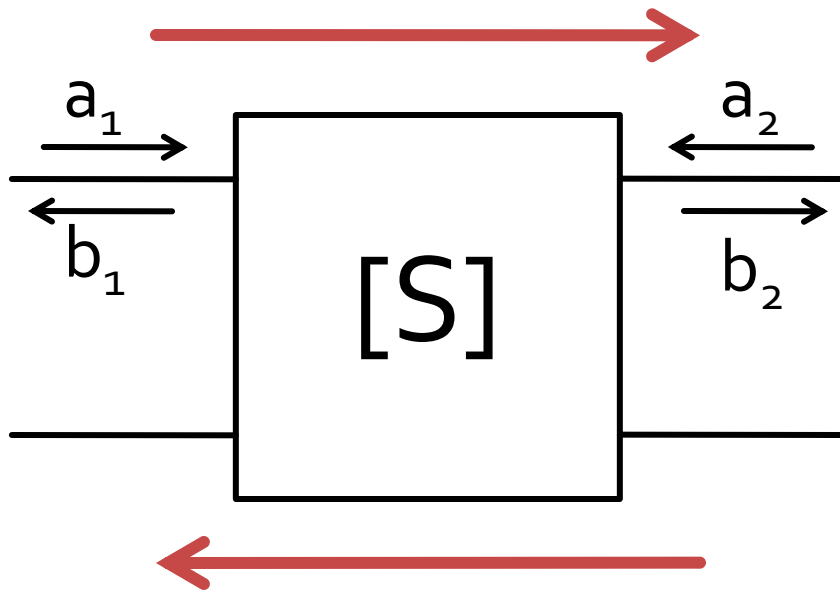


$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$S_{21} = \left. \frac{b_2}{a_1} \right|_{a_2=0} \quad S_{12} = \left. \frac{b_1}{a_2} \right|_{a_1=0}$$

- S_{21} and S_{12} are signal amplitude gain when the other port is matched

Scattering matrix – S



$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

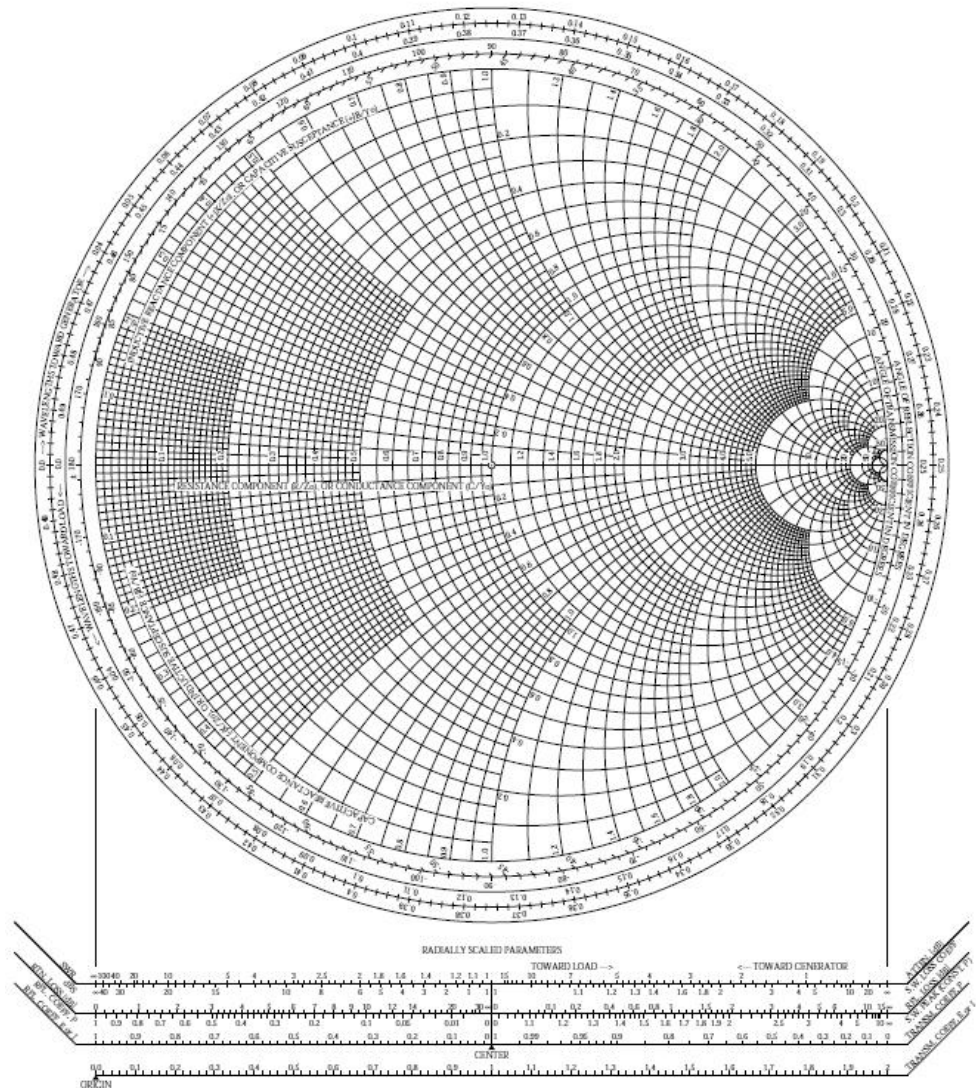
$$|S_{21}|^2 = \frac{\text{Power in } Z_0 \text{ load}}{\text{Power from } Z_0 \text{ source}}$$

- a, b
 - information about signal power **AND** signal phase
- S_{ij}
 - network effect (gain) over signal power **including** phase information

Impedance Matching

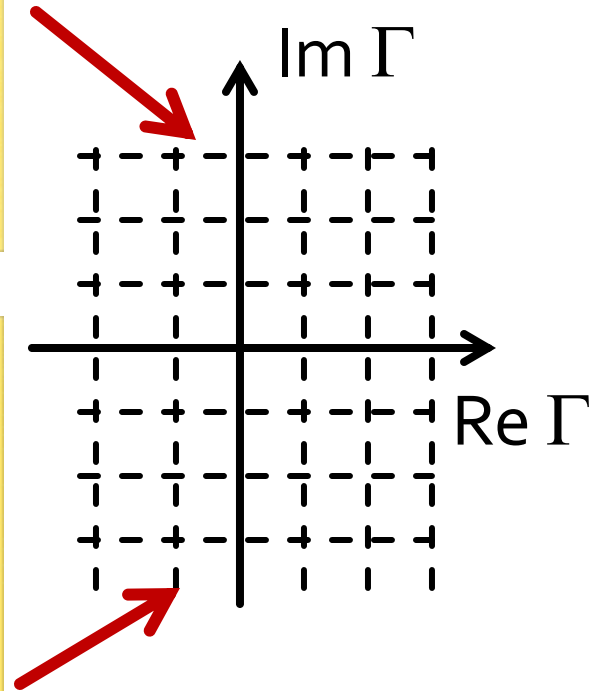
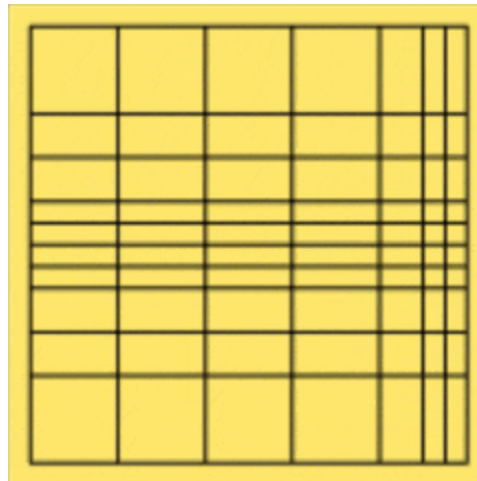
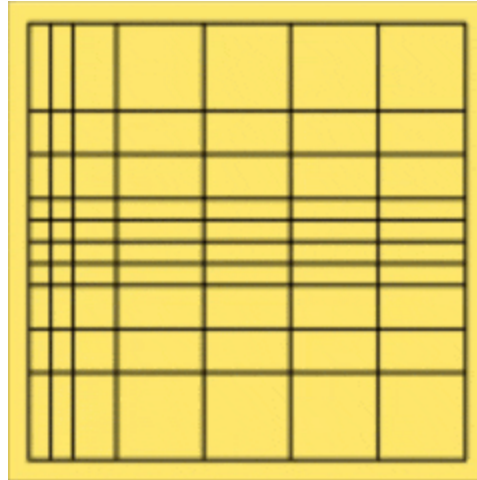
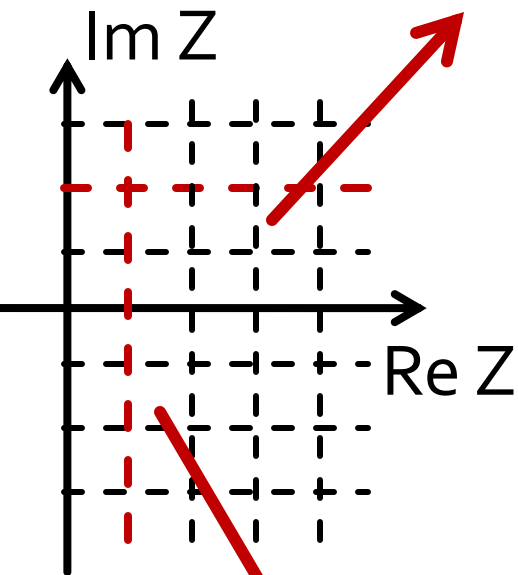
The Smith Chart

The Smith Chart



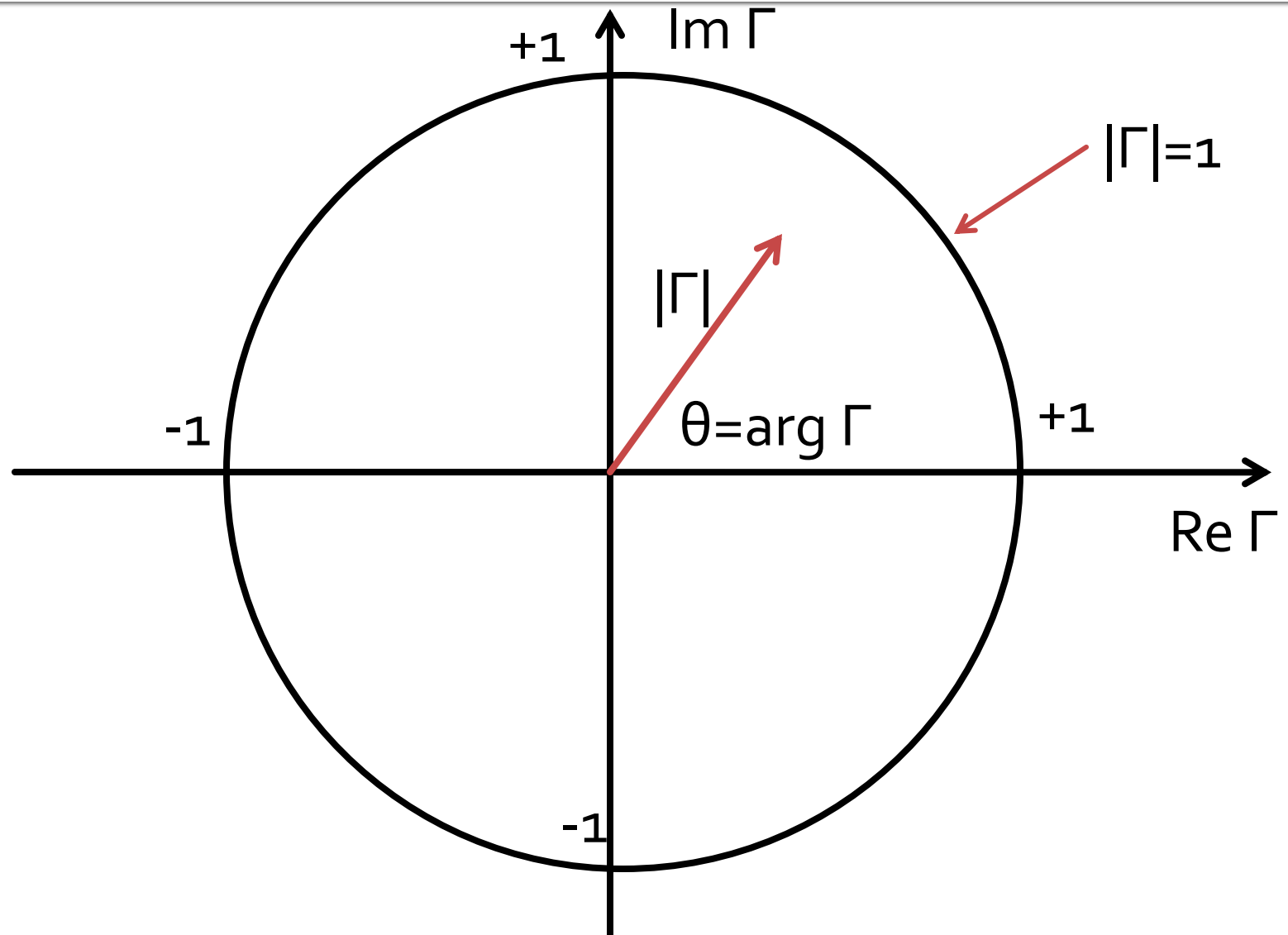
The Smith Chart

$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{z_L - 1}{z_L + 1}$$



$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{Y_0 - Y_L}{Y_0 + Y_L} = \frac{1 - y_L}{1 + y_L}$$

The Smith Chart

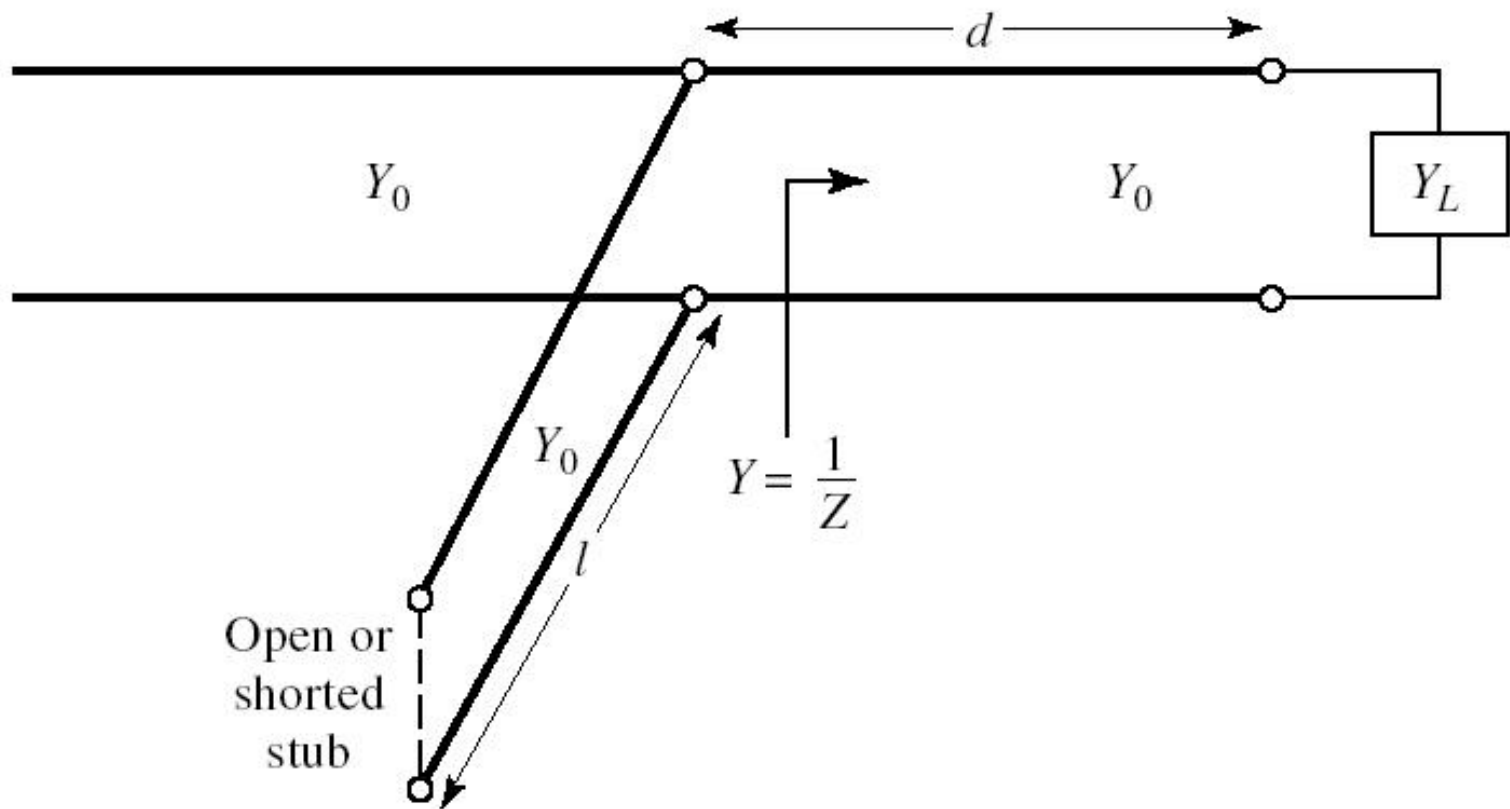


Impedance Matching with Stubs

Impedance Matching

Shunt Stub

- Shunt Stub



Analytical solution, Γ

$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

$$\Gamma_S = 0.593 \angle 46.85^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$|\Gamma_S| = 0.593; \quad \varphi = 46.85^\circ \quad \cos(\varphi + 2\theta) = -0.593 \Rightarrow (\varphi + 2\theta) = \pm 126.35^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **shunt stub** equation

- **"+" solution** ↓

$$(46.85^\circ + 2\theta) = +126.35^\circ \quad \theta = +39.7^\circ \quad \text{Im } y_s = \frac{-2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = -1.472$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_s) = -55.8^\circ (+180^\circ) \rightarrow \theta_{sp} = 124.2^\circ$$

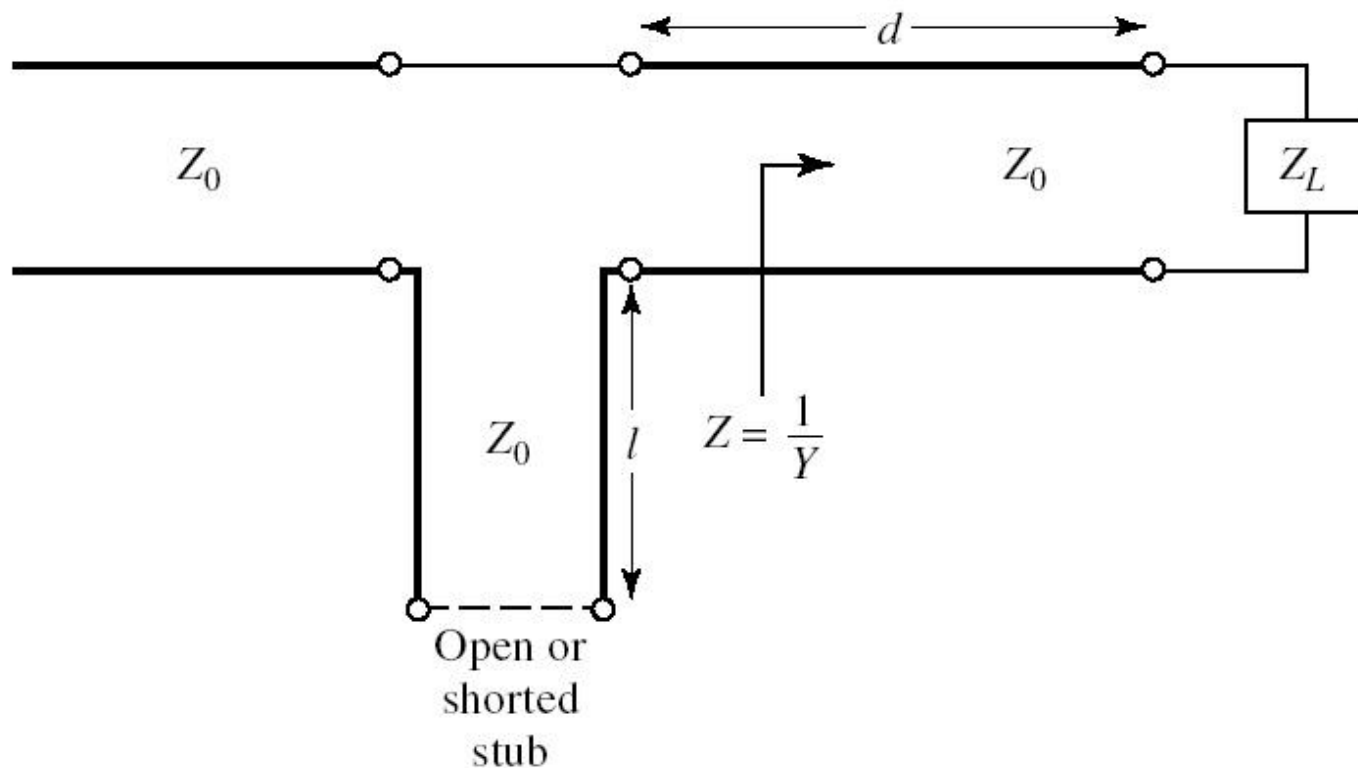
- **"-" solution** ↓

$$(46.85^\circ + 2\theta) = -126.35^\circ \quad \theta = -86.6^\circ (+180^\circ) \rightarrow \theta = 93.4^\circ$$

$$\text{Im } y_s = \frac{+2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = +1.472 \quad \theta_{sp} = \tan^{-1}(\text{Im } y_s) = 55.8^\circ$$

Series Stub

- Series Stub
- difficult to realize in single conductor line technologies (microstrip)



Analytical solution, Γ

$$\cos(\varphi + 2\theta) = |\Gamma_s|$$

$$\theta_{ss} = \beta \cdot l = \cot^{-1} \frac{\mp 2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}}$$

$$\Gamma_s = 0.555 \angle -29.92^\circ$$

$$|\Gamma_s| = 0.555; \quad \varphi = -29.92^\circ \quad \cos(\varphi + 2\theta) = 0.555 \Rightarrow (\varphi + 2\theta) = \pm 56.28^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **series stub** equation

- **"+" solution**

$$(-29.92^\circ + 2\theta) = +56.28^\circ$$

$$\theta = 43.1^\circ$$

$$\text{Im } z_s = \frac{+2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = +1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_s) = -36.8^\circ (+180^\circ) \rightarrow \theta_{ss} = 143.2^\circ$$

- **"-" solution**

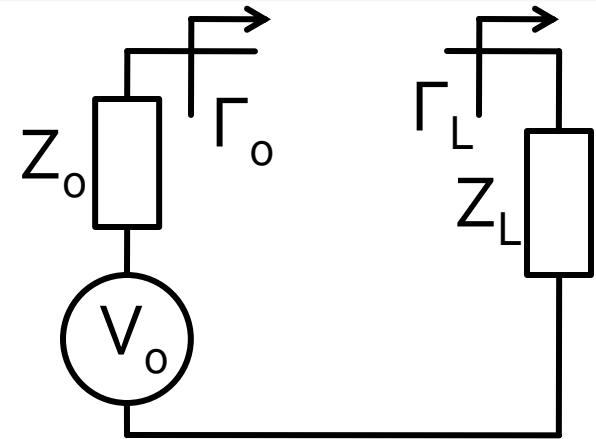
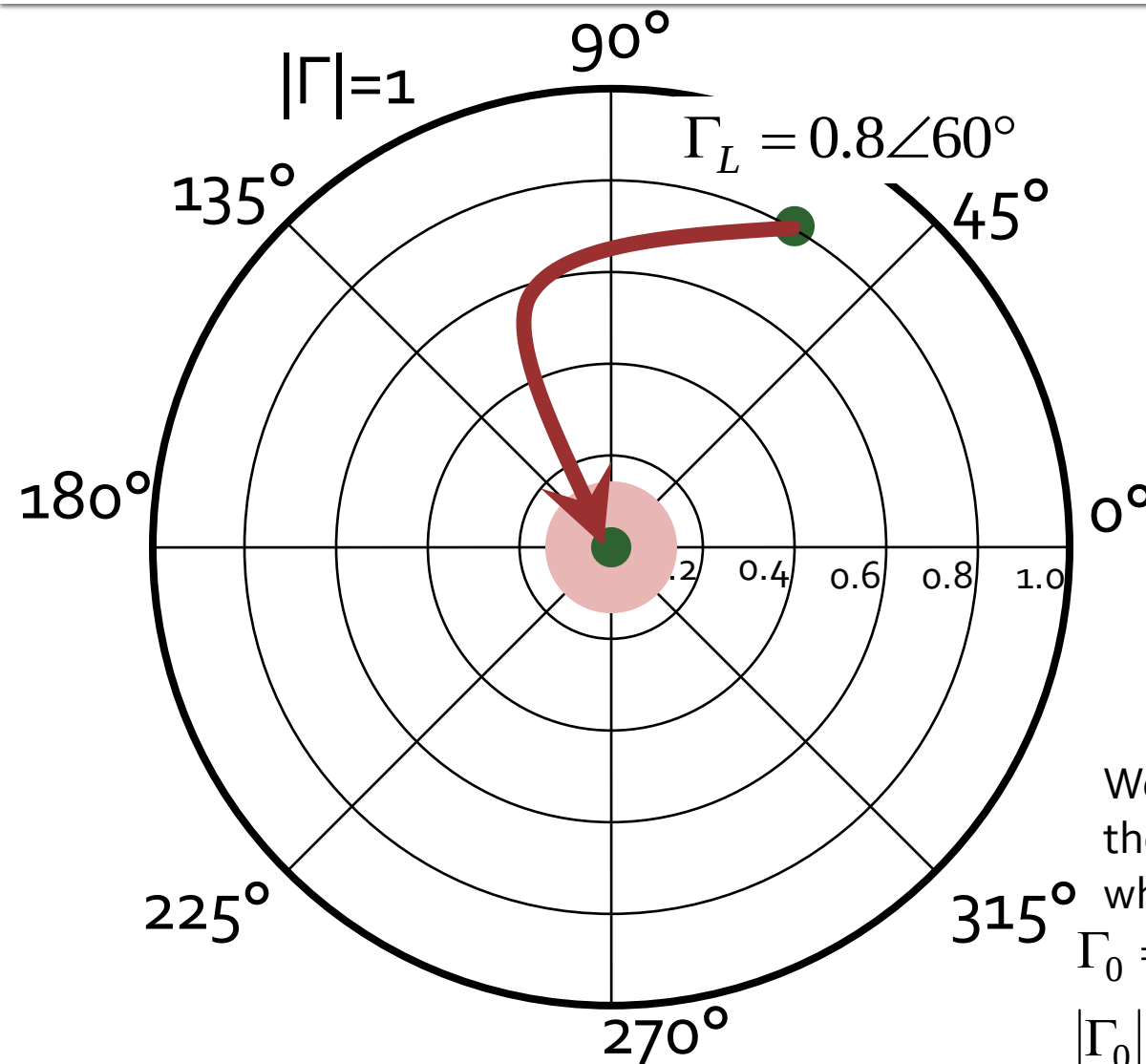
$$(-29.92^\circ + 2\theta) = -56.28^\circ$$

$$\theta = -13.2^\circ (+180^\circ) \rightarrow \theta = 166.8^\circ$$

$$\text{Im } z_s = \frac{-2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}} = -1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_s) = 36.8^\circ$$

The Smith Chart, matching, $Z_L \neq Z_o$



Matching Z_L load to Z_o source.
We normalize Z_L over Z_o

$$Z_L = 21.429\Omega + j \cdot 82.479\Omega$$

$$z_L = 0.429 + j \cdot 1.65$$

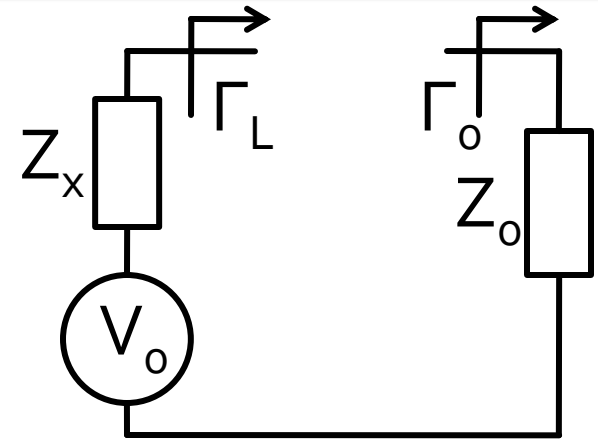
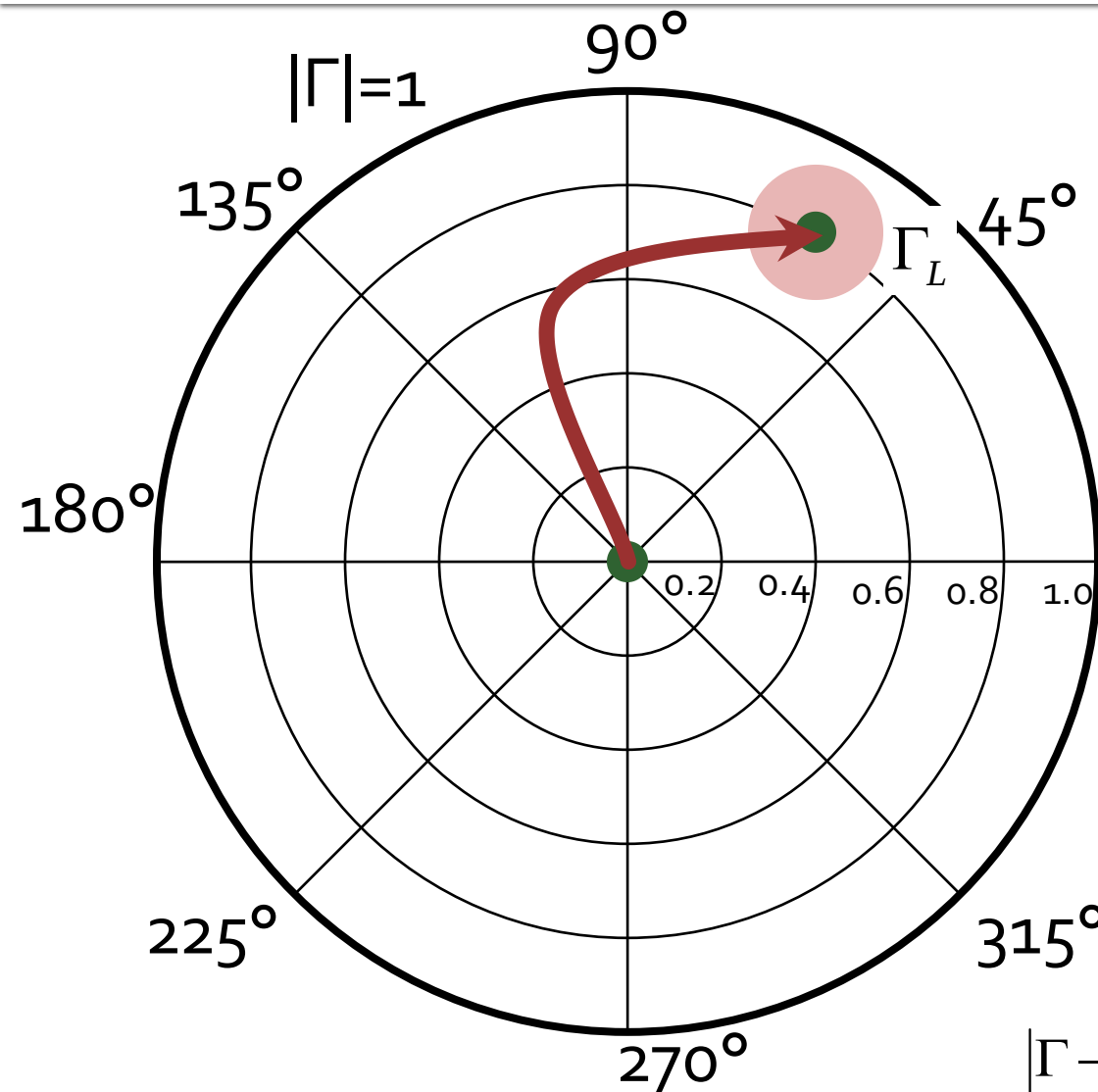
$$\Gamma_L = 0.8 \angle 60^\circ$$

We must move the point denoting the reflection coefficient in the area where with a Z_o source we have:

$$\Gamma_o = 0 \text{ perfect match}$$

$$|\Gamma_o| \leq \Gamma_m \text{ "good enough" match}$$

The Smith Chart, matching, $Z_L = Z_o$



0° The source (eg. the transistor) having Z_x needs to see a certain reflection coefficient Γ_L towards the load Z_o

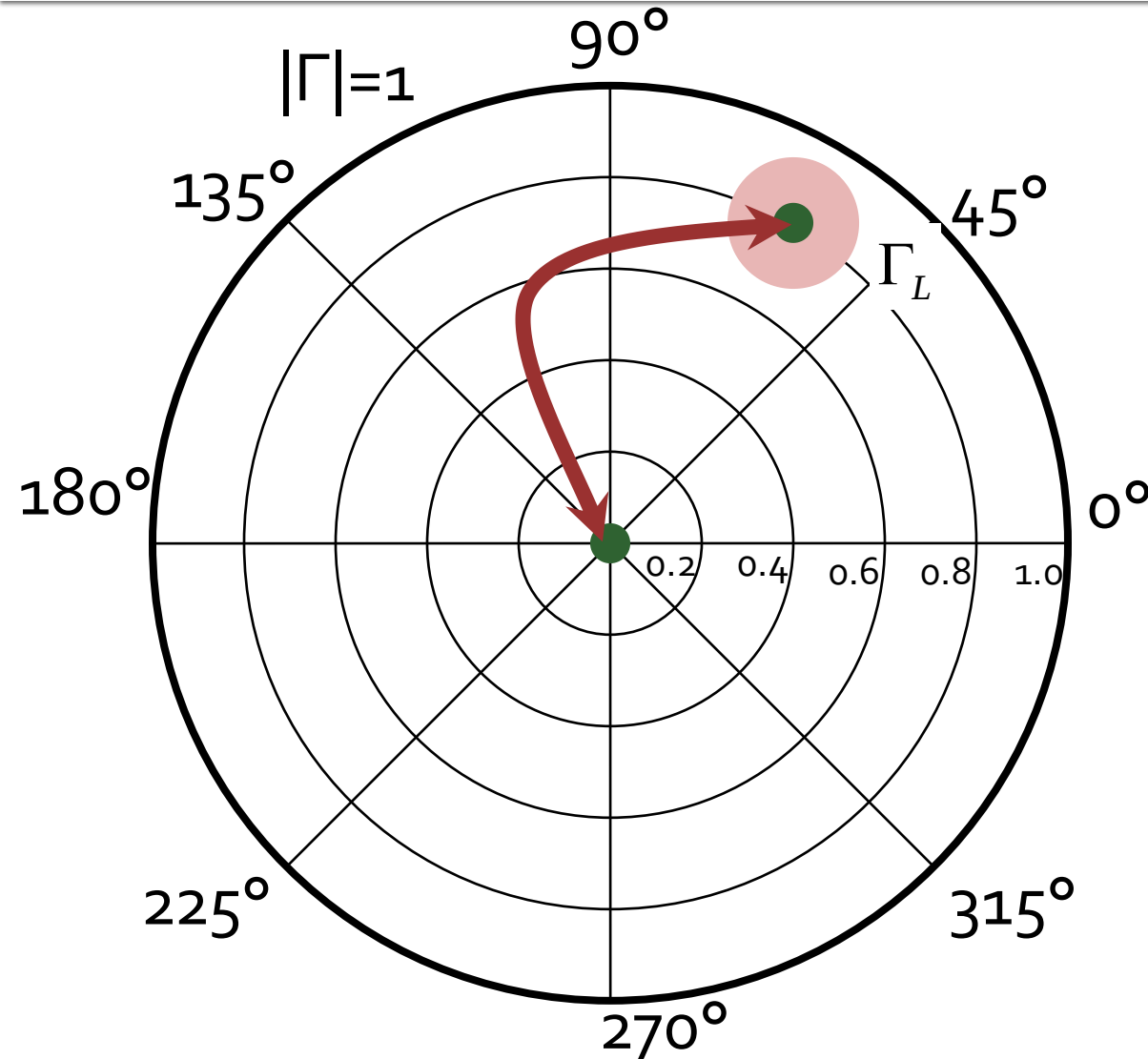
The matching circuit must move the point denoting the reflection coefficient in the area where for a Z_o load ($\Gamma_o=0$) we see towards it:

$\Gamma = \Gamma_L$ perfect match

$|\Gamma - \Gamma_L| \leq \Gamma_m$ "good enough" match

The Smith Chart, matching ,

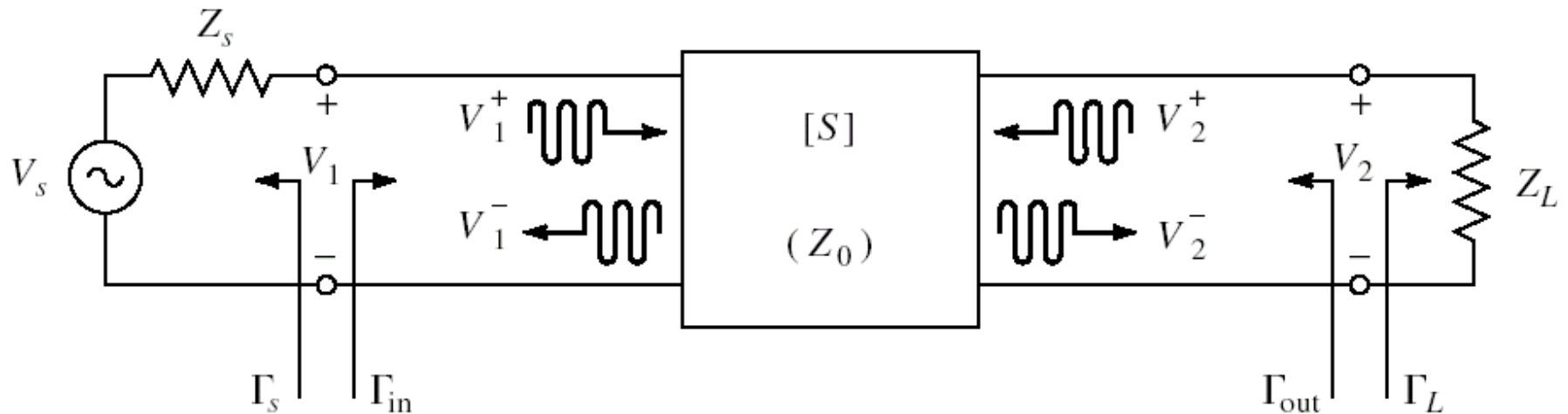
$Z_L \neq Z_o, Z_L = Z_o$



- The matching sections needed to move
 - Γ_L in Γ_o
 - Γ_o in Γ_L
- are **identical**. They differ only by the **order** in which the elements are introduced into the matching circuit
- As a result, we can use in match design the same:
 - **methods**
 - **formulae**

Microwave Amplifiers

Amplifier as two-port



- Characterized with S parameters
- normalized at Z_0 (implicit 50Ω)
- Datasheets: S parameters for specific bias conditions

Datasheets

NE46100

VCE = 5 V, Ic = 50 mA

FREQUENCY (MHz)	S11		S21		S12		S22		K	MAG ² (dB)
	MAG	ANG	MAG	ANG	MAG	ANG	MAG	ANG		
100	0.778	-137	26.776	114	0.028	30	0.555	-102	0.16	29.8
200	0.815	-159	14.407	100	0.035	29	0.434	-135	0.36	26.2
500	0.826	-177	5.855	84	0.040	38	0.400	-162	0.75	21.7
800	0.827	176	3.682	76	0.052	43	0.402	-169	0.91	18.5
1000	0.826	173	2.963	71	0.058	47	0.405	-172	1.02	16.3
1200	0.825	170	2.441	66	0.064	47	0.412	-174	1.08	14.0
1400	0.820	167	2.111	61	0.069	47	0.413	-176	1.17	12.4
1600	0.828	165	1.863	57	0.078	54	0.426	-177	1.15	11.4
1800	0.827	162	1.671	53	0.087	50	0.432	-178	1.14	10.6
2000	0.828	159	1.484	49	0.093	50	0.431	-180	1.17	9.5
2500	0.822	153	1.218	39	0.11	48	0.462	177	1.18	7.8
3000	0.818	148	1.010	30	0.135	46	0.490	174	1.16	6.3
3500	0.824	142	0.876	21	0.147	44	0.507	170	1.16	5.3
4000	0.812	137	0.762	13	0.168	38	0.535	167	1.14	4.3

VCE = 5 V, Ic = 100 mA

100	0.778	-144	27.669	111	0.027	35	0.523	-114	0.27	30.2
200	0.820	-164	14.559	97	0.029	29	0.445	-144	0.42	27.0
500	0.832	-179	5.885	84	0.035	38	0.435	-166	0.81	22.2
800	0.833	175	3.691	76	0.048	45	0.435	-173	0.95	18.8
1000	0.831	172	2.980	71	0.056	51	0.437	-176	1.05	16.0
1200	0.836	169	2.464	67	0.061	52	0.432	-178	1.11	14.0
1400	0.829	166	2.121	61	0.072	53	0.447	-180	1.12	12.6
1600	0.831	164	1.867	58	0.080	54	0.445	179	1.14	11.4

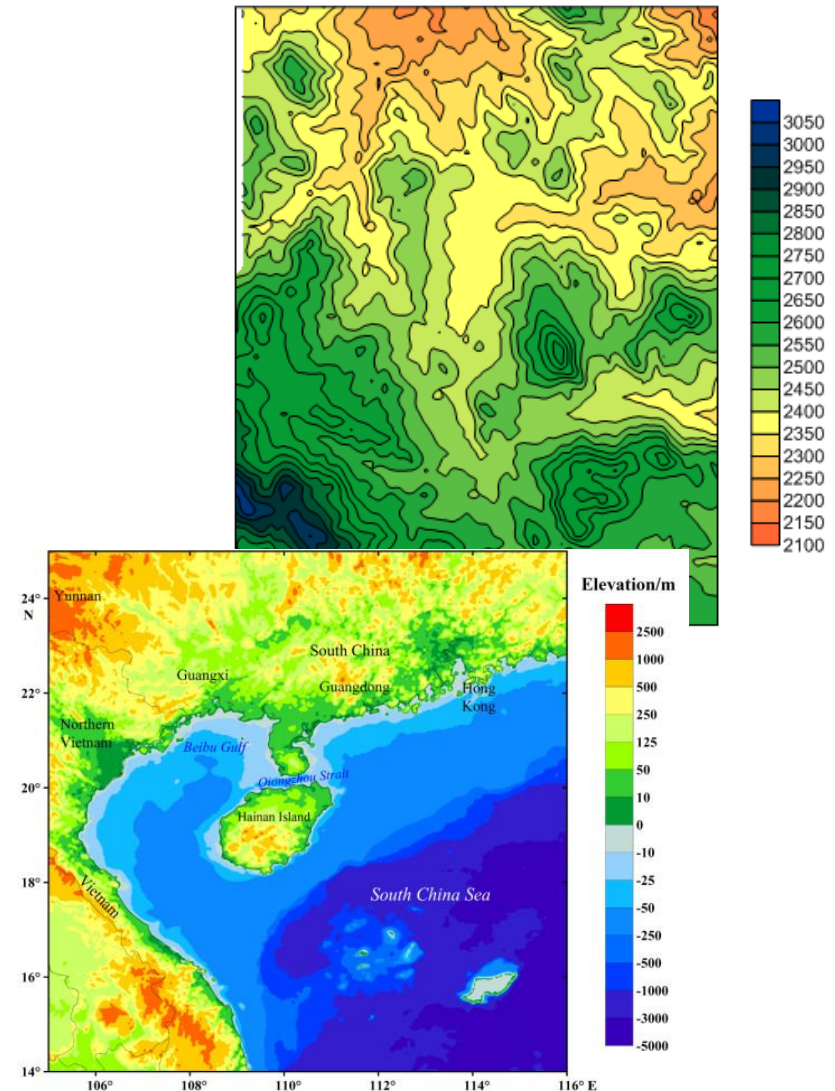
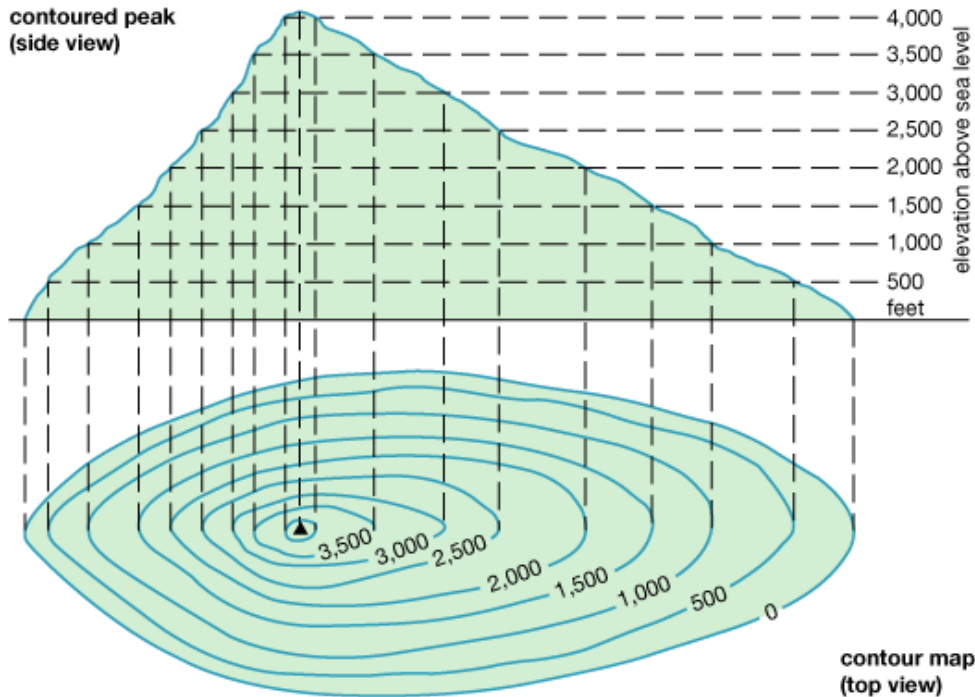
S2P - Touchstone

- Touchstone file format (*.s2p)

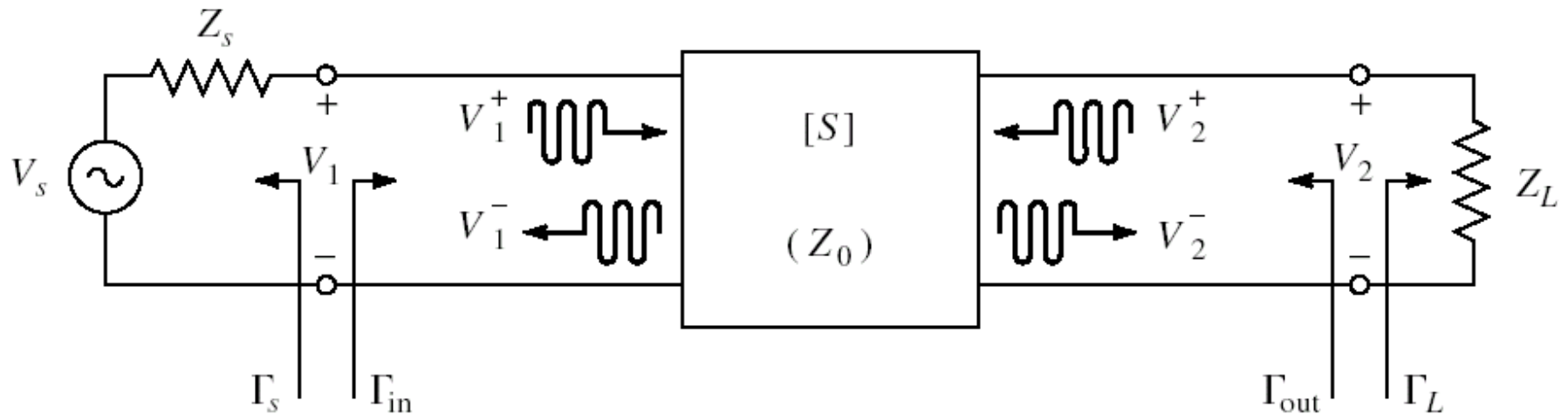
```
! SIEMENS Small Signal Semiconductors
! VDS = 3.5 V   ID = 15 mA
# GHz S MA R 50
! f      S11      S21      S12      S22
! GHz   MAG ANG   MAG ANG   MAG ANG   MAG ANG
1.000 0.9800 -18.0 2.230 157.0 0.0240 74.0 0.6900 -15.0
2.000 0.9500 -39.0 2.220 136.0 0.0450 57.0 0.6600 -30.0
3.000 0.8900 -64.0 2.210 110.0 0.0680 40.0 0.6100 -45.0
4.000 0.8200 -89.0 2.230 86.0 0.0850 23.0 0.5600 -62.0
5.000 0.7400 -115.0 2.190 61.0 0.0990 7.0 0.4900 -80.0
6.000 0.6500 -142.0 2.110 36.0 0.1070 -10.0 0.4100 -98.0
!
! f      Fmin  Gammaopt rn/50
! GHz   dB   MAG ANG  -
2.000   1.00 0.72 27 0.84
4.000   1.40 0.64 61 0.58
```

Contour map/lines

$$\begin{cases} F = f(x, y) & x, y \in \mathbf{R} \\ F = f(z) & z \in \mathbf{C} \end{cases}$$



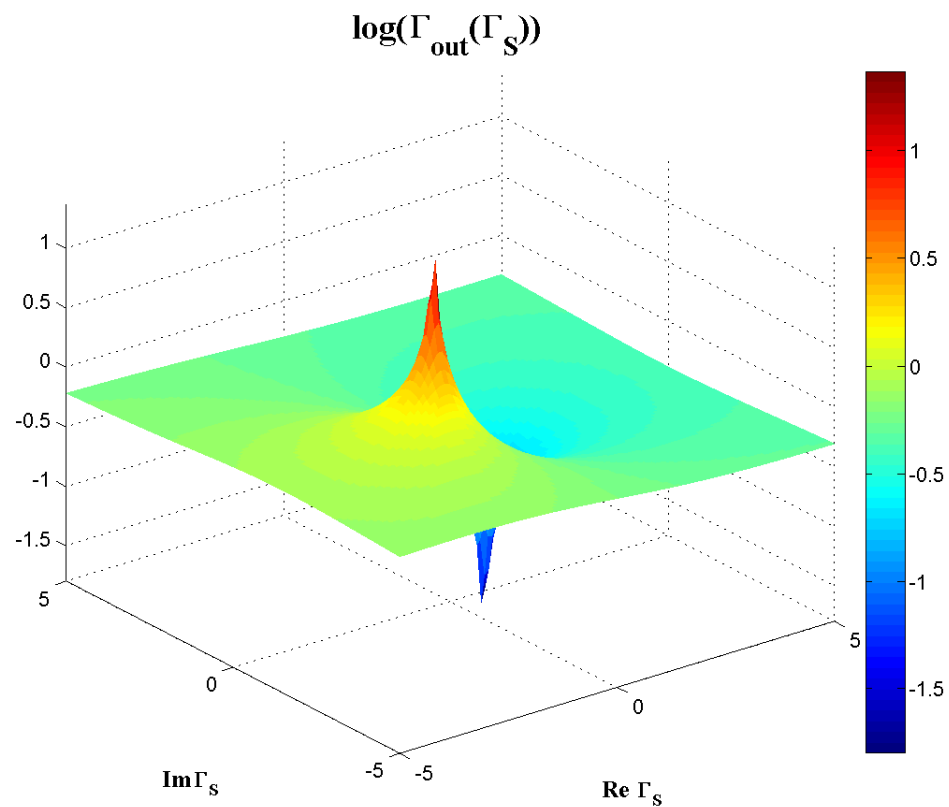
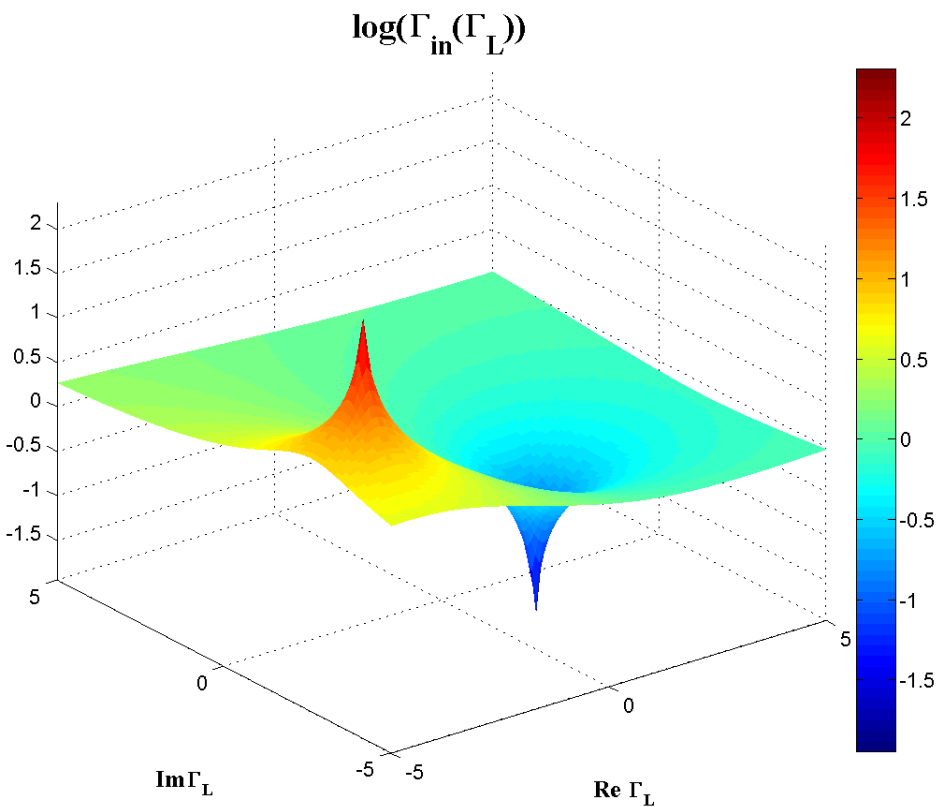
Amplifier as two-port



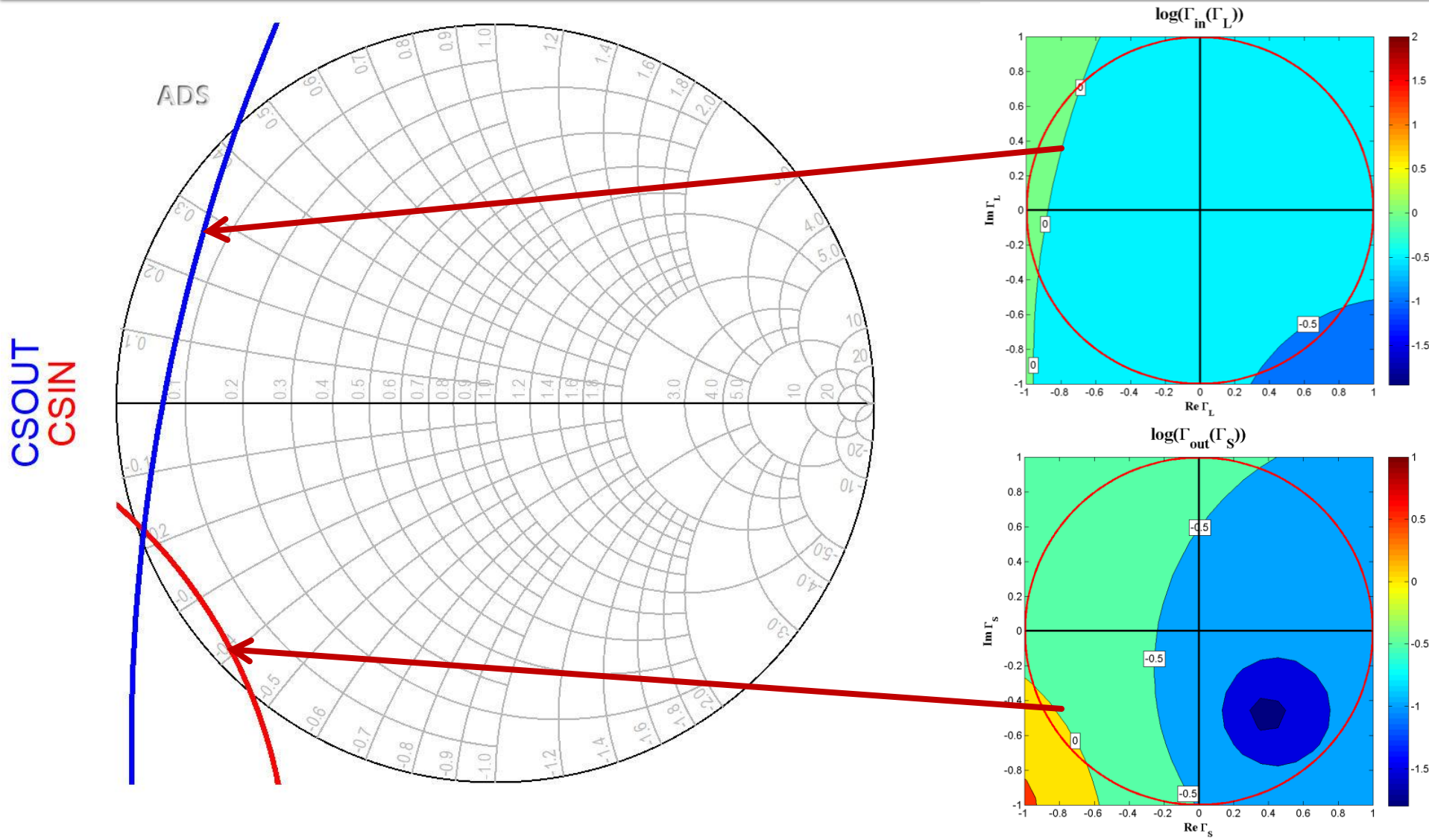
- For an amplifier two-port we are interested in:
 - **stability**
 - power gain
 - noise (sometimes – small signals)
 - linearity (sometimes – large signals)

3D representation of $|\Gamma_{in}|$, $|\Gamma_{out}|$

■ $\log_{10}|\Gamma_{in}|, \log_{10}|\Gamma_{out}|$



CSIN, CSOUT, $|\Gamma_{in}|=1$, $|\Gamma_{out}|=1$



Rollet's condition

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 \cdot |S_{12} \cdot S_{21}|}$$

$$\Delta = S_{11} \cdot S_{22} - S_{12} \cdot S_{21}$$

- The two-port is **unconditionally stable** if:
- two conditions are simultaneously satisfied:
 - $K > 1$
 - $|\Delta| < 1$
- together with the implicit conditions:
 - $|S_{11}| < 1$
 - $|S_{22}| < 1$

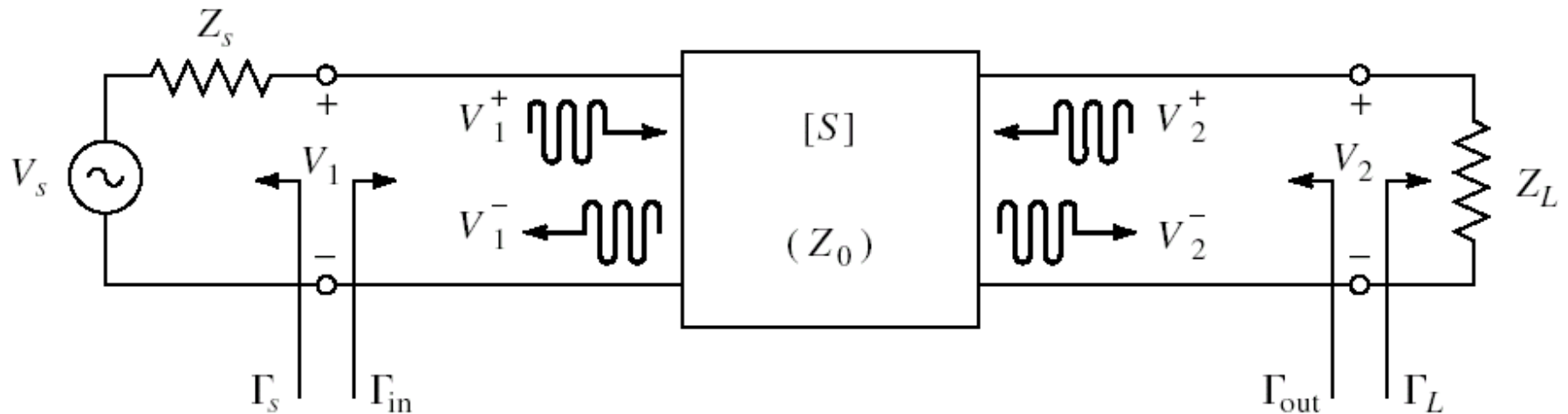
$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2 \cdot |S_{12} \cdot S_{21}|} > 1$$

$$|\Delta| = |S_{11} \cdot S_{22} - S_{12} \cdot S_{21}| < 1$$

Power Gain of Microwave Amplifiers

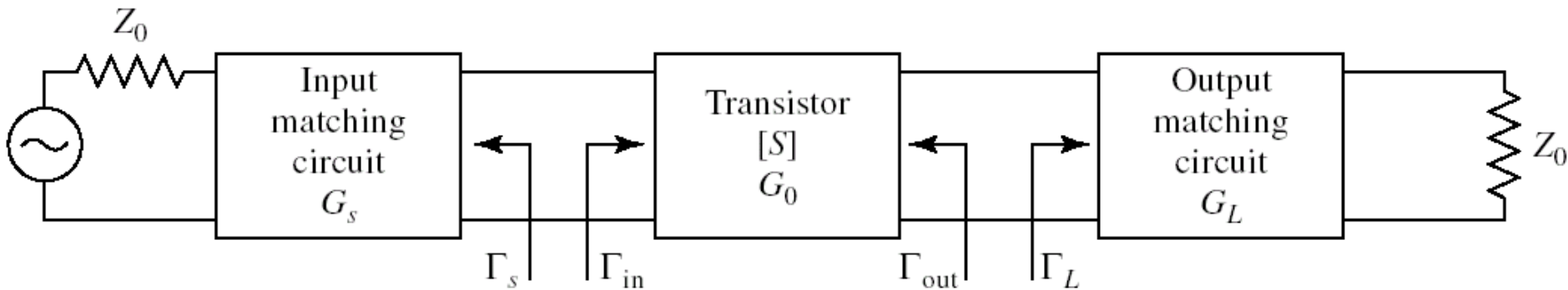
Microwave Amplifiers

Amplifier as two-port



- For an amplifier two-port we are interested in:
 - stability
 - **power gain**
 - noise (sometimes – small signals)
 - linearity (sometimes – large signals)

Design for Maximum Gain



- Maximum power gain (complex conjugate matching):

$$\Gamma_{in} = \Gamma_s^* \quad \Gamma_{out} = \Gamma_L^*$$

- For lossless matching sections

$$G_{T\max} = \frac{|S_{21}|^2 \cdot (1 - |\Gamma_s|^2) \cdot (1 - |\Gamma_L|^2)}{|1 - \Gamma_s \cdot \Gamma_{in}|^2 \cdot |1 - S_{22} \cdot \Gamma_L|^2} \quad G_{T\max} = \frac{1}{1 - |\Gamma_s|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

- For the general case of the bilateral transistor ($S_{12} \neq 0$)

Γ_{in} and Γ_{out} depend on each other so the input and output sections must be matched simultaneously

Simultaneous matching

- Simultaneous matching can be achieved **if and only if** the amplifier is **unconditionally stable** at the operating frequency, and $|\Gamma| < 1$ solutions are those with “–” sign of quadratic solutions

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases}$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

$$\begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

Example

- ATF-34143 at $V_{ds}=4V$ $I_d=40mA$.
- @5GHz
 - $S_{11} = 0.64 \angle 111^\circ$
 - $S_{12} = 0.117 \angle -27^\circ$
 - $S_{21} = 2.923 \angle -6^\circ$
 - $S_{22} = 0.21 \angle 111^\circ$

Computations

$$\begin{cases} B_1 = 1 + |S_{11}|^2 - |S_{22}|^2 - |\Delta|^2 \\ C_1 = S_{11} - \Delta \cdot S_{22}^* \end{cases}$$

$$\begin{cases} B_1 = 1.207 \\ C_1 = -0.277 + j \cdot 0.529 \end{cases}$$

$$\Gamma_S = \frac{B_1 - \sqrt{B_1^2 - 4 \cdot |C_1|^2}}{2 \cdot C_1}$$

$$\Gamma_S = -0.403 - j \cdot 0.768$$

$$|\Gamma_S| = 0.867 < 1$$

$$\Gamma_S = 0.867 \angle -117.7^\circ$$

$$\begin{cases} B_2 = 1 + |S_{22}|^2 - |S_{11}|^2 - |\Delta|^2 \\ C_2 = S_{22} - \Delta \cdot S_{11}^* \end{cases}$$

$$\begin{cases} B_2 = 0.476 \\ C_2 = -0.222 - j \cdot 0.013 \end{cases}$$

$$\Gamma_L = \frac{B_2 - \sqrt{B_2^2 - 4 \cdot |C_2|^2}}{2 \cdot C_2}$$

$$\Gamma_L = -0.685 + j \cdot 0.04$$

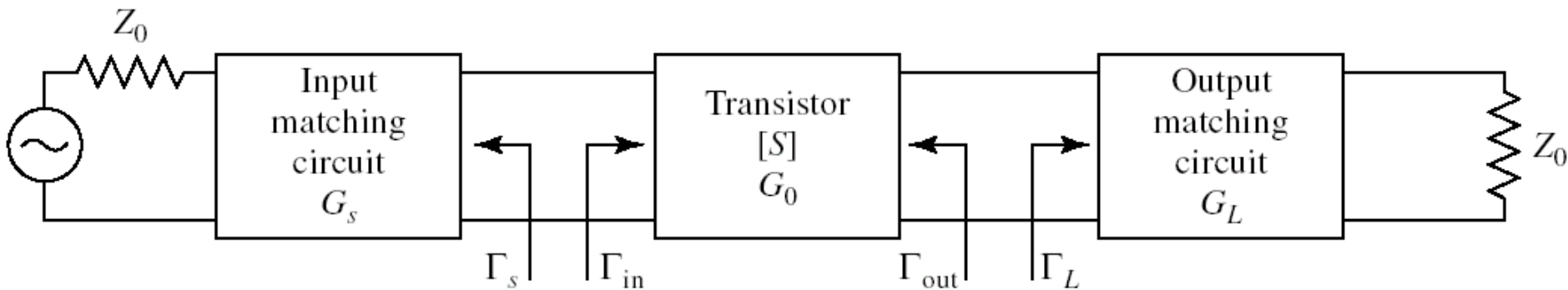
$$|\Gamma_L| = 0.686 < 1$$

$$\Gamma_L = 0.686 \angle 176.7^\circ$$

Design for Specified Gain

- In many cases we need an approach other than “brute force” when we prefer to design for **less than the maximum obtainable gain**, in order to:
 - improve noise behavior ($L_3 + C_9$)
 - improve stability
 - improve VSWR
 - control performance at multiple frequencies
 - improve amplifier's bandwidth

Design for Specified Gain



- In the unilateral assumption:

$$G_{TU} = \frac{1 - |\Gamma_s|^2}{|1 - S_{11} \cdot \Gamma_s|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

$$G_s = \frac{1 - |\Gamma_s|^2}{|1 - S_{11} \cdot \Gamma_s|^2}$$

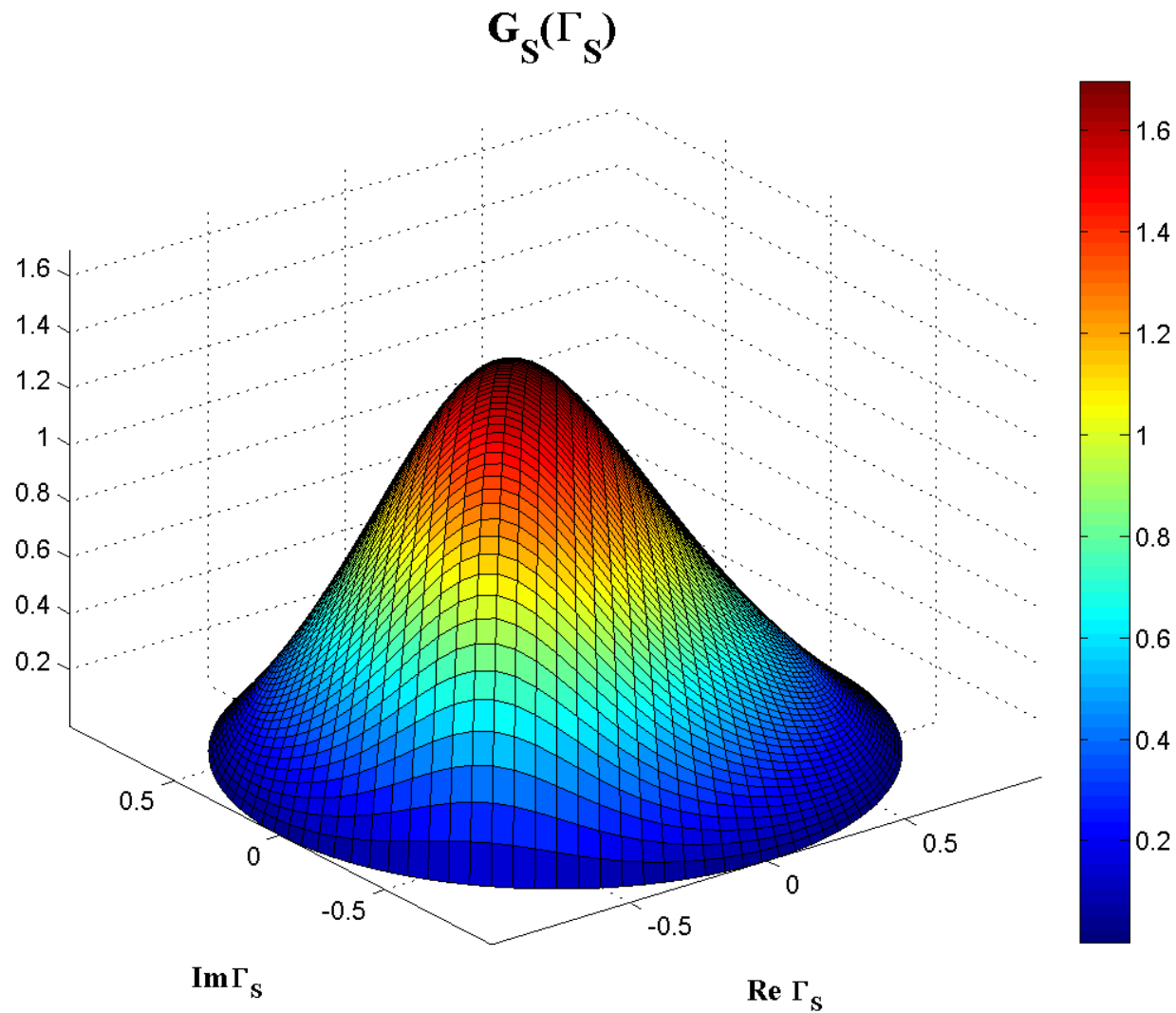
$$G_s = G_s(\Gamma_s)$$

$$G_0 = |S_{21}|^2$$

$$G_L = \frac{1 - |\Gamma_L|^2}{|1 - S_{22} \cdot \Gamma_L|^2}$$

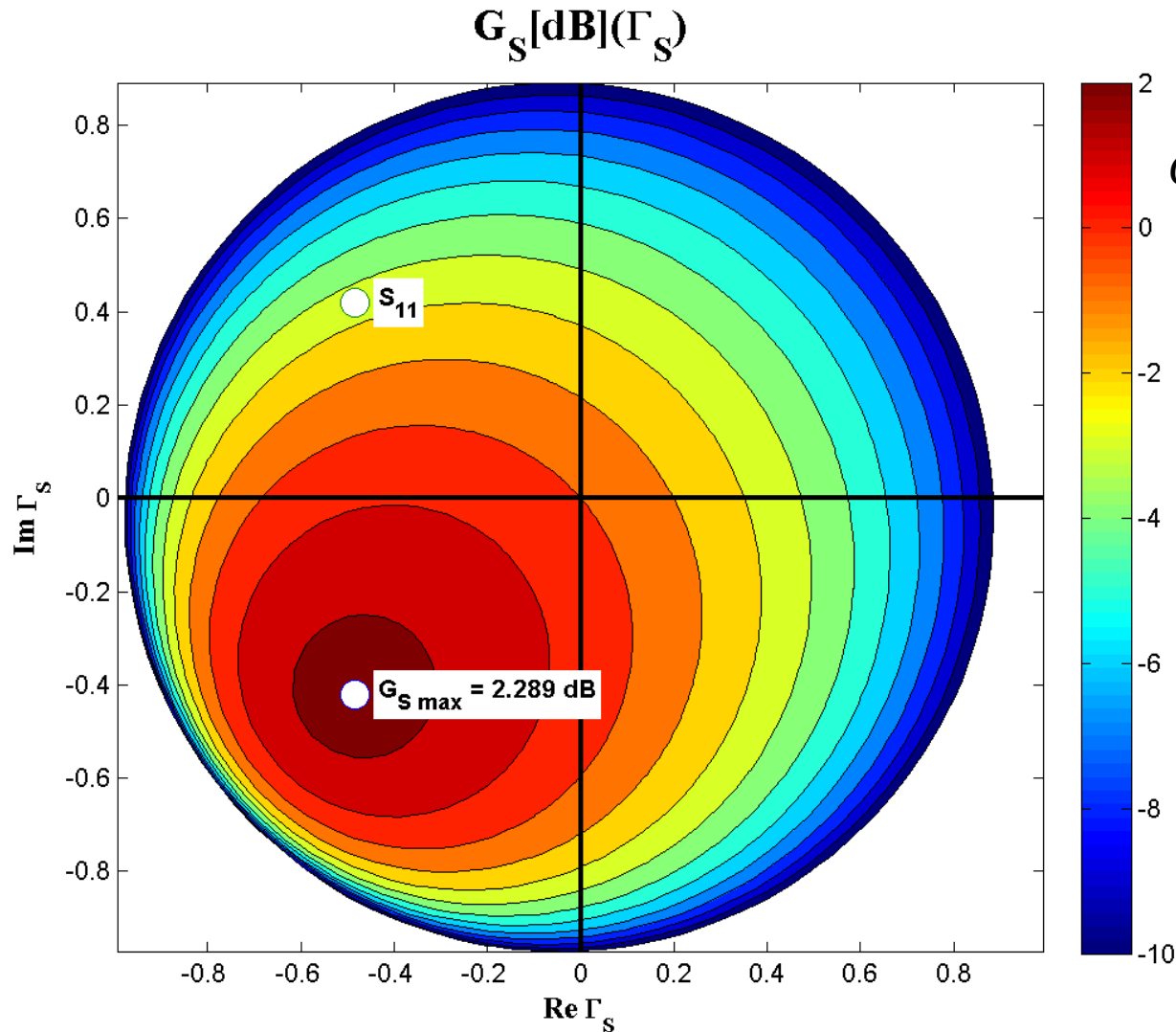
$$G_L = G_L(\Gamma_L)$$

$$G_S(\Gamma_S)$$



$$G_S = \frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2}$$

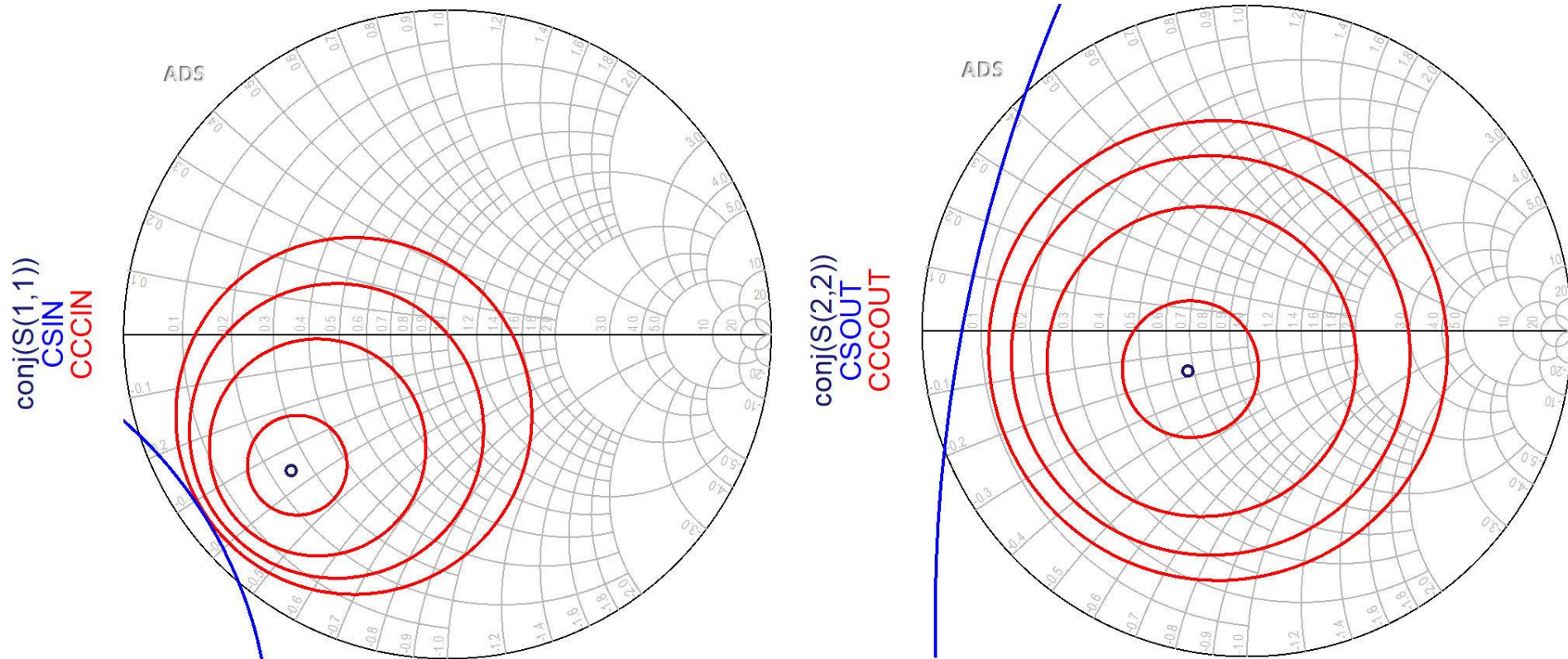
$G_S[\text{dB}](\Gamma_S)$, constant value contours



$$G_S[\text{dB}] = 10 \cdot \log \left(\frac{1 - |\Gamma_S|^2}{|1 - S_{11} \cdot \Gamma_S|^2} \right)$$

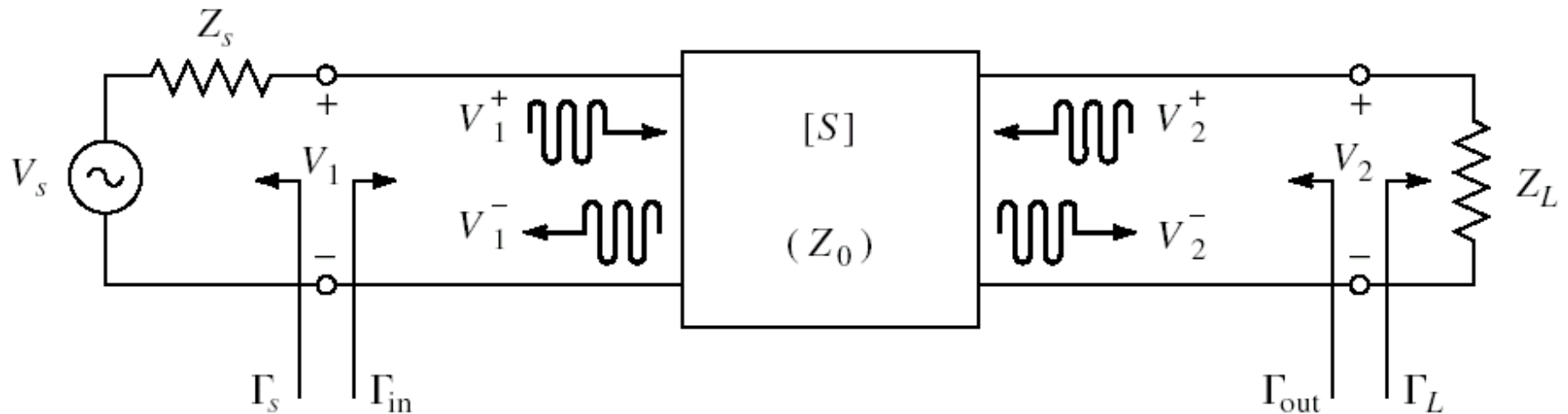
$$G_{S \max} = G_S|_{\Gamma_S = S_{11}^*}$$

ADS



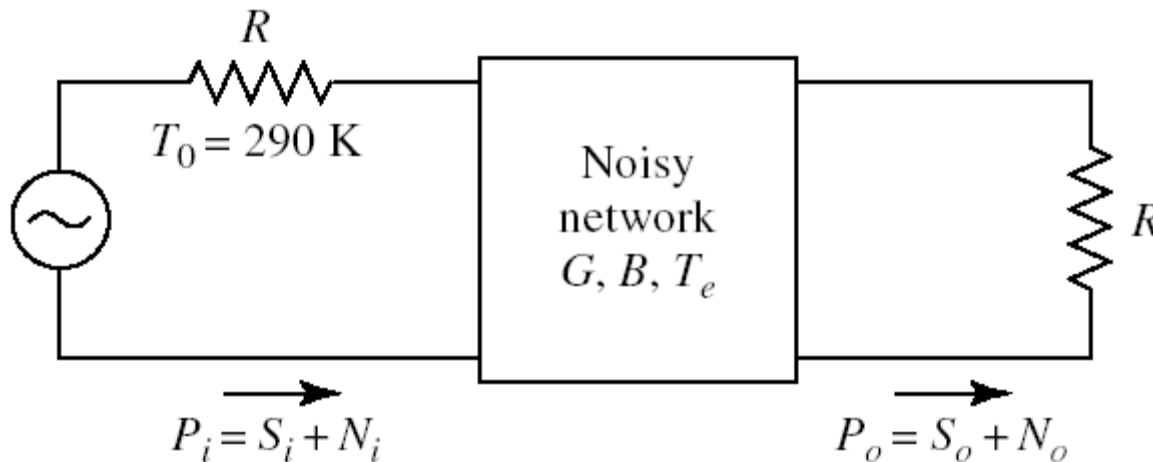
- Circles are plotted for requested values (**in dB!**)
- It is useful to compute $G_{S_{\max}}$ and $G_{L_{\max}}$ before
 - in order to request relevant circles

Amplifier as two-port



- For an amplifier two-port we are interested in:
 - stability
 - power gain
 - **noise** (sometimes – small signals)
 - linearity (sometimes – large signals)

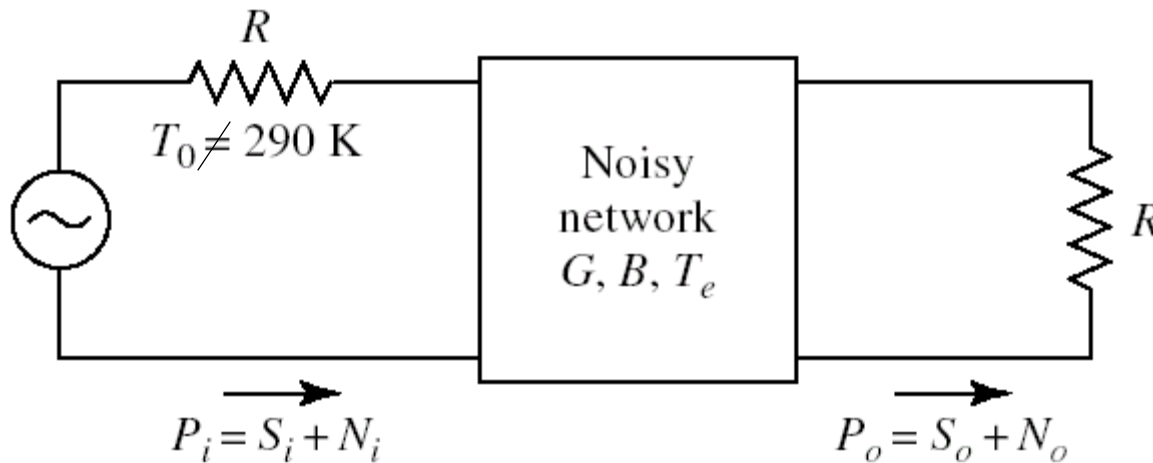
Noise Figure F



- The noise figure F , is a measure of the reduction in signal-to-noise ratio between the input and output of a device, when (by definition) the input noise power is assumed to be the noise power resulting from a matched resistor at $T_0 = 290\text{ K}$ (reference noise conditions)

$$F = \left. \frac{S_i/N_i}{S_o/N_o} \right|_{T_0=290K}$$

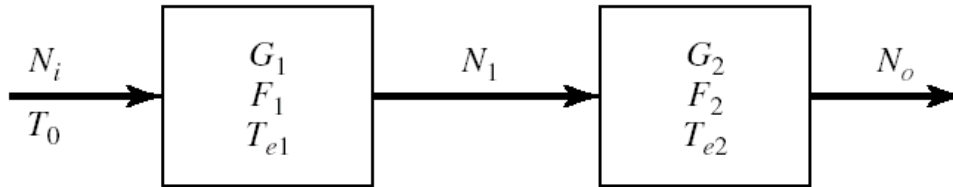
Noise Figure F



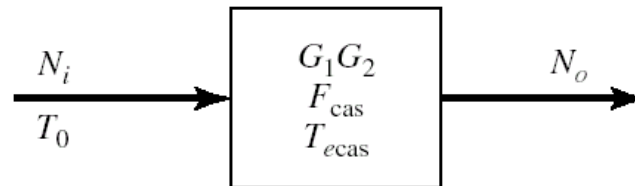
- The noise figure F , **is not** directly a measure of the reduction in signal-to-noise ratio between the input and output of a device, when the input noise power is different from that of the reference noise conditions

$$F \neq \left. \frac{S_i/N_i}{S_o/N_o} \right|_{T_0 \neq 290\text{ K}}$$

Noise figure of a cascaded system



(a)



(b)

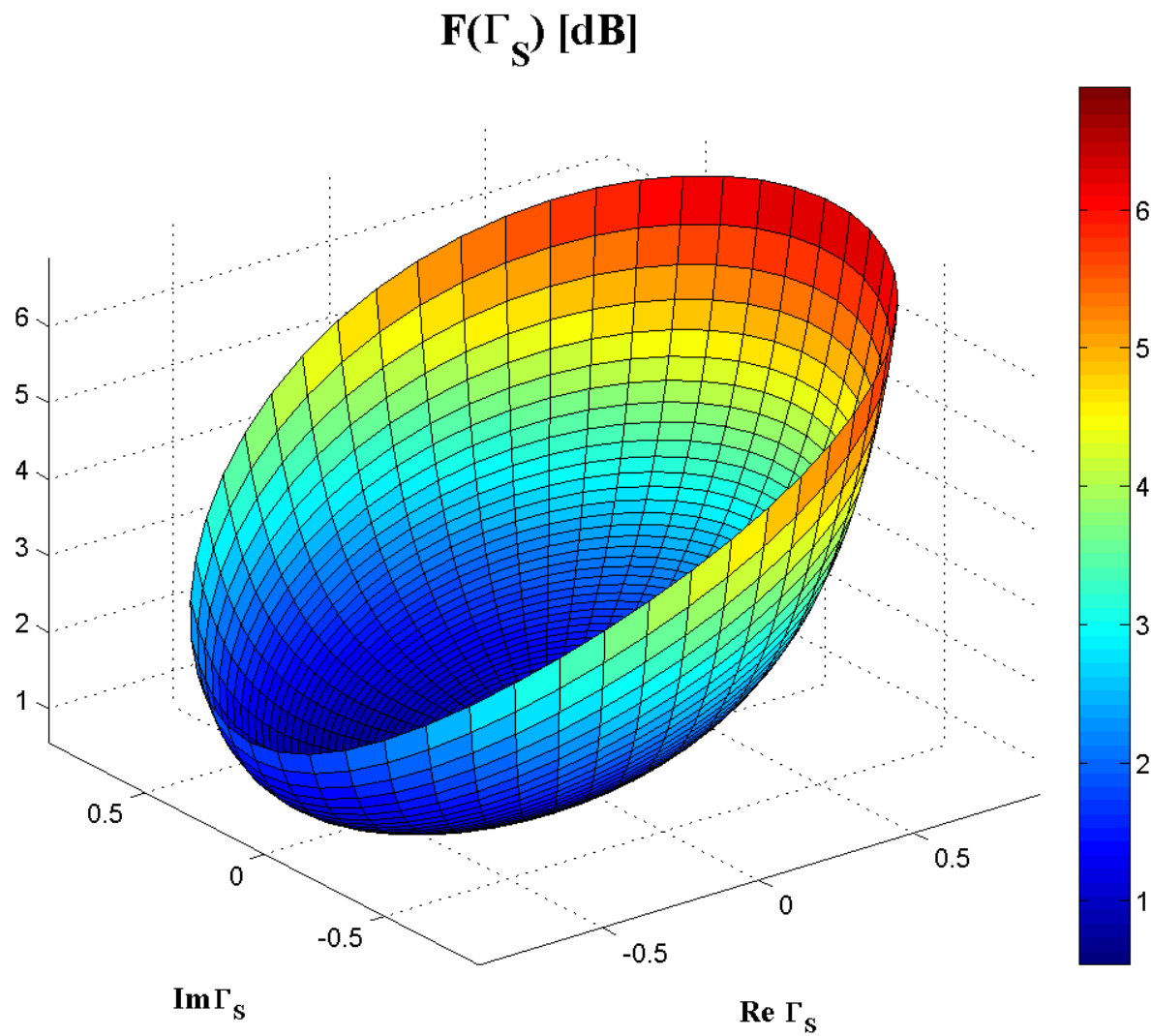
$$G_{cas} = G_1 \cdot G_2$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1)$$

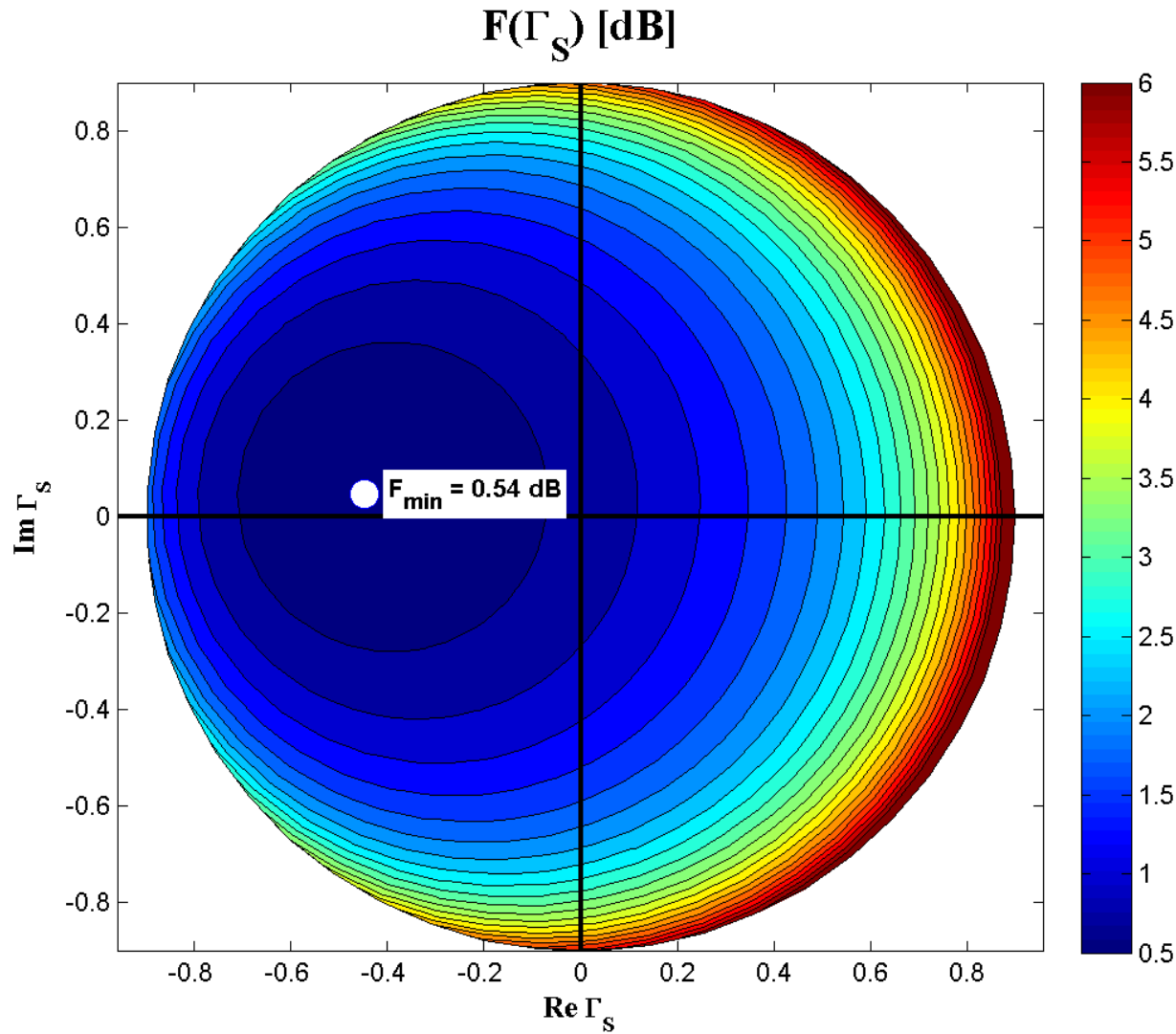
- Friis Formula (!linear scale)

$$F_{cas} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 \cdot G_2} + \frac{F_4 - 1}{G_1 \cdot G_2 \cdot G_3} + \dots$$

$F[\text{dB}](\Gamma_s)$

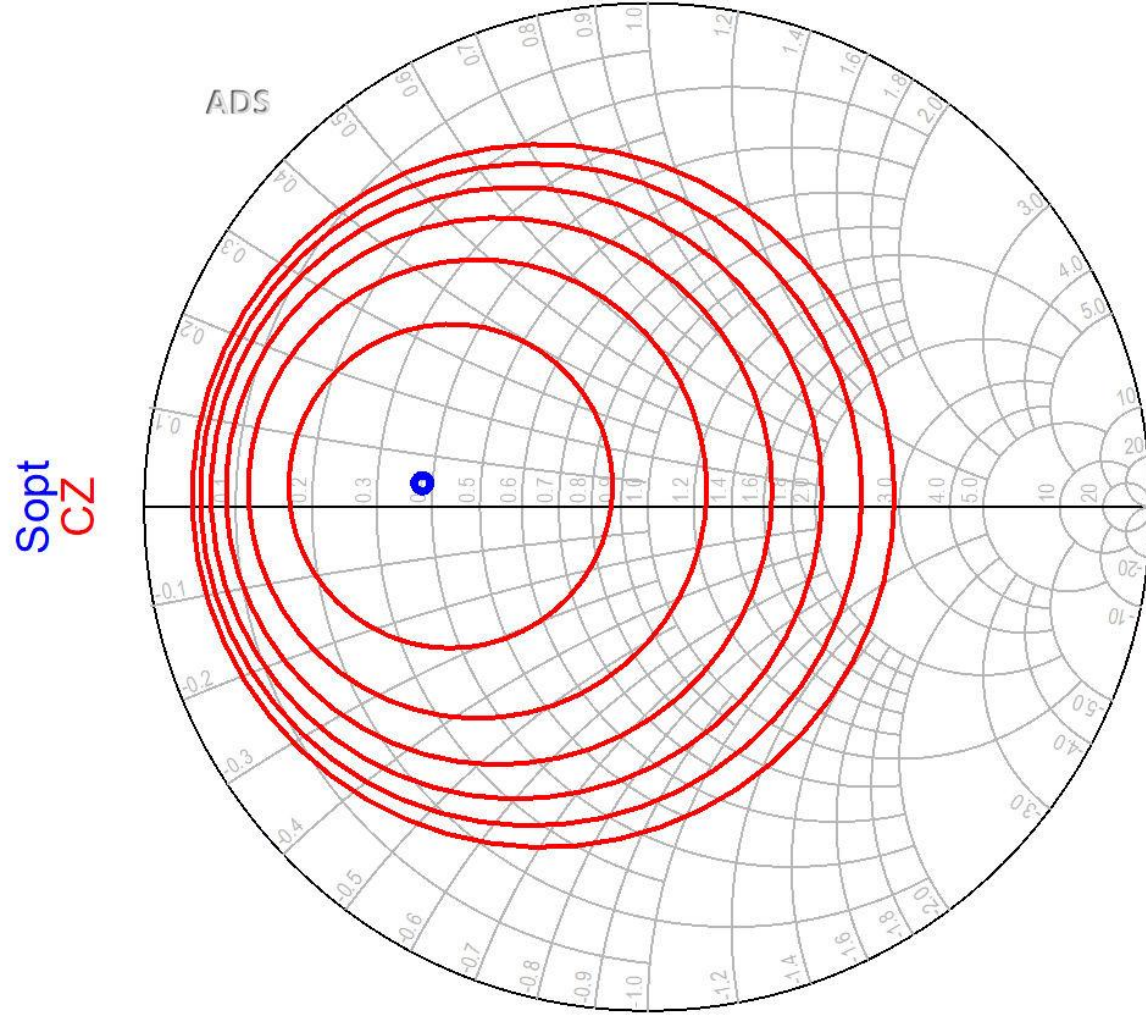


$G_s[\text{dB}](\Gamma_s)$, constant value contours



$$\Gamma_{\text{opt}} = 0.45 \angle 174^\circ$$

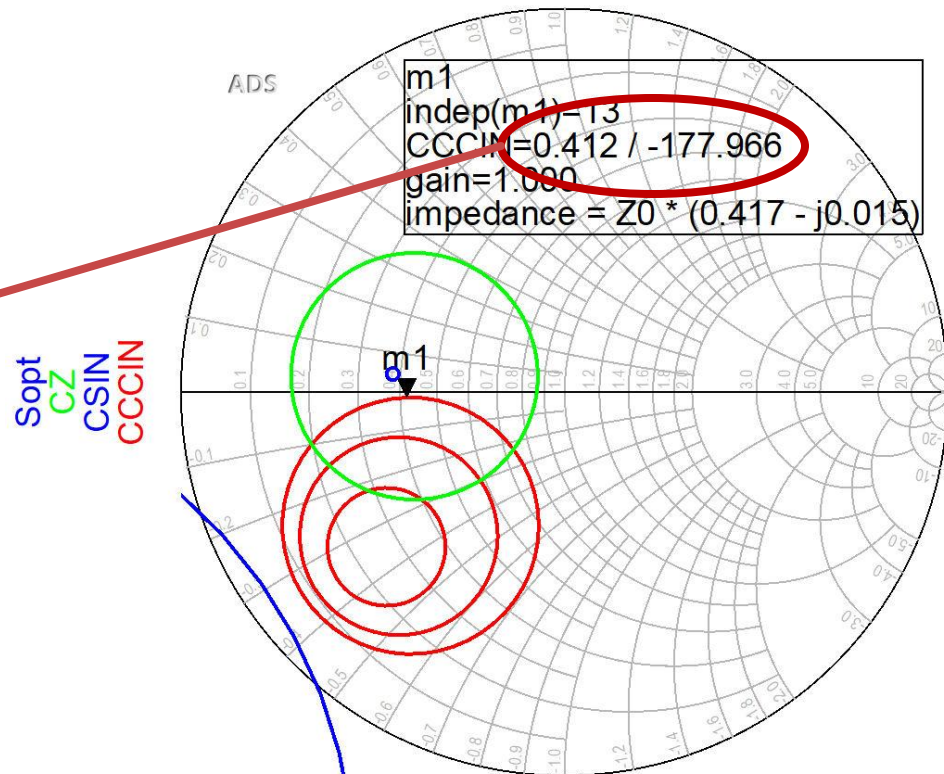
ADS



Matching – 2

- We plot on the complex plane (Smith Chart) the stability/gain/noise circles (depending on the particular application)
- We choose a point with a suitable position relative to these circles (also application dependent)
- We determine the input reflection coefficient corresponding to this point, Γ_s

$$\Gamma_s = 0.412 \angle -177.966^\circ$$

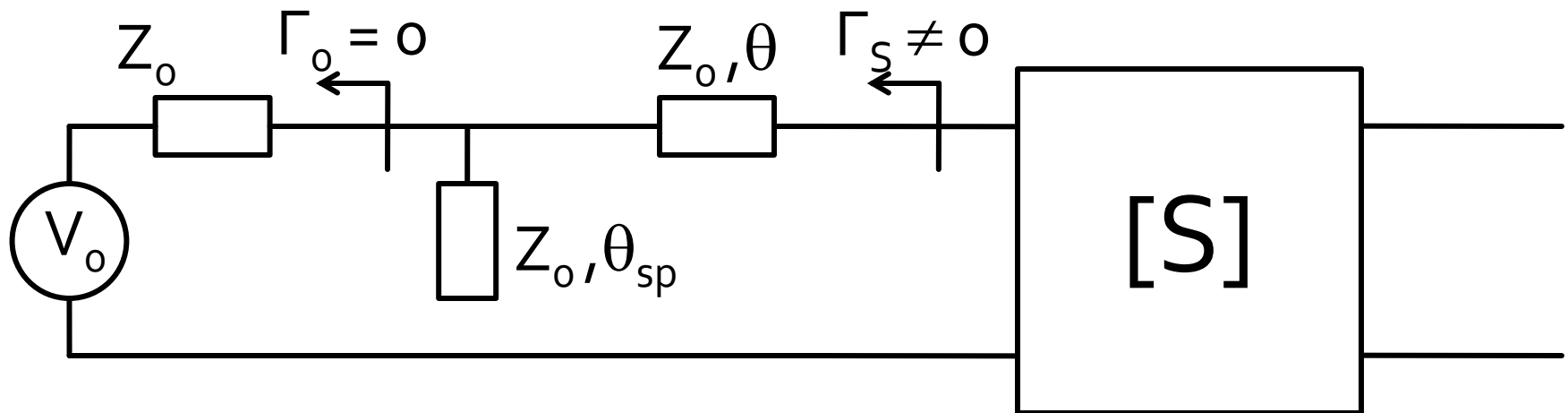


Matching – 5

- Computation depends solely on Γ_s (magnitude and phase)

$$\cos(\varphi_s + 2\theta) = -|\Gamma_s| \quad \tan \theta_{sp} = \frac{\mp 2 \cdot |\Gamma_s|}{\sqrt{1 - |\Gamma_s|^2}}$$

- The sign (+/-) chosen for the series line equation imposes the sign used for the shunt stub equation

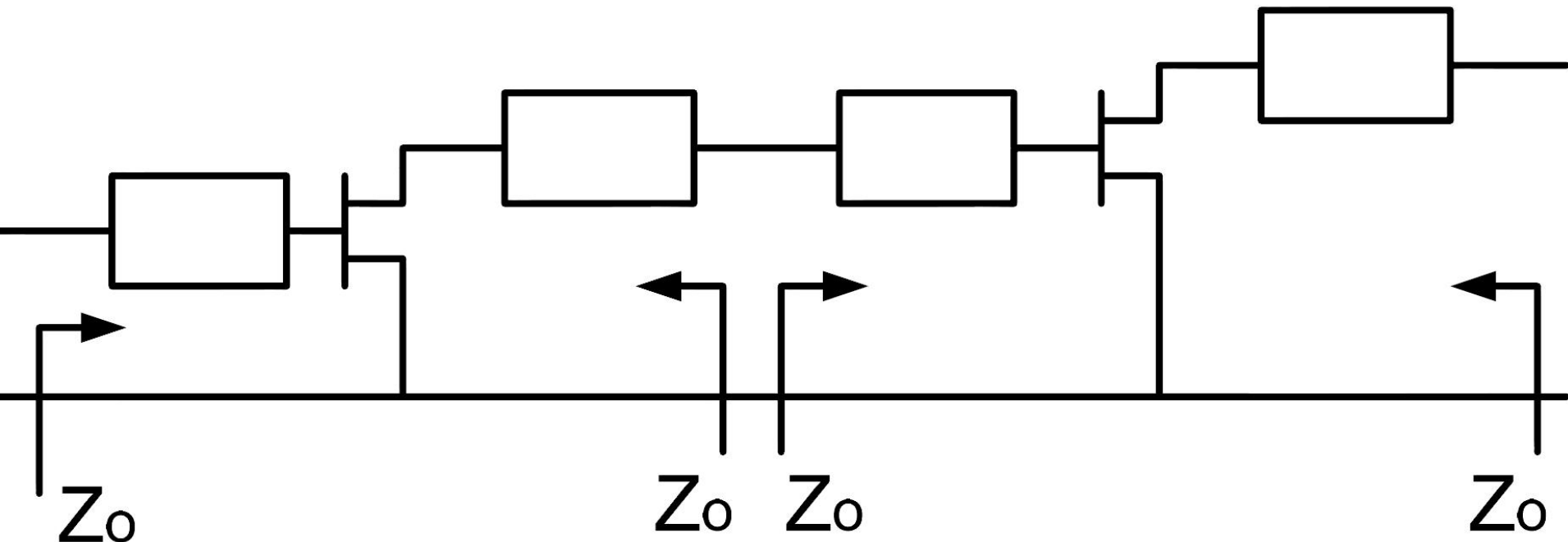


Multistage Amplifier Design

Microwave Amplifiers

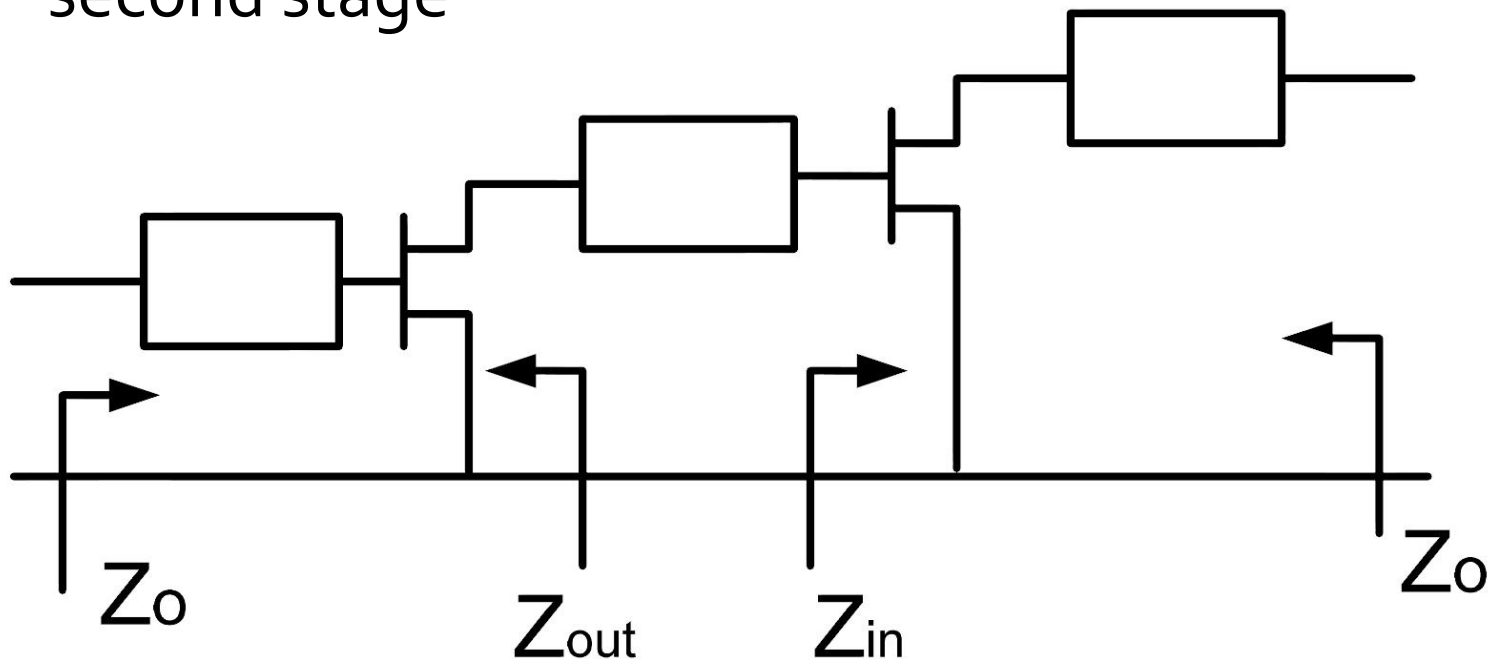
Multistage amplifiers

- Interstage matching can be designed in two modes:
 - Each stage is matched to a virtual $\Gamma = 0$



Multistage amplifiers

- Interstage matching can be designed in two modes:
 - One stage is matched to offer necessary Γ for the second stage

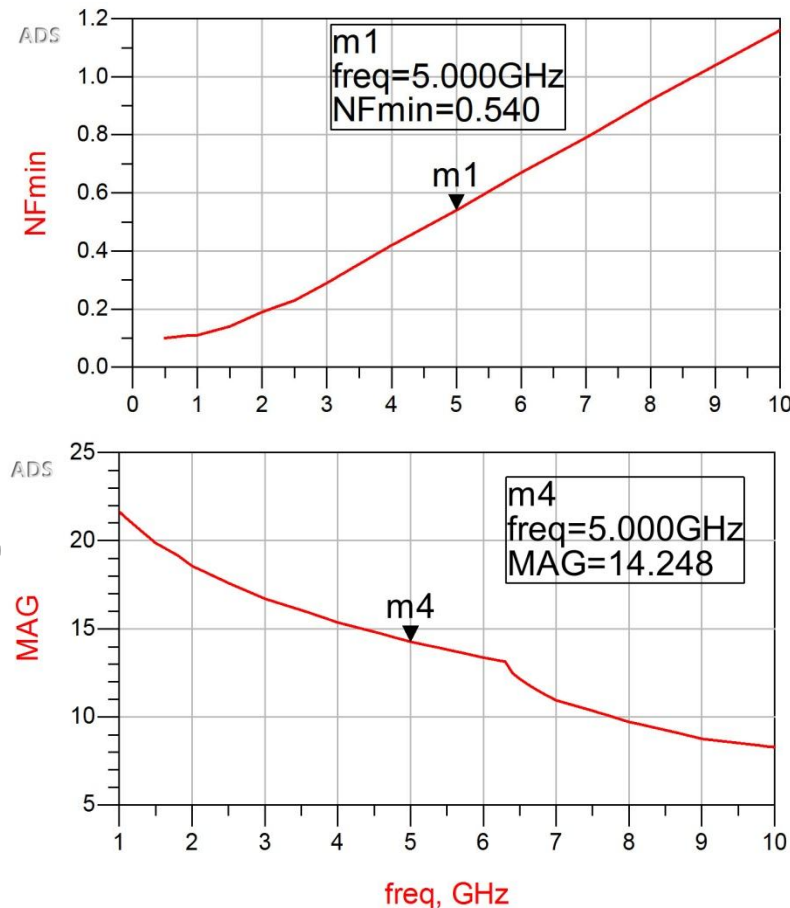


Example multistage LNA

- Similar to the homework
- LNA using ATF-34143 providing:
 - $G = 20\text{dB}$
 - $F = 1\text{dB}$
 - $@f = 5\text{GHz}$

Example

- ATF-34143 at $V_{ds}=3V$ $I_d=20mA$.
- @5GHz
 - $S_{11} = 0.64 \angle 139^\circ$
 - $S_{12} = 0.119 \angle -21^\circ$
 - $S_{21} = 3.165 \angle 16^\circ$
 - $S_{22} = 0.22 \angle 146^\circ$
 - $F_{min} = 0.54$ (typically[dB] !)
 - $\Gamma_{opt} = 0.45 \angle 174^\circ$
 - $r_n = 0.03$



Multistage amplifiers

- If we need more power gain than only one transistor can supply
 - necessary 20dB
 - $MAG @ 5GHz = 14.248 \text{ dB} < 20\text{dB}$
- We use Friis formula to divide the necessary:
 - Power gain
 - Noise
- between two amplifier stages

Friis Formula (noise)

$$F_{cas} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 \cdot G_2} + \frac{F_4 - 1}{G_1 \cdot G_2 \cdot G_3} + \dots$$

- Effects of Friis Formula:
 - it's essential that the first stage is as **noiseless** as possible even if that means sacrificing power
 - the second stage can be optimized for power **gain**
- Friis Formula **must** be used in **linear scale!**
- **Avago/Broadcom AppCAD**
 - AppCAD Free Design Assistant Tool for Microsoft Windows → Google

Friis Formula (noise)

$$G_{cas} = G_1 \cdot G_2$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1)$$

- Friis formula
 - first stage: low noise factor, probably resulting in a smaller gain
 - second stage: high gain, probably resulting in higher noise factor
- It's essential to introduce a design margin (reserve: ΔF , ΔG)
 - $G = G_{\text{design}} + \Delta G$
 - $F = F_{\text{design}} - \Delta F$
- Interpretation of the design target
 - $G > G_{\text{design}}$, better, but it's not required to sacrifice other parameters to maximize the gain
 - $F < F_{\text{design}}$, better, the smaller the better, we must target **the smallest possible noise** factor as long as the other design parameters **are met**

Friis Formula (noise)

- Friis formula
 - first stage: low noise factor, probably resulting in a smaller gain
 - second stage: high gain, probably resulting in higher noise factor
- Division between the two stages (Estimated!)
 - input stage: $F_1 = 0.7 \text{ dB}$, $G_1 = 9 \text{ dB}$
 - output stage: $F_2 = 1.2 \text{ dB}$, $G_2 = 13 \text{ dB}$
- To verify the result apply Friis formula
- First transform to **linear scale** !

$$F_1 = 10^{\frac{F_1[\text{dB}]}{10}} = 10^{0.07} = 1.175$$

$$F_2 = 10^{\frac{F_2[\text{dB}]}{10}} = 10^{0.12} = 1.318$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1) = 1.215$$

$$F_{cas} = 10 \cdot \log(1.215) = 0.846 \text{ dB}$$

$$G_1 = 10^{\frac{G_1[\text{dB}]}{10}} = 10^{0.9} = 7.943$$

$$G_2 = 10^{\frac{G_2[\text{dB}]}{10}} = 10^{1.3} = 19.953$$

$$G_{cas} = G_1 \cdot G_2 = 158.49$$

$$G_{cas} = 10 \cdot \log(158.49) = 22 \text{ dB}$$

Friis Formula (noise)

■ Avago/Broadcom AppCAD

AppCAD - [NoiseCalc]

File Calculate Application Examples Options Help

NoiseCalc Set Number of Stages = 2 Calculate [F4]

Stage Data	Units	Stage 1	Stage 2
Stage Name:		Avago Duplexer	Avago ATF-36xxx
Noise Figure	dB	0.7	1.2
Gain	dB	9	13
Output IP3	dBm	100	14.5
dNF/dTemp	dB/°C	0	0
dG/dTemp	dB/°C	0	0

Stage Analysis:

NF (Temp corr)	dB	0.70	1.20
Gain (Temp corr)	dB	9.00	13.00
Input Power	dBm	-50.00	-41.00
Output Power	dBm	-41.00	-28.00
d NF/d NF	dB/dB	0.97	0.15
d NF/d Gain	dB/dB	-0.03	0.00
d IP3/d IP3	dBm/dBm	0.00	1.00

Enter System Parameters:

Input Power	-50	dBm
Analysis Temperature	25	°C
Noise BW	1	MHz
Ref Temperature	25	°C
S/N (for sensitivity)	10	dB
Noise Source (Ref)	290	°K

System Analysis:

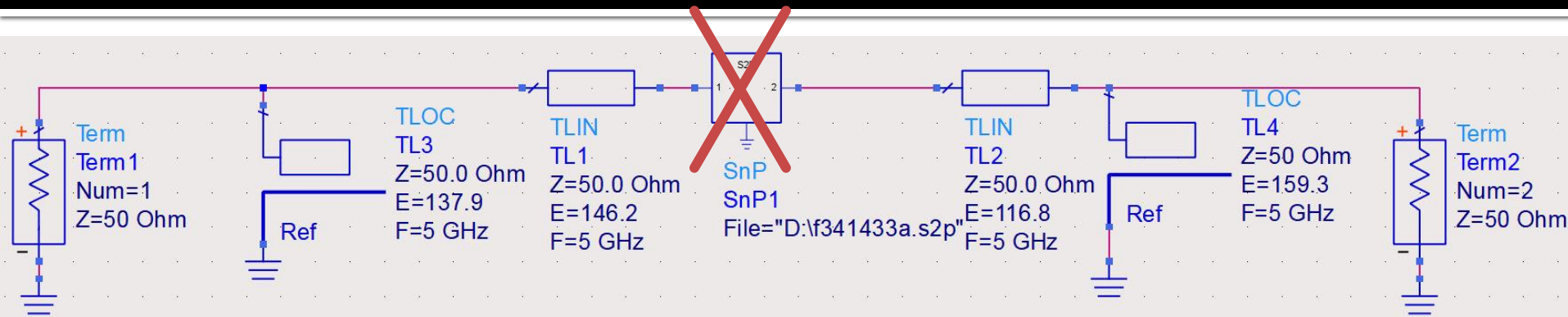
Gain =	22.00	dB
Noise Figure =	0.85	dB
Noise Temp =	82.34	°K
SNR =	63.13	dB
MDS =	-113.13	dBm
Sensitivity =	-103.13	dBm
Noise Floor =	-173.13	dBm/Hz

Input IP3 =	-7.50	dBm
Output IP3 =	14.50	dBm
Input IM level =	-135.00	dBm
Input IM level =	-85.00	dbc
Output IM level =	-113.00	dBm
Output IM level =	-85.00	dbc
SFDR =	70.42	dB

Multistage amplifier design

- Division between the two stages (Estimated!)
 - input stage: $F_1 = 0.7$ dB, $G_1 = 9$ dB
 - output stage: $F_2 = 1.2$ dB, $G_2 = 13$ dB
 - total: $F = 0.85$ dB, $G = 22$ dB
- Meets design specifications (with design margin)
- We can reuse the single stage LNA design (Lecture 9)
 - input matching (LNA L₉) can be used for the input of the first stage – very low noise, good enough power gain
 - output matching (LNA L₉) was designed for maximum gain, can be used for the output of the second stage
 - input and output matching in L₉ were designed for 50Ω source and load, similar to current conditions

Input and output matching, stubs



$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

$$\text{Im}[y_S(\theta)] = \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$(\varphi + 2\theta) = \begin{cases} +114.33^\circ \\ -114.33^\circ \end{cases} \quad \theta = \begin{cases} 146.2^\circ \\ 31.8^\circ \end{cases}$$

$$\text{Im}[y_S(\theta)] = \begin{cases} -0.904 \\ +0.904 \end{cases} \quad \theta_{sp} = \begin{cases} 137.9^\circ \\ 42.1^\circ \end{cases}$$

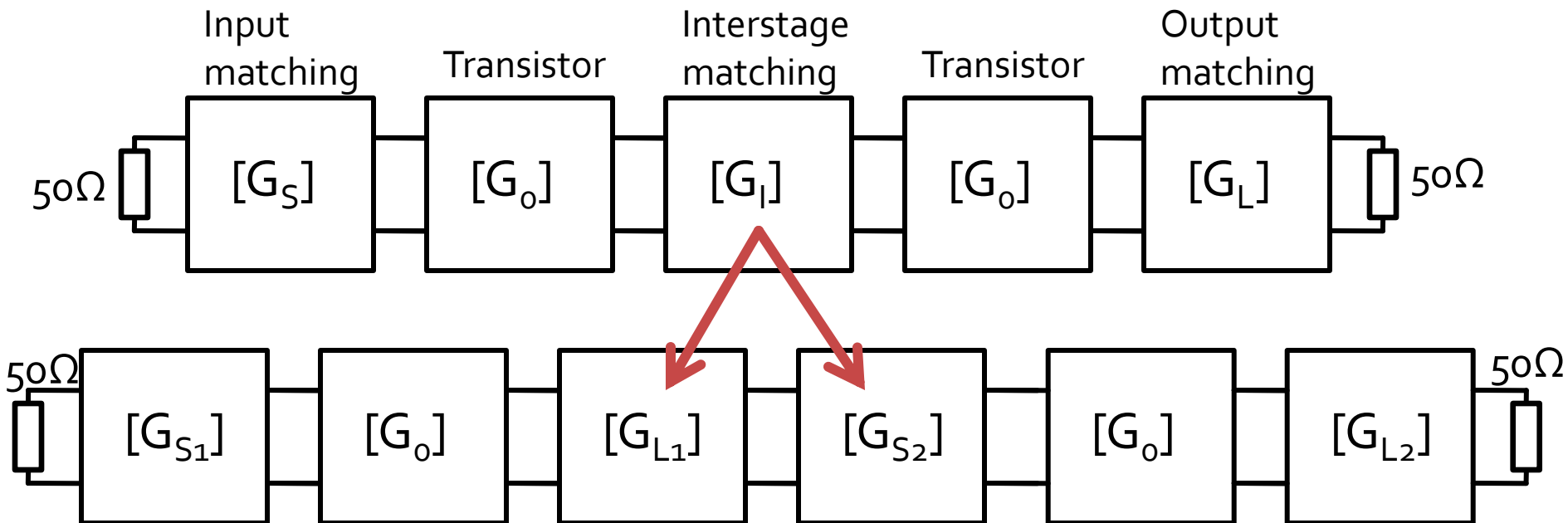
$$\cos(\varphi + 2\theta) = -|\Gamma_L|$$

$$\text{Im}[y_L(\theta)] = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -0.379$$

$$(\varphi + 2\theta) = \begin{cases} +100.72^\circ \\ -100.72^\circ \end{cases} \quad \theta = \begin{cases} 116.8^\circ \\ 16.1^\circ \end{cases}$$

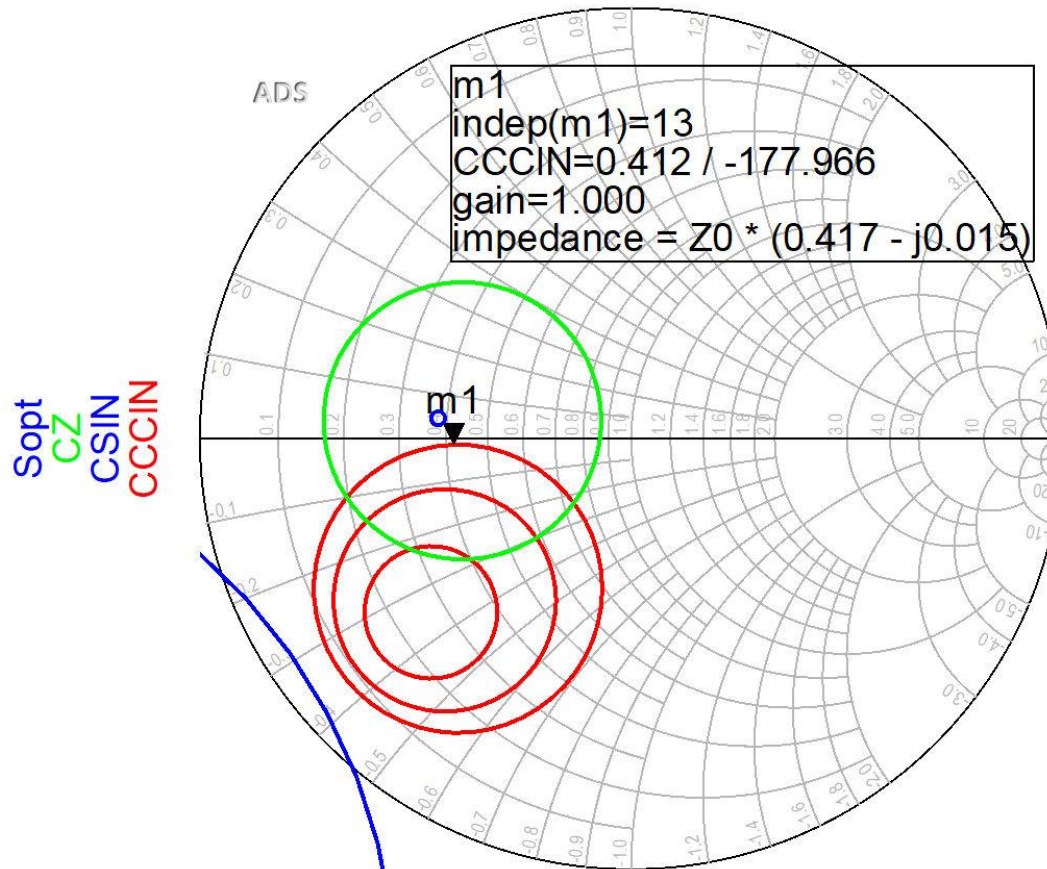
$$\text{Im}[y_L(\theta)] = \begin{cases} -0.379 \\ +0.379 \end{cases} \quad \theta_{sp} = \begin{cases} 159.3^\circ \\ 20.7^\circ \end{cases}$$

Multistage amplifier design



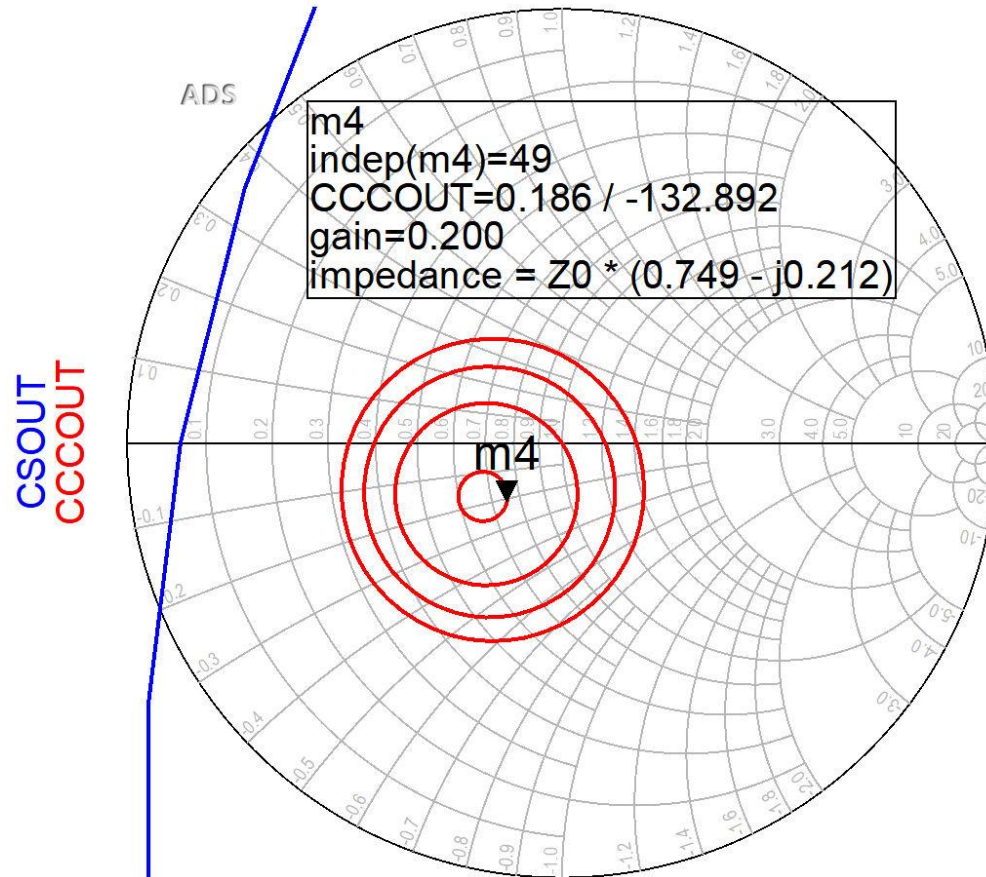
- Gain computation
 - Interstage matching can supplement the gain for both amplifier stages
 - The design for input and output matching must be achieved on a single transistor schematic (recommended: easier)

Input matching circuit (L9)



- If we can afford a 1.2dB decrease of the input gain for better NF, Q ($G_s = 1$ dB), position m1 above is better
- We obtain better (smaller) NF

Output matching circuit (Lg)



- output constant gain circles CCCOUT: -0.4dB, -0.2dB, 0dB, +0.2dB
- The lack of noise restrictions allows optimization for better gain (close to maximum – position m4)

Proiectare etaje cascade

- Power gain

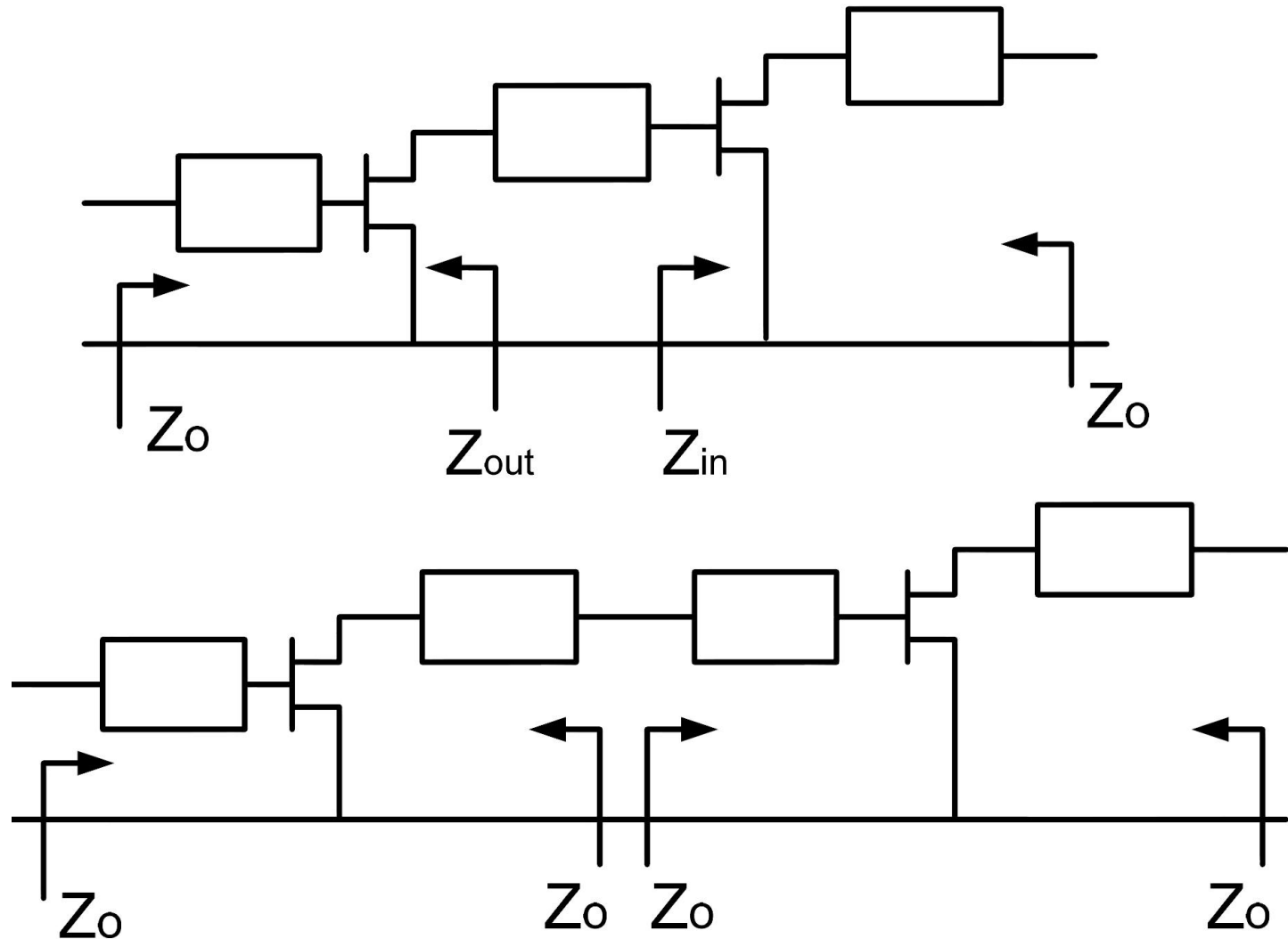
$$G_T[dB] = G_{S1}[dB] + G_0[dB] + G_{L1}[dB] + G_{S2}[dB] + G_0[dB] + G_{L2}[dB]$$

$$G_T[dB] = 1\text{ dB} + 10\text{ dB} + G_{L1}[dB] + G_{S2}[dB] + 10\text{ dB} + 0.2\text{ dB}$$

$$G_T[dB] = 21.2\text{ dB} + G_{L1}[dB] + G_{S2}[dB]$$

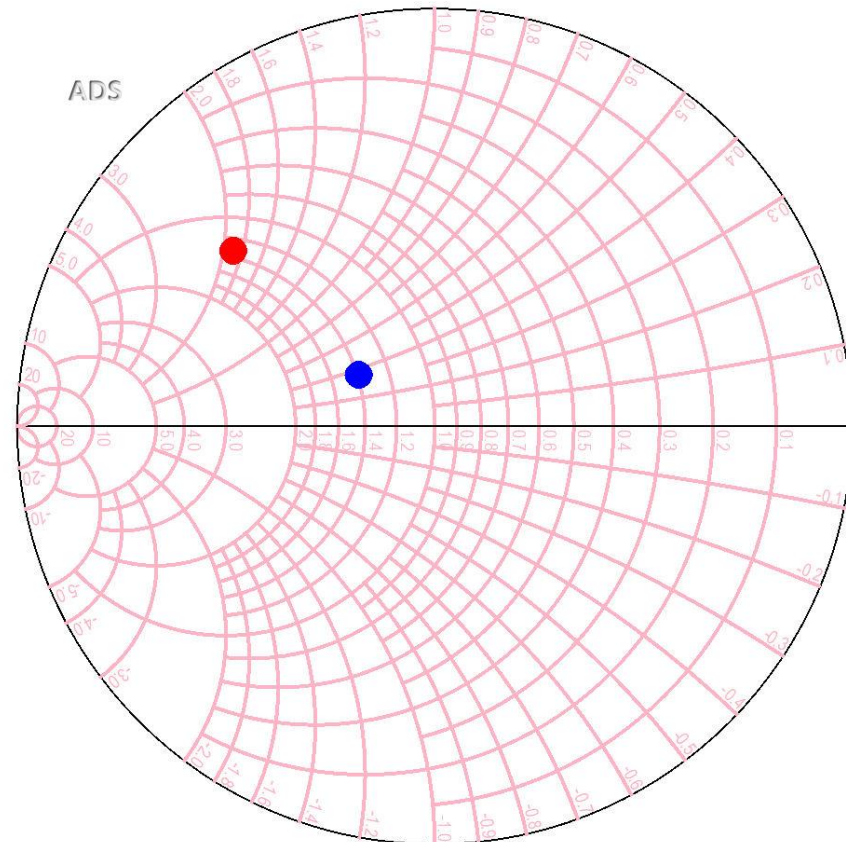
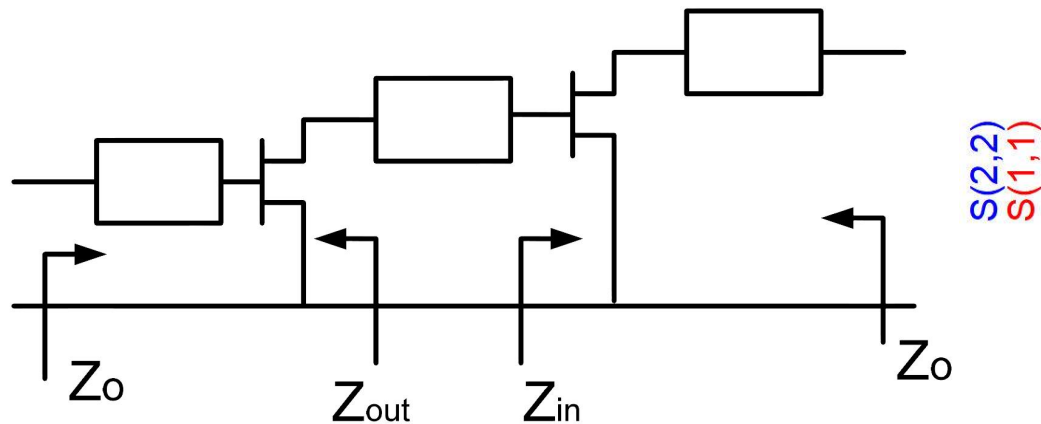
- Interstage design must provide at least 0.8dB gain to meet specifications, by better match for the output of the first transistor and for the input of the second transistor

Interstage matching 1/2



Interstage matching 1

- A single transmission line keeps constant the magnitude of the reflection coefficient
 - a circle around the Smith Chart center



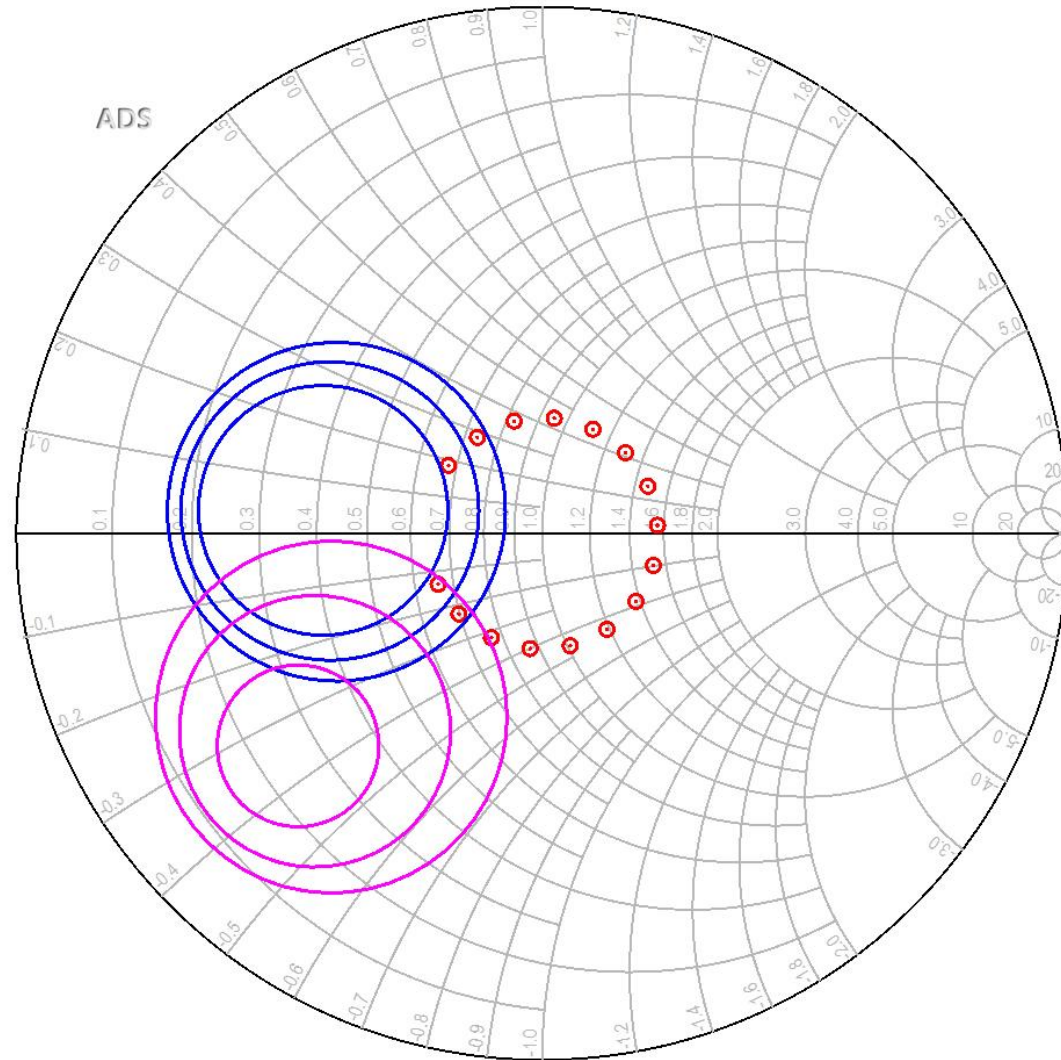
Interstage matching 1

- Dual design:
 - starting from the output of the first stage (reflection coefficient S_{22}) towards the circles (drawn for the second stage):
 - stability
 - gain
 - noise
 - starting from the input of the second stage (reflection coefficient S_{11}) towards the circles (drawn for the first stage):
 - stability
 - gain
- First design direction has the advantage to control the noise introduced by the second stage

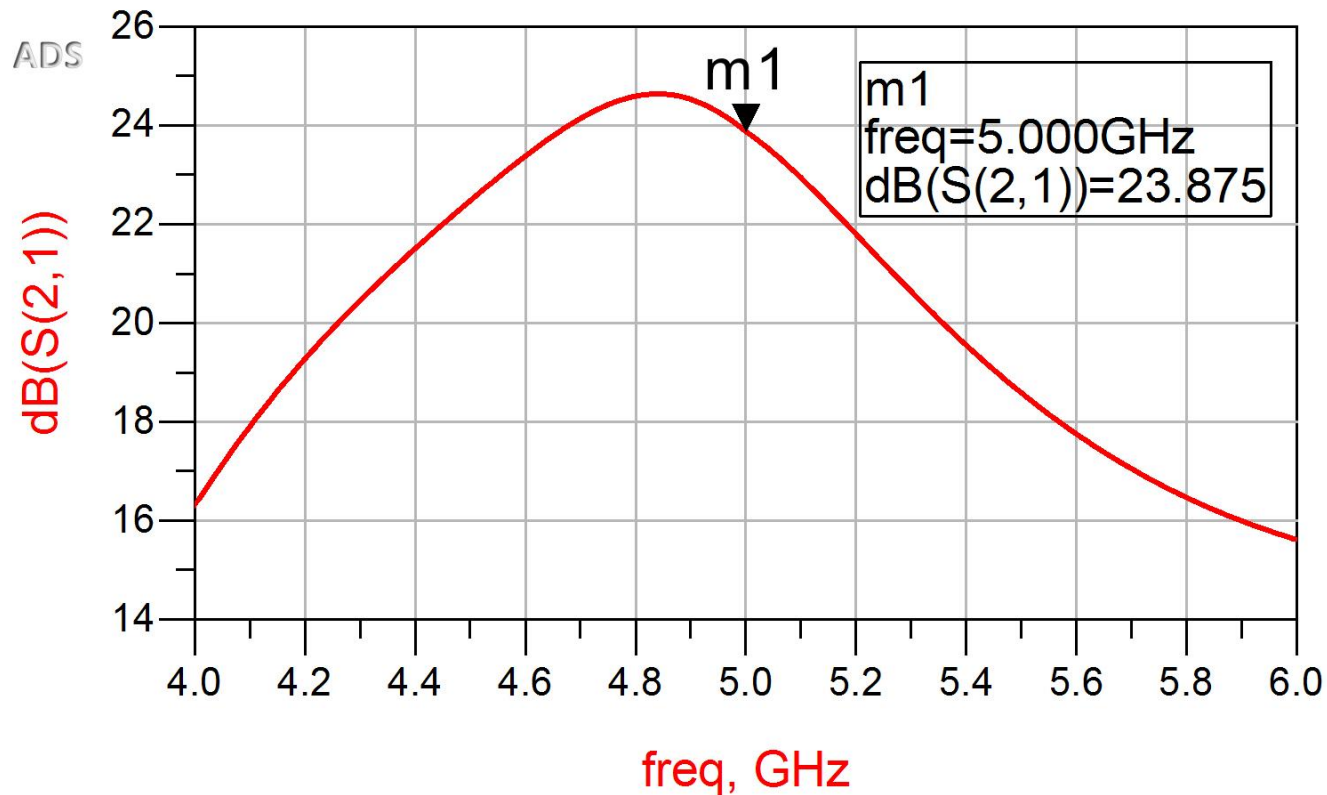
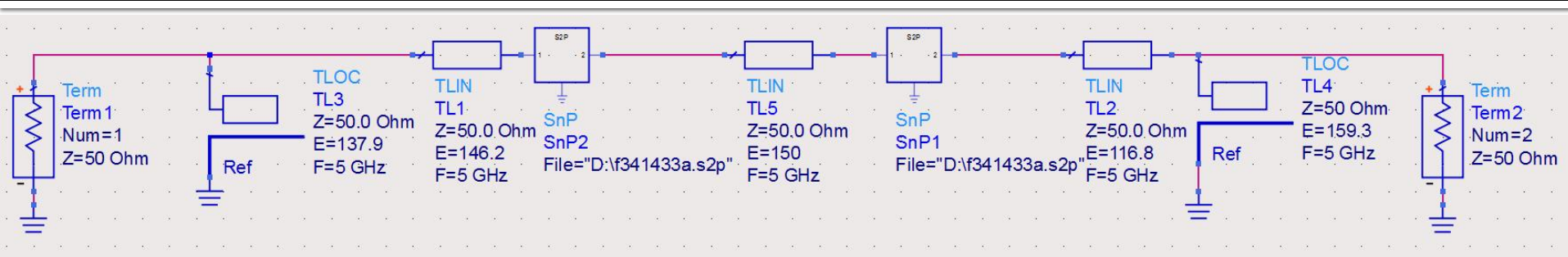
Interstage matching 1

- A **single** transmission line allows reaching a point that cannot be optimized
 - $G_{L1} = 0.2\text{dB (max)}$
 - $G_{S2} = \sim 1\text{ dB}$
 - $F_2 = \sim 0.65\text{ dB}$
- Only one parameter is available for wide band performance tuning

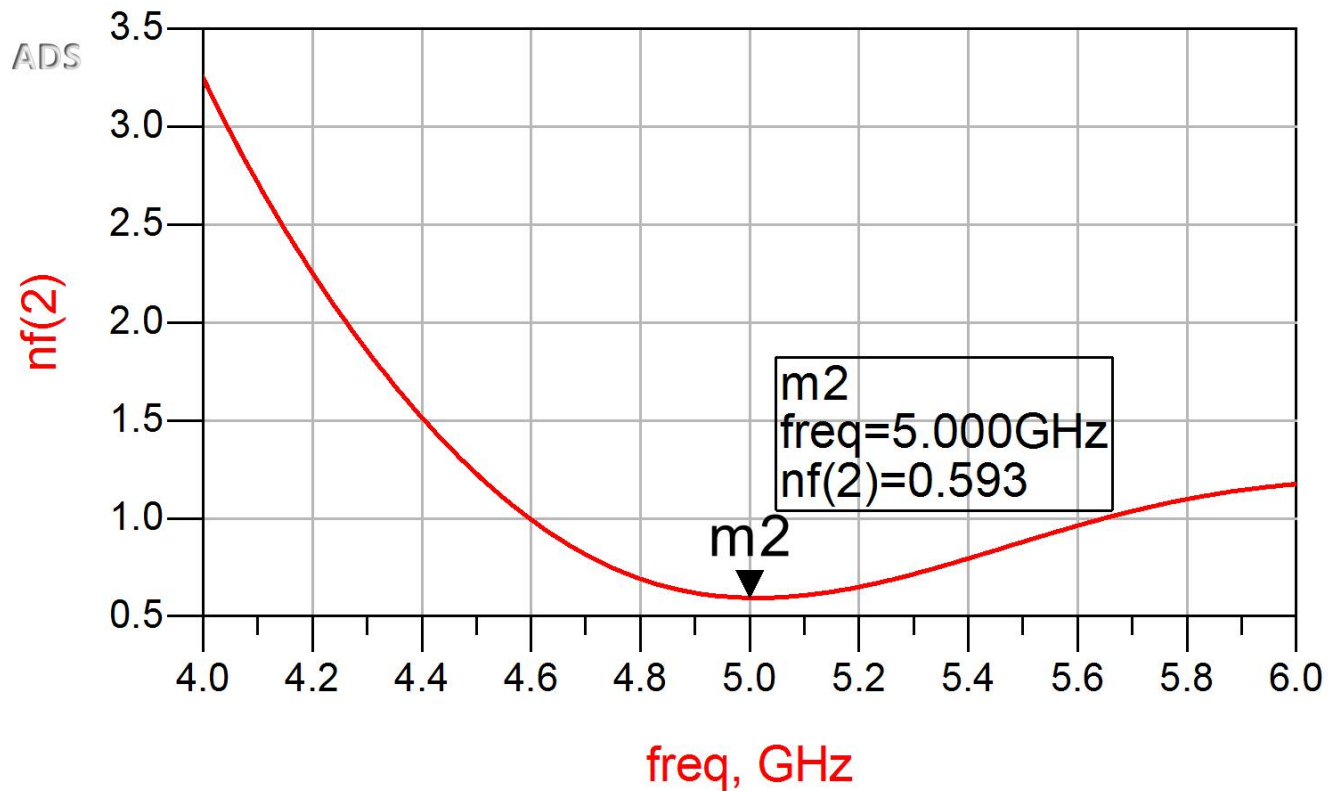
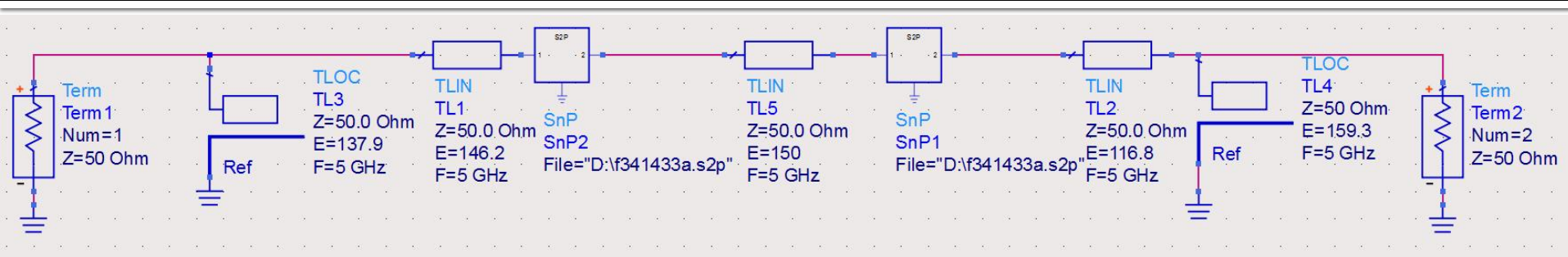
ref..CCCIN
ref..CZ
S(2,2)



ADS

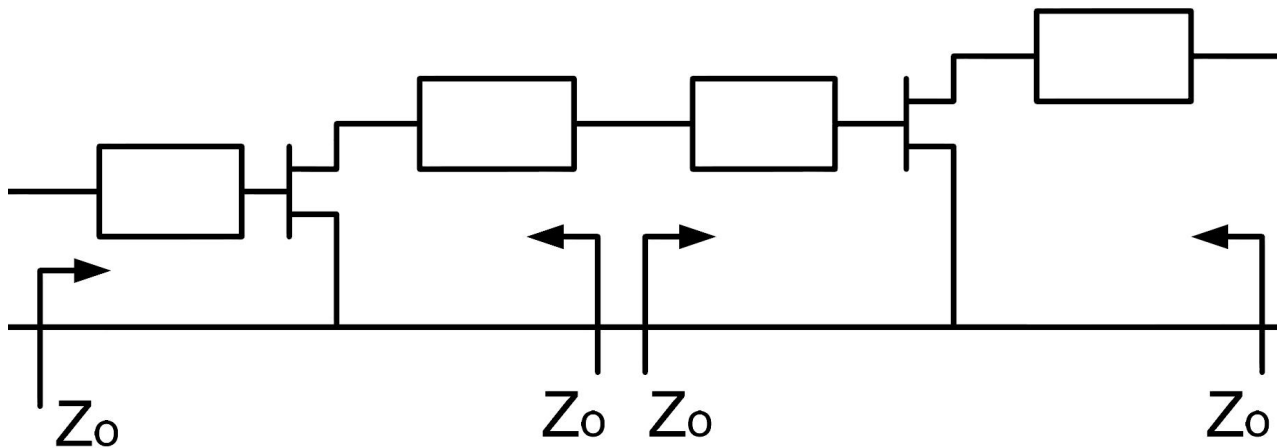


ADS



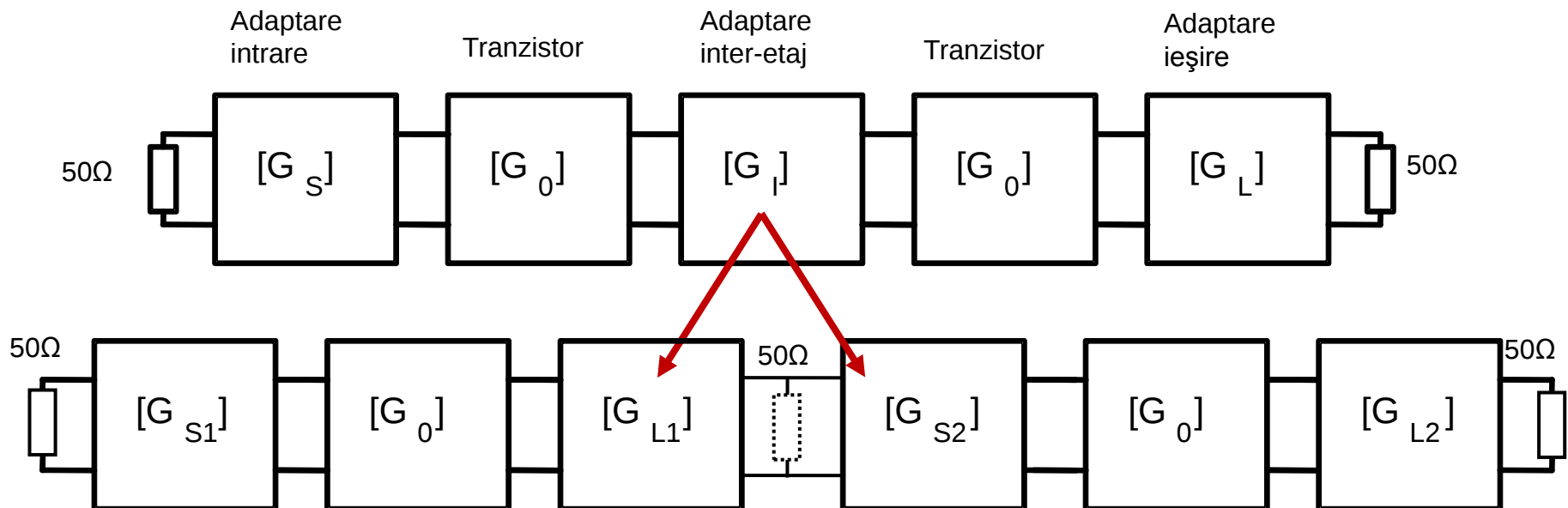
Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate $\Gamma=0$ (virtual) allows detailed control over final reflection coefficient



Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate $\Gamma=0$ (virtual) allows detailed control over final reflection coefficient

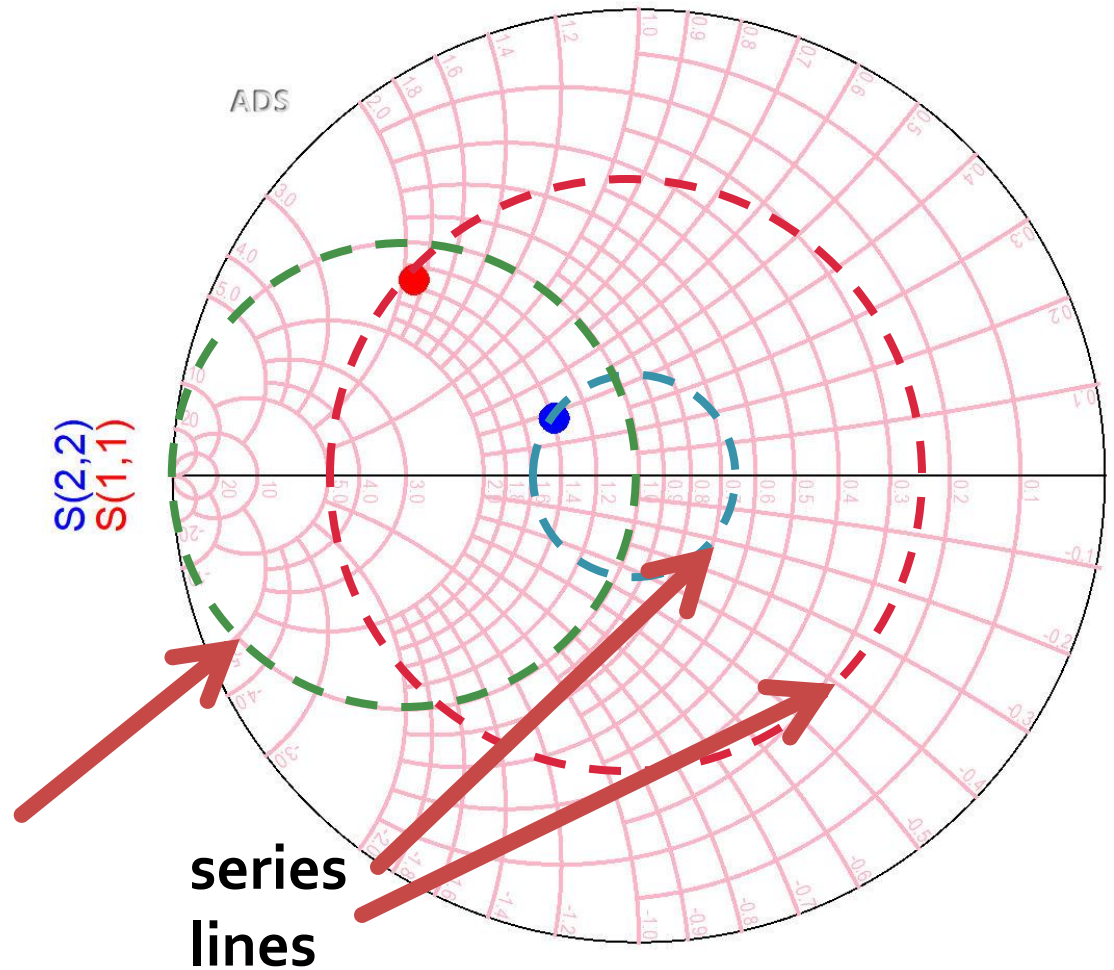


Smith Chart

- series line $\rightarrow$
moves around
the center of the
SC
- shunt stub $\rightarrow$ on
the circle $g=1$

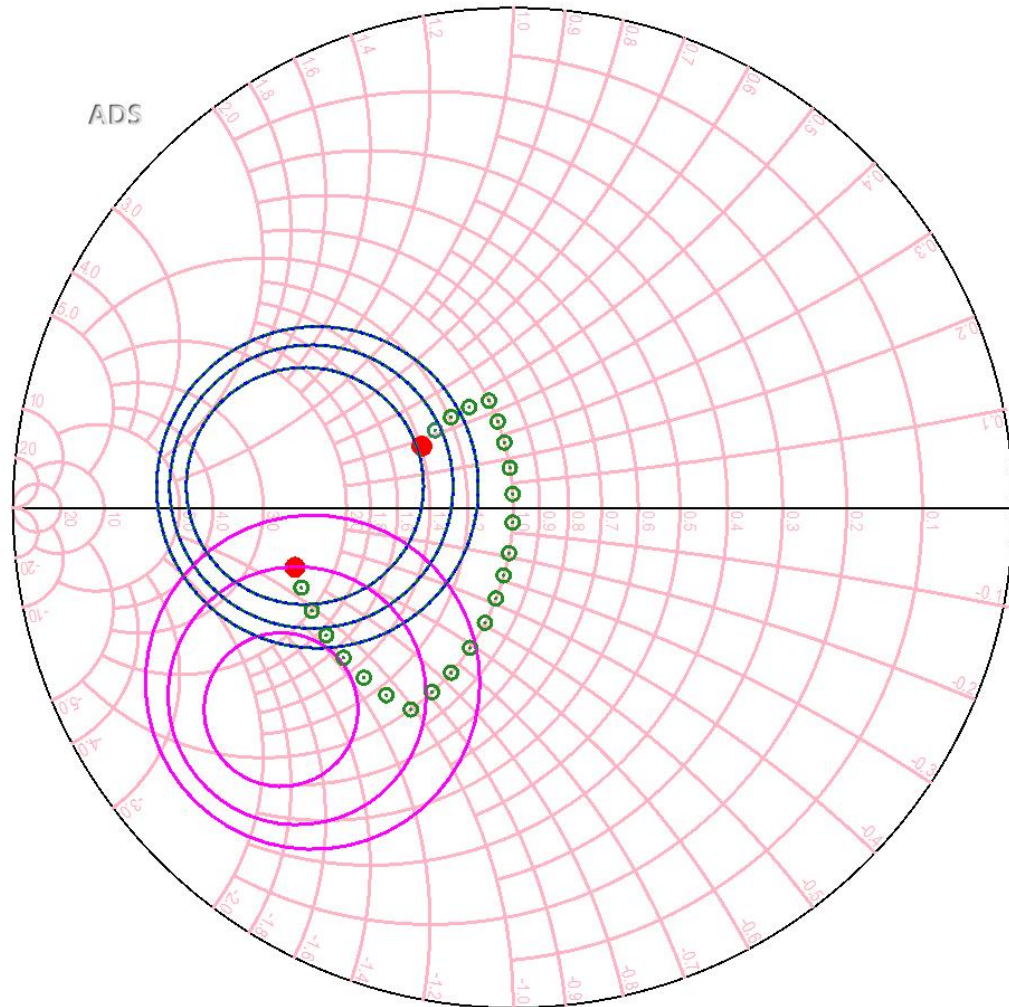
shunt
stub

series
lines



Adaptare inter-etaje

- For every stage we use a series line and a shunt stub
 - the series line moves the reflection coefficient from the desired starting point on the unity conductance circle $g=1$
 - the shunt stub moves the point to the center of the Smith Chart (Z_0 match)
- The two shunt stubs combine into one



Calcul analitic

- G_{L1} (plecare din S_{22} spre origine)

$$S_{22} = 0.22 \angle 146^\circ$$

$$|S_{22}| = 0.22; \quad \varphi = 146^\circ$$

$$\cos(\varphi + 2\theta) = -|S_{22}|$$

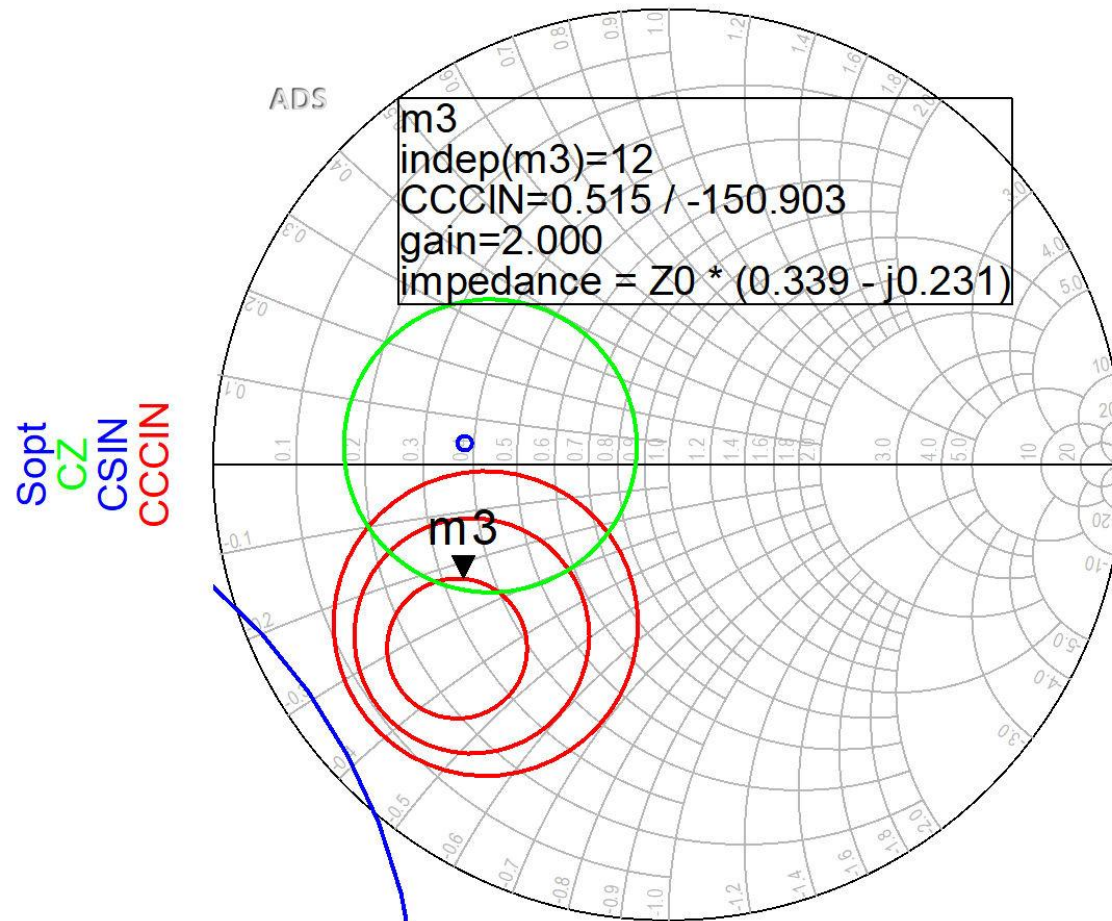
$$\operatorname{Im}[y_{L1}(\theta)] = \frac{\mp 2 \cdot |S_{22}|}{\sqrt{1 - |S_{22}|^2}}$$

$$\cos(\varphi + 2\theta) = -0.22 \Rightarrow (\varphi + 2\theta) = \pm 102.71^\circ$$

$$(\varphi + 2\theta) = \begin{cases} +102.71^\circ \\ -102.71^\circ \end{cases} \quad \theta = \begin{cases} 158.4^\circ \\ 55.6^\circ \end{cases} \quad \operatorname{Im}[y_{L1}(\theta)] = \begin{cases} -0.451 \\ +0.451 \end{cases} \quad \theta_{sp} = \begin{cases} 155.7^\circ \\ 24.3^\circ \end{cases}$$

Calcul analitic

- G_{S_2} (plecare din Γ_{S_2} ales spre origine – castig 2dB)



Calcul analitic

- G_{S_2} (plecare din 2 spre origine)

$$\Gamma_{S_2} = 0.515 \angle -150.9^\circ$$

$$|\Gamma_{S_2}| = 0.515; \quad \varphi = -150.9^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_{S_2}| \quad \text{Im}[y_{S_2}(\theta)] = \frac{\mp 2 \cdot |\Gamma_{S_2}|}{\sqrt{1 - |\Gamma_{S_2}|^2}}$$

$$\cos(\varphi + 2\theta) = -0.515 \Rightarrow \quad (\varphi + 2\theta) = \pm 121^\circ$$

$$(\varphi + 2\theta) = \begin{cases} +121^\circ \\ -121^\circ \end{cases} \quad \theta = \begin{cases} 135.9^\circ \\ 15^\circ \end{cases} \quad \text{Im}[y_{S_2}(\theta)] = \begin{cases} -1.202 \\ +1.202 \end{cases} \quad \theta_{sp} = \begin{cases} 129.8^\circ \\ 50.2^\circ \end{cases}$$

Calcul analitic

- **Cele doua stub-uri in gol se combina intr-unul singur**
- Exista **4 combinatii posibile** in functie de cum se combina lungimile electrice ale celor doua linii serie
 - pentru fiecare lungime electrica aleasa (θ) se foloseste obligatoriu $\text{Im}[y(\theta)]$ corespunzator
- Ex:

$$\theta_{L1} = 158.4^\circ \quad \theta_{S2} = 135.9^\circ \quad \text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.653$$
$$\theta_{sp} = \tan^{-1}(\text{Im}[y_{sp}]) \quad \theta_{sp} = 121.2^\circ$$

Diagrama Smith

- linie serie $\rightarrow$ pe cercul cu centrul in originea DS
- stub paralel $\rightarrow$ pe cercul $g=1$

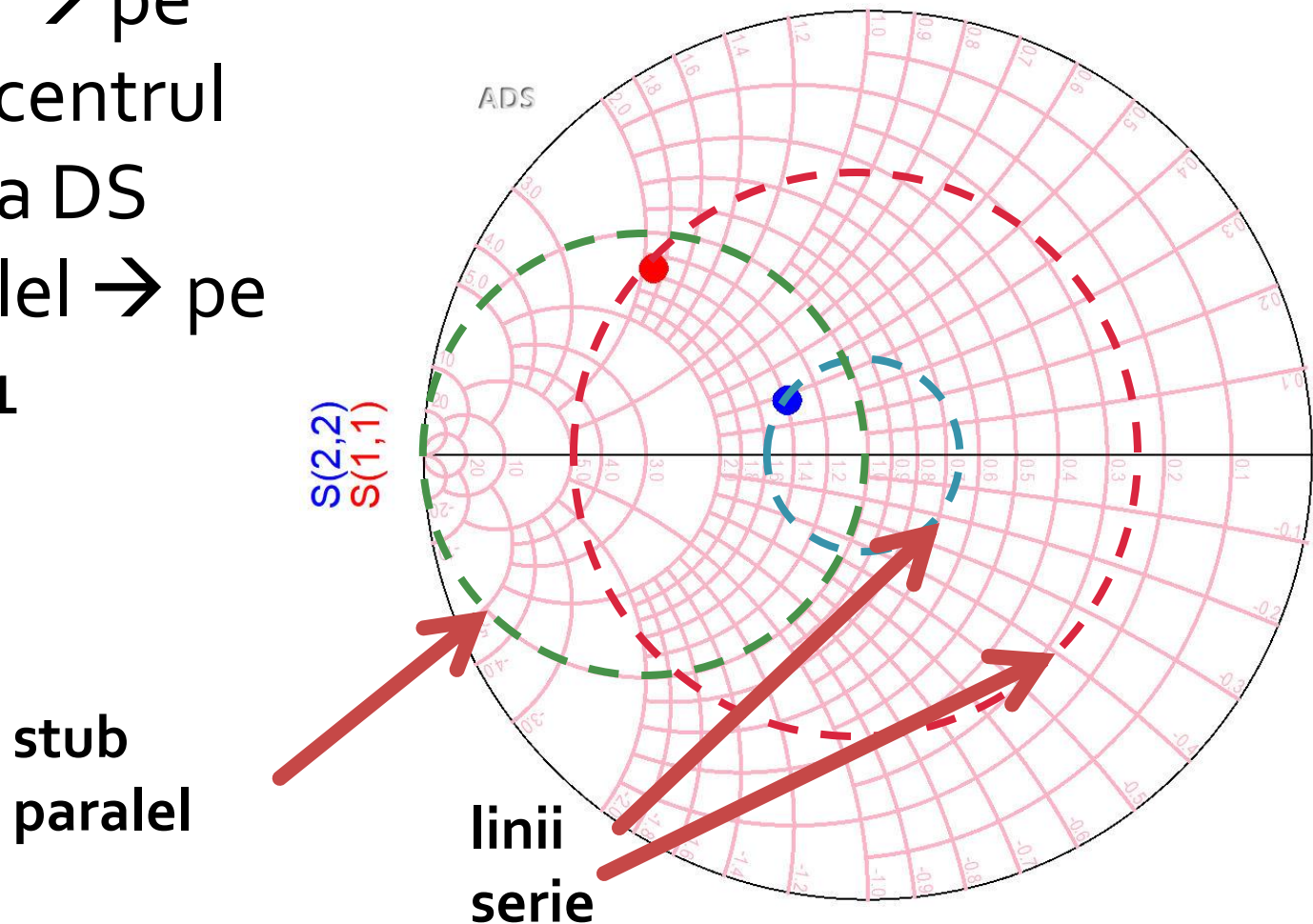


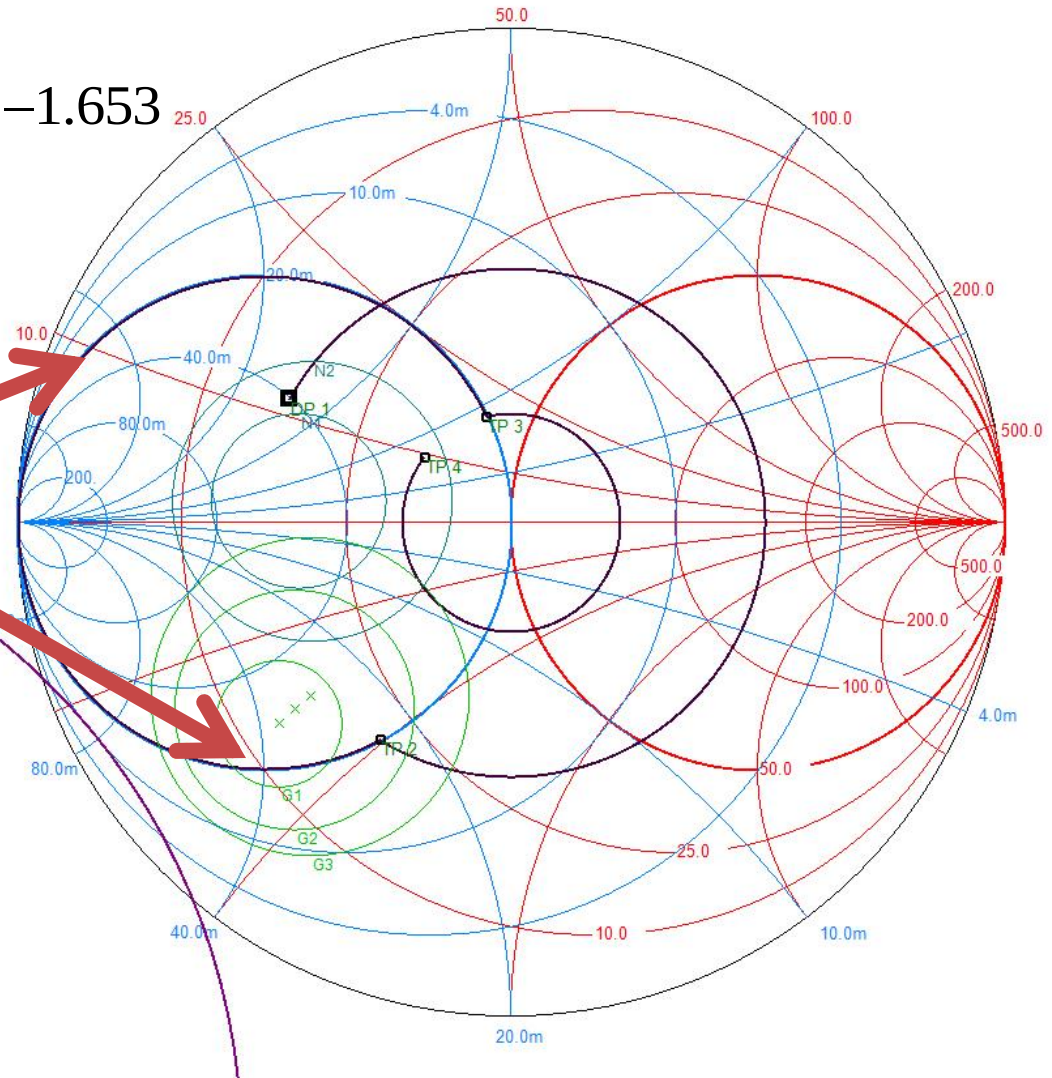
Diagrama Smith 1

$$\theta_{L1} = 158.4^\circ \quad \theta_{S2} = 135.9^\circ$$

$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.653$$

$$\theta_{sp} = 121.2^\circ$$

stub
"combinat"



ADS 1

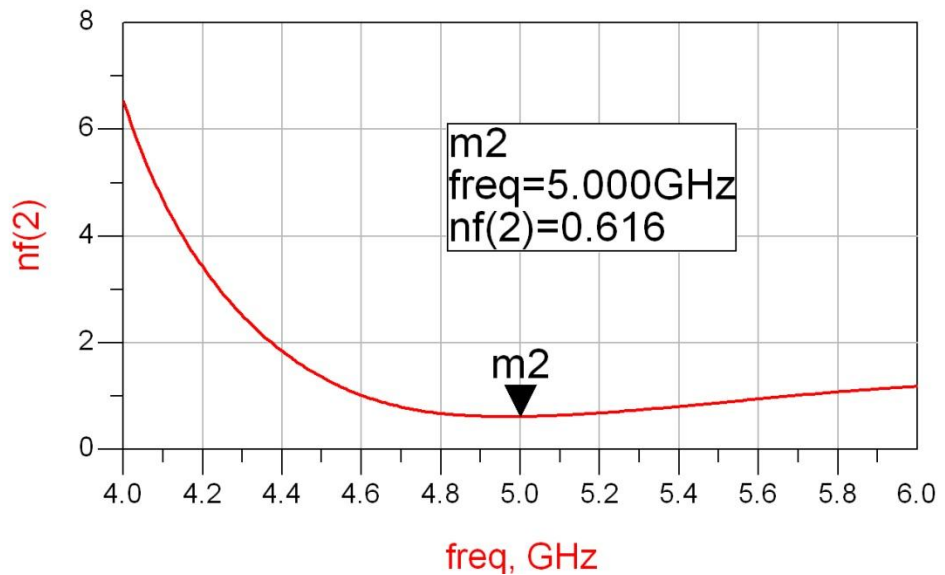
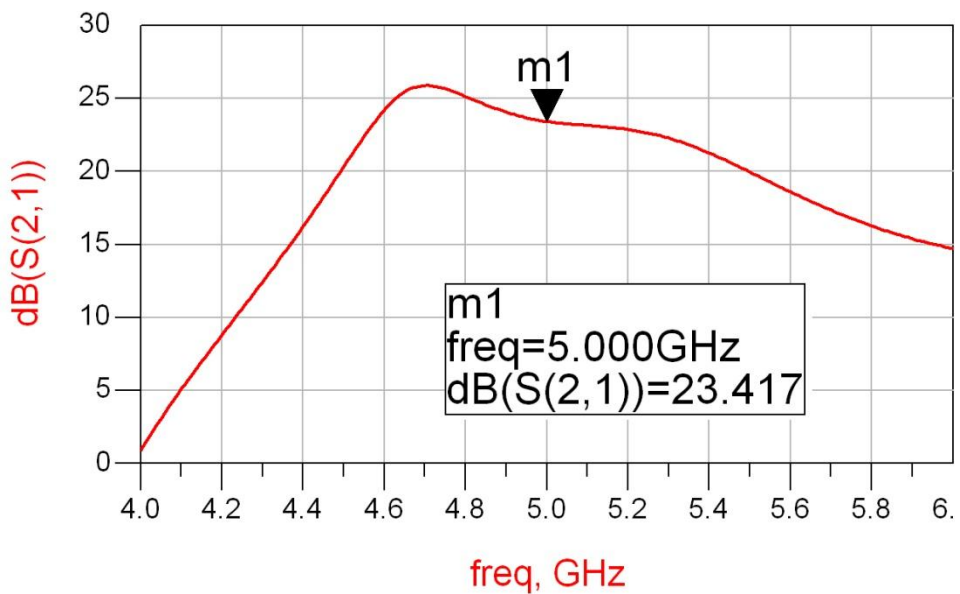
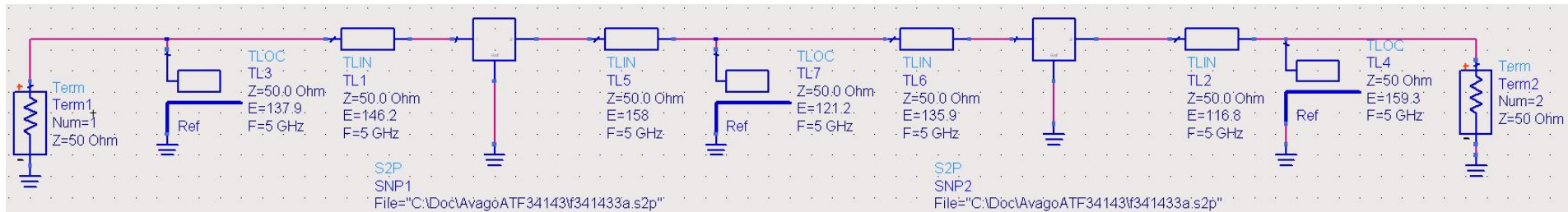


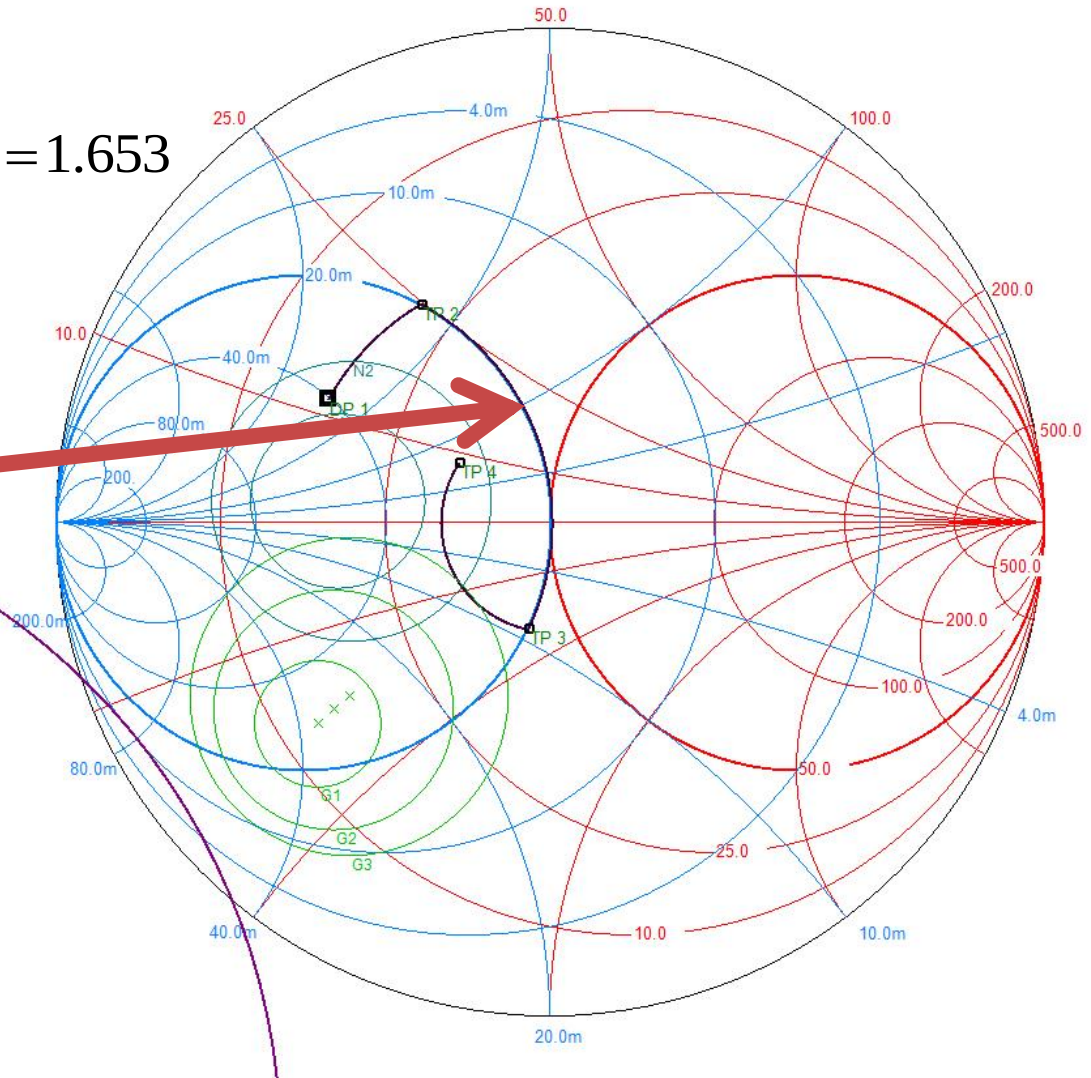
Diagrama Smith 2

$$\theta_{L1} = 55.6^\circ \quad \theta_{S2} = 15^\circ$$

$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = 1.653$$

$$\theta_{sp} = 58.8^\circ$$

stub
"combinat"



ADS 2

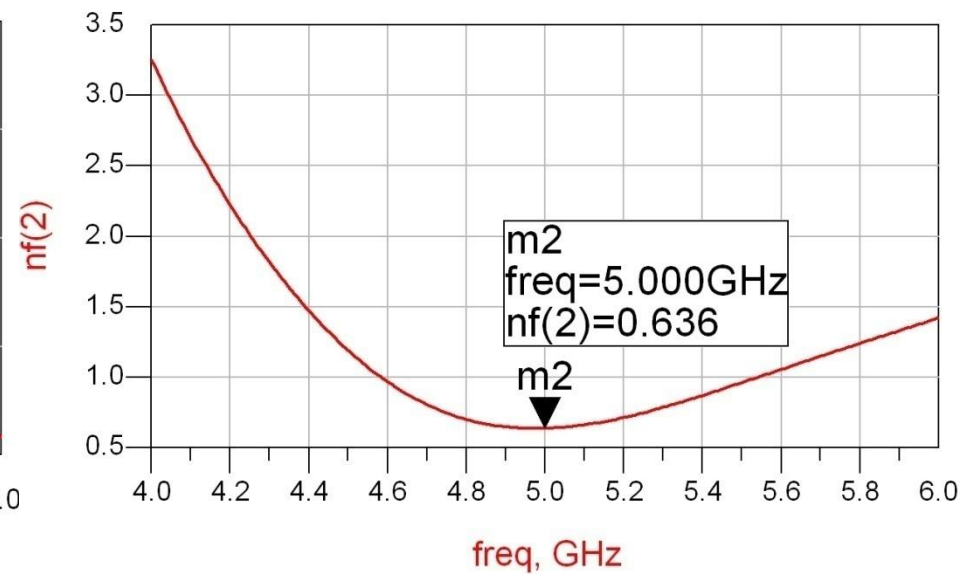
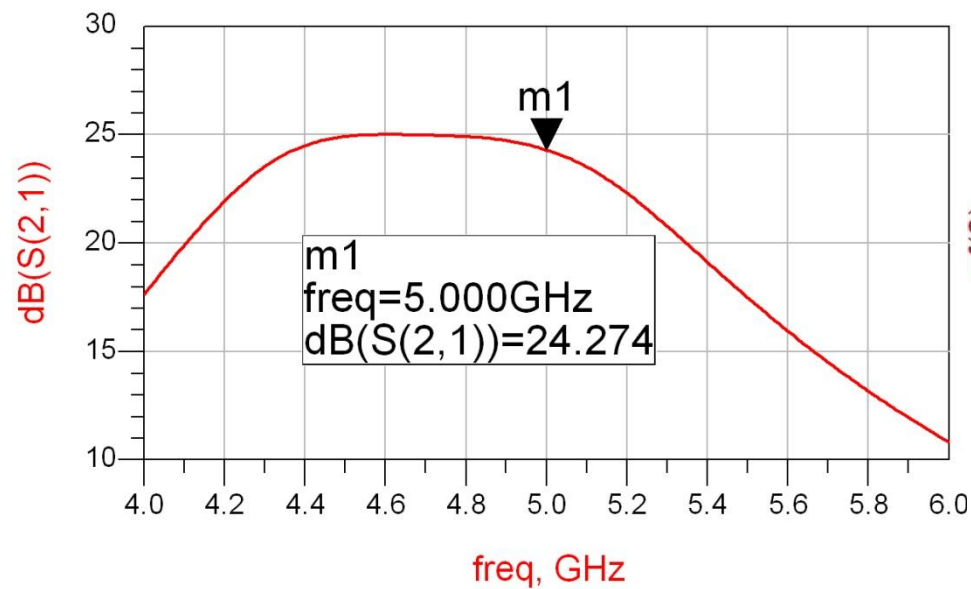
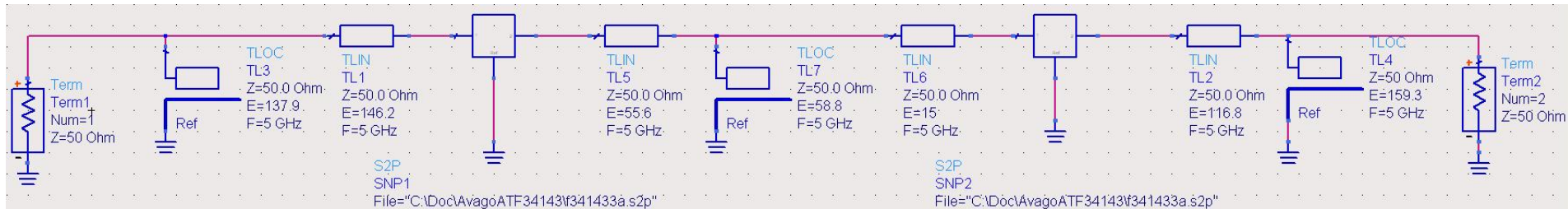


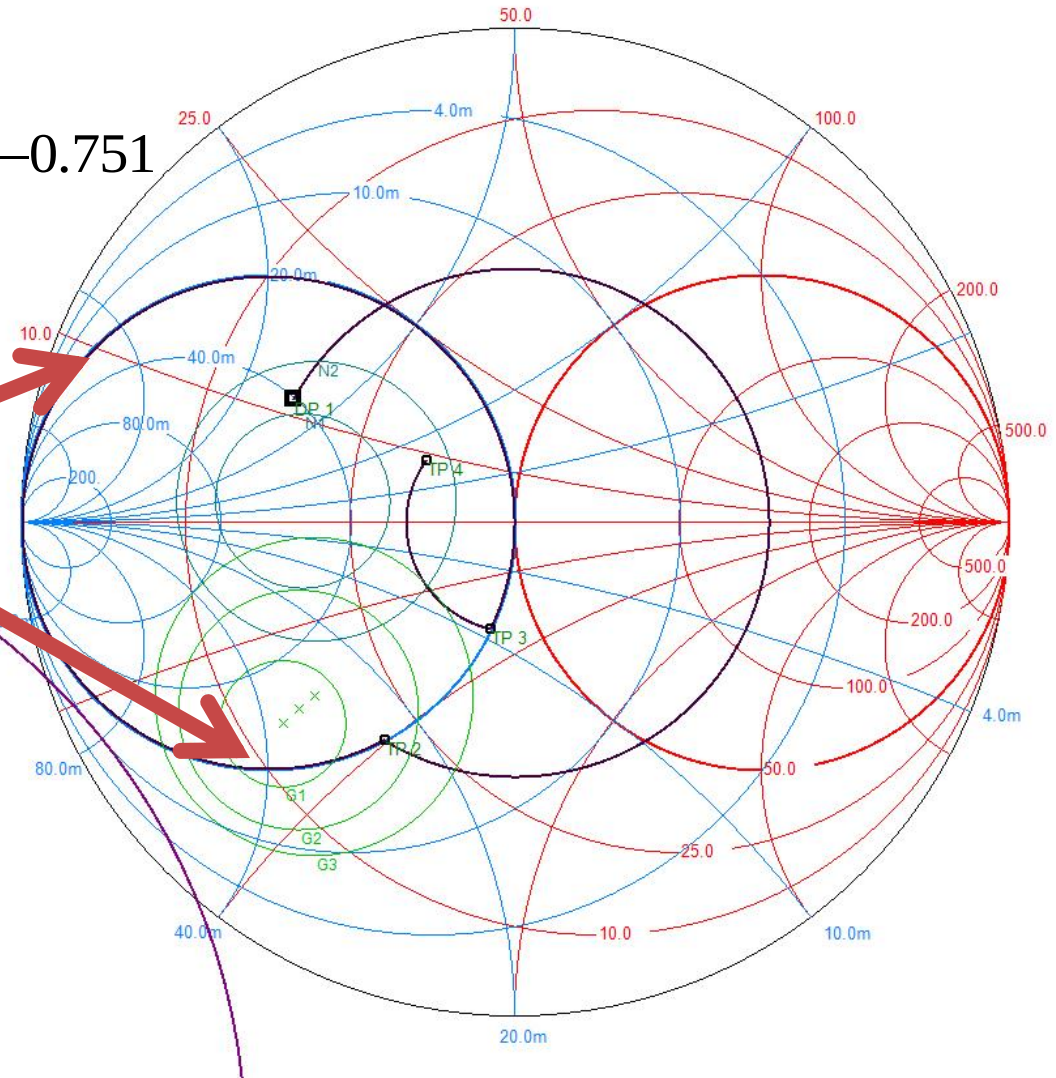
Diagrama Smith 3

$$\theta_{L1} = 55.6^\circ \quad \theta_{S2} = 135.9^\circ$$

$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -0.751$$

$$\theta_{sp} = 143.1^\circ$$

stub
"combinat"



ADS 3

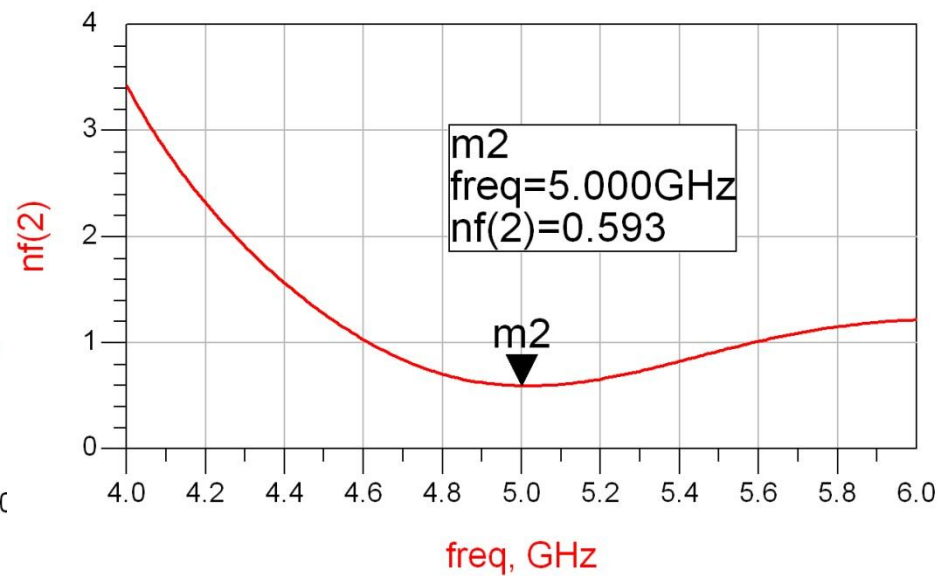
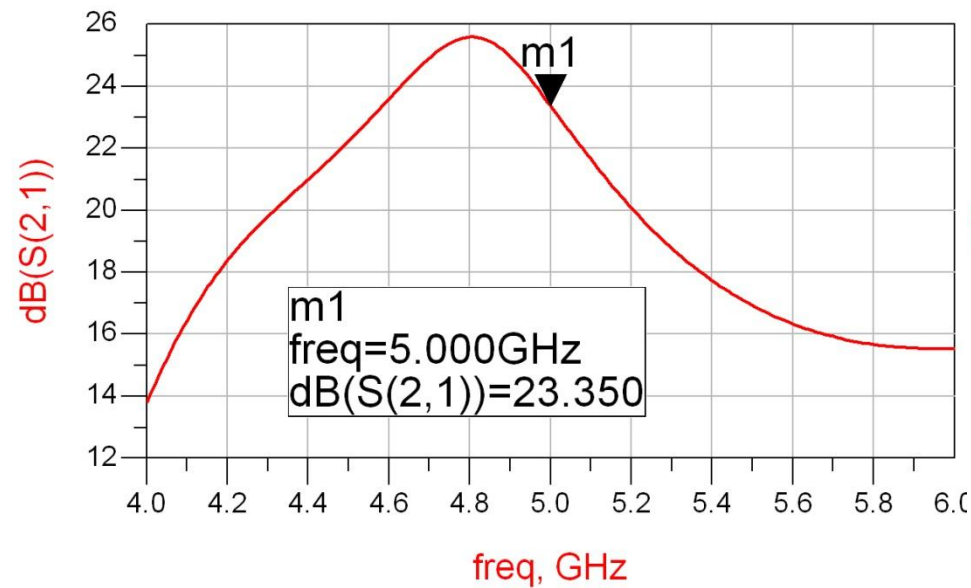
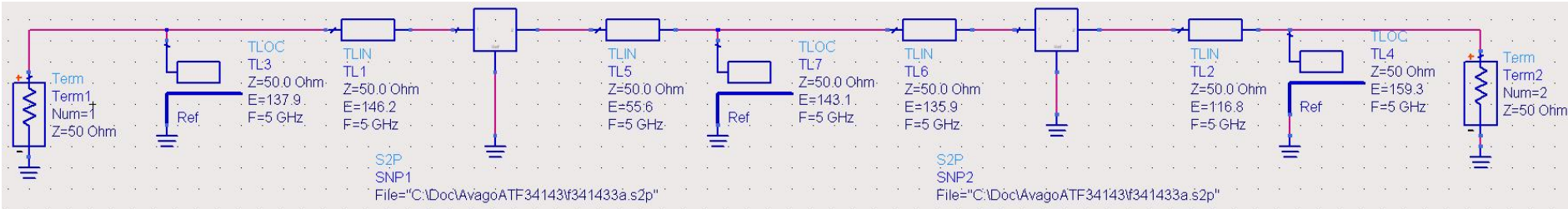


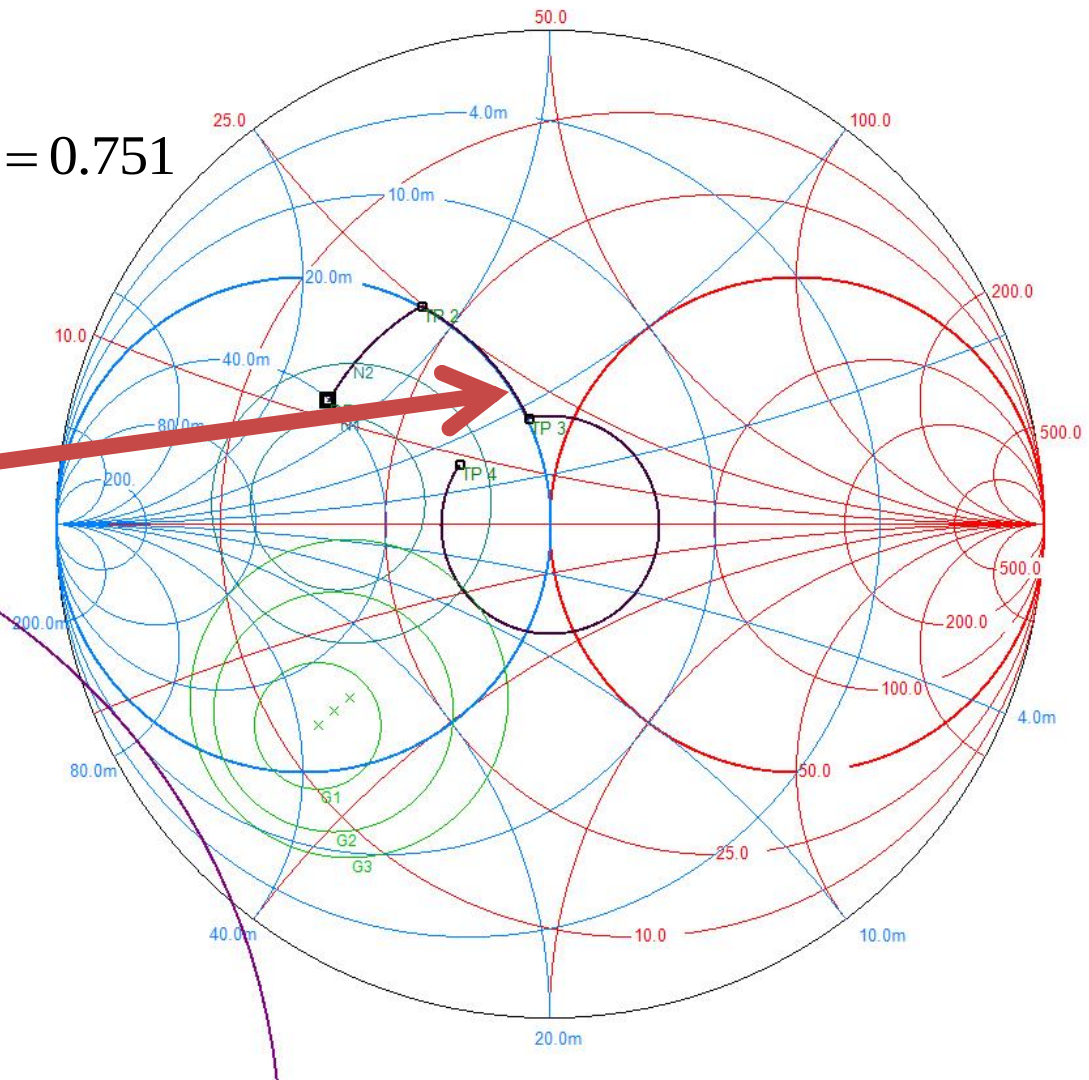
Diagrama Smith 4

$$\theta_{L1} = 158.4^\circ \quad \theta_{S2} = 15^\circ$$

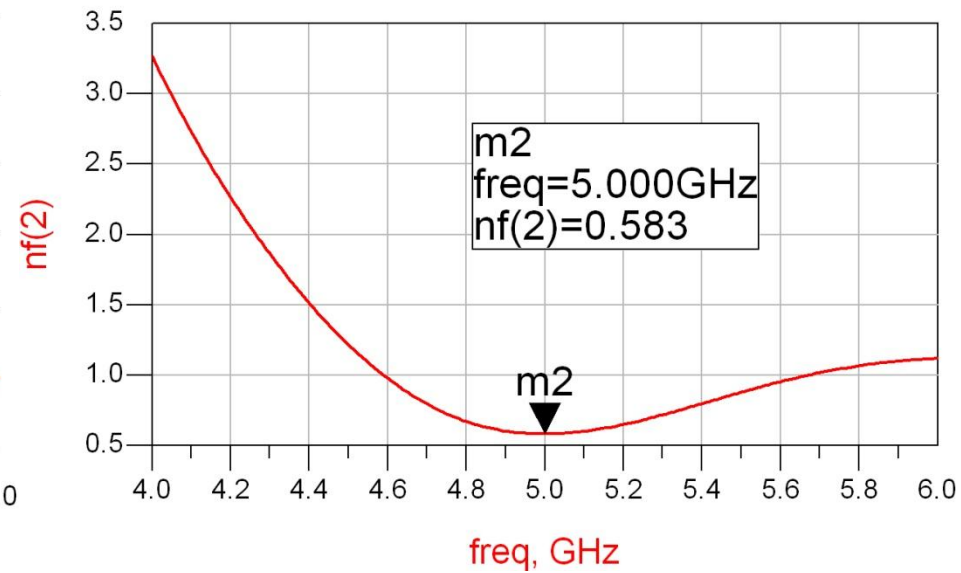
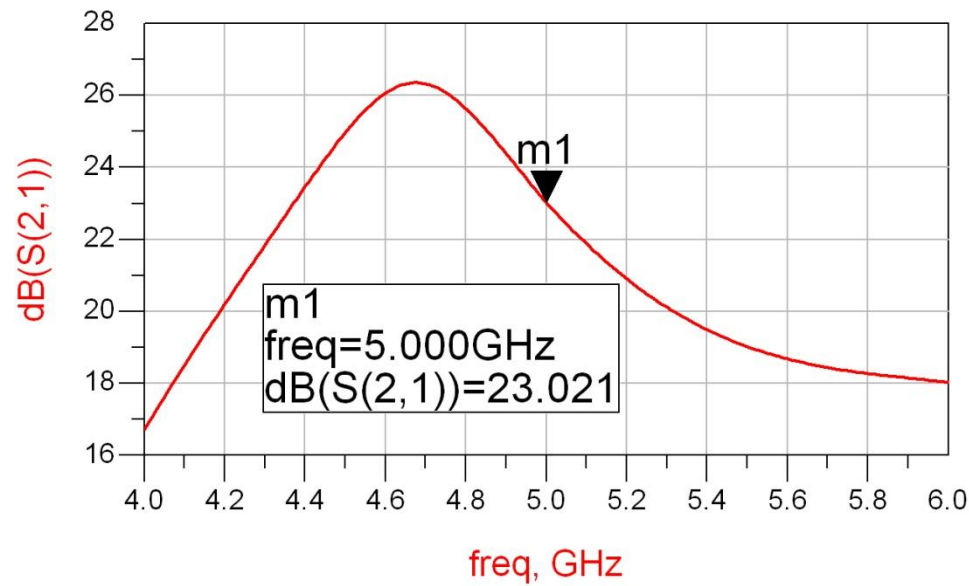
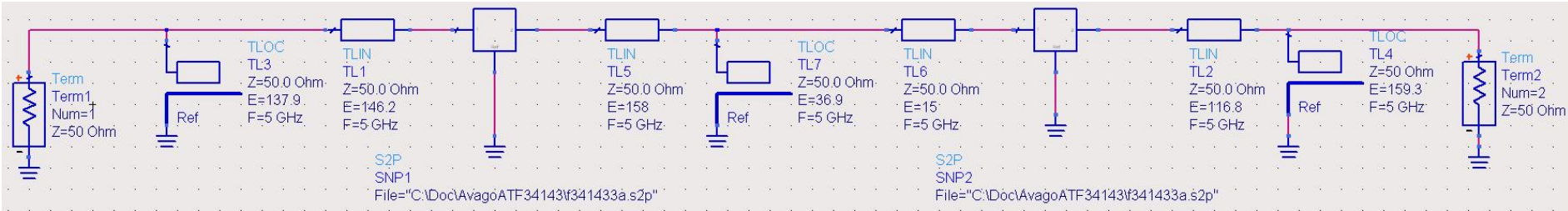
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = 0.751$$

$$\theta_{sp} = 36.9^\circ$$

stub
"combinat"



ADS 4



Adaptare inter-etaje

- Toate variantele obtinute indeplinesc conditiile de castig si zgomot
- Se alege una convenabila in functie de:
 - dimensiunile fizice ale liniilor $l = \frac{\theta}{360^\circ} \cdot \lambda$
 - comportare in frecventa
 - stabilitate
 - performanta (zgomot/castig)
 - reflexie intrare iesire
 - etc.

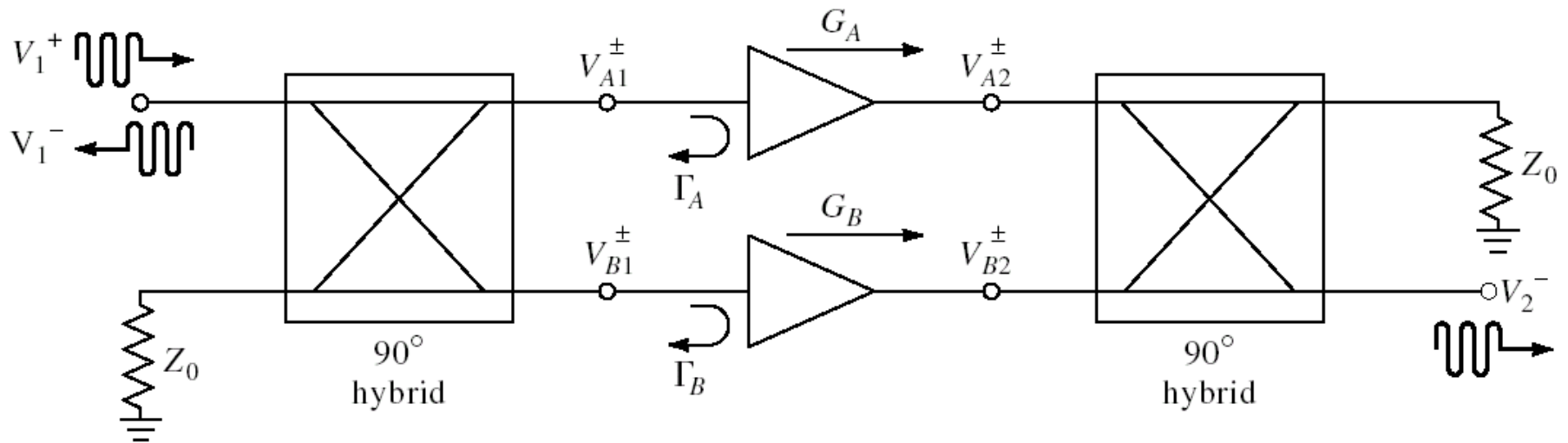
Amplificatoare de banda larga

Amplificatoare de microunde

Amplificatoare de banda larga

- Se pot obtine prin un numar de tehnici de proiectare
 1. Retele de adaptare care sa compenseze scaderea castigului cu frecventa
 2. Retele de adaptare rezistive
 3. Reactie negativa
 4. Amplificatoare echilibrate
 5. Amplificatoare distribuite
 6. Amplificatoare differentiale

Amplificatoare echilibrate



- 2 Amplificatoare (identice) cu doua cuploare hibride 3 dB / 90° la intrare si iesire

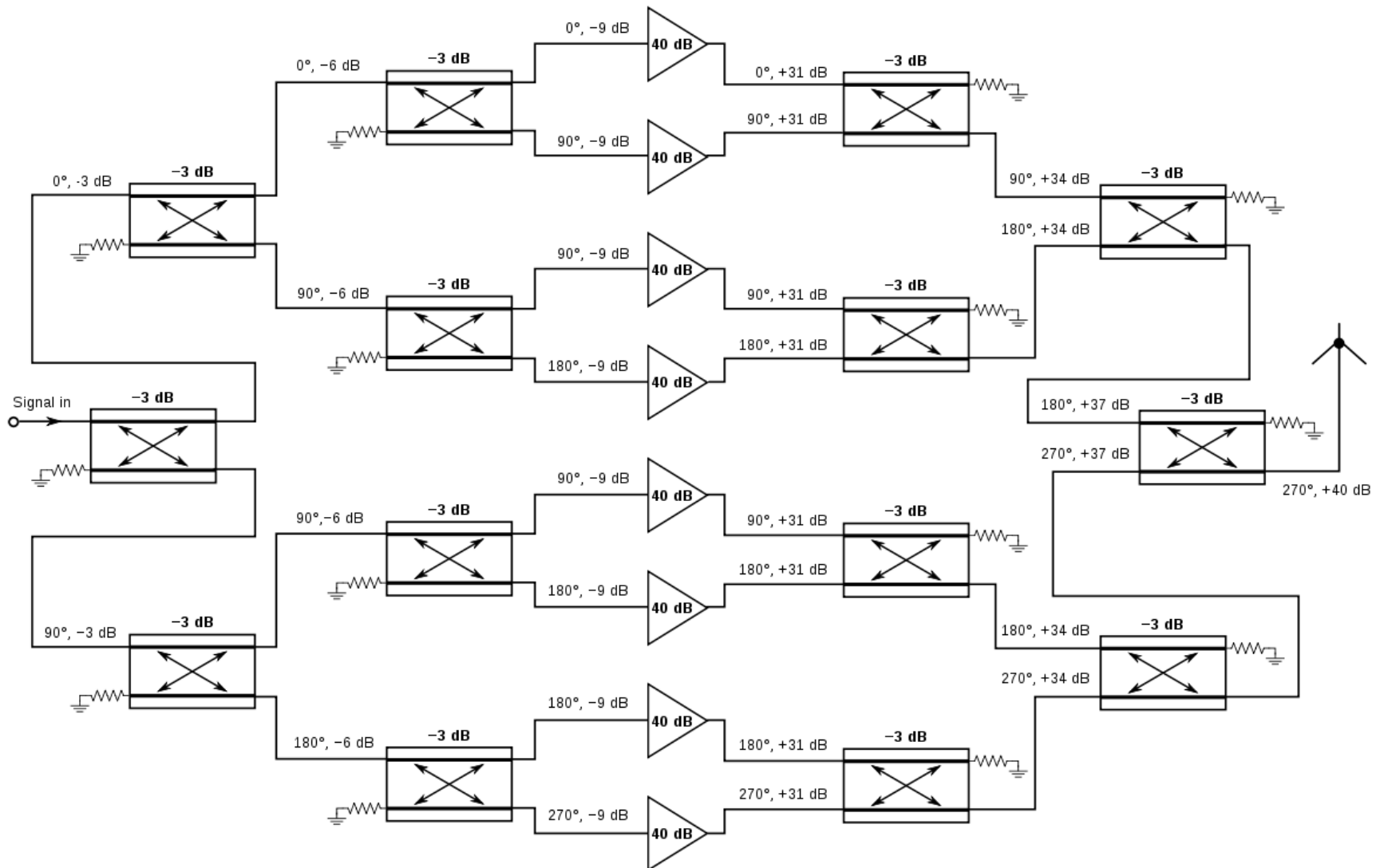
$$S_{21} = \frac{-j}{2} \cdot (G_A + G_B)$$

$$S_{21}|_{A=B} = -j \cdot G$$

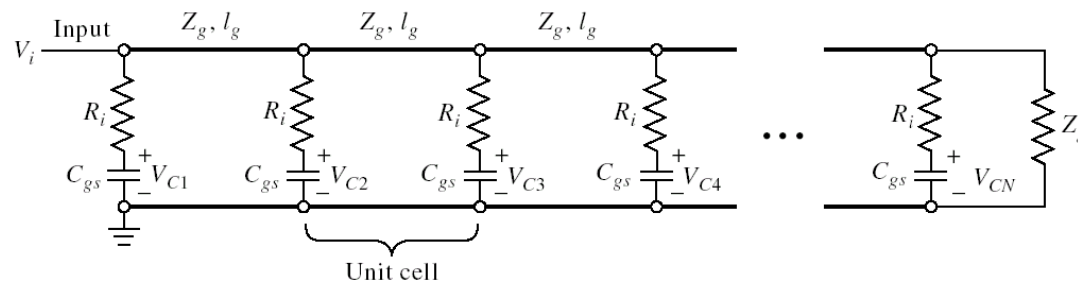
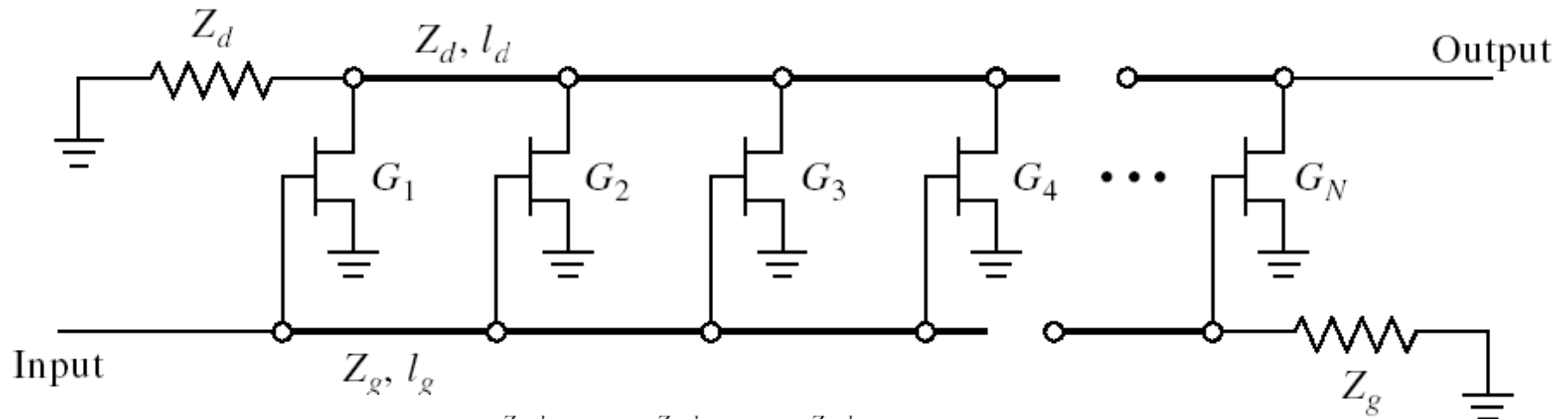
$$S_{11} = \frac{1}{2} \cdot (\Gamma_A - \Gamma_B) \quad F = \frac{1}{2} \cdot (F_A + F_B)$$

$$S_{11}|_{A=B} = 0$$

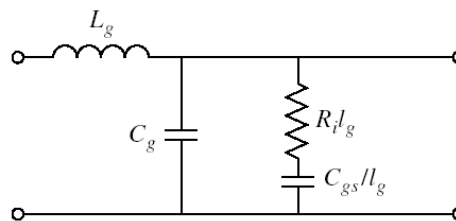
Amplificatoare echilibrate



Amplificatoare distribuite



(a)



(b)

Amplificatoare distribuite

- Conditia de sincronizare

- intarzierea pe liniile de intrare (grila) egala cu cea de pe liniile de iesire (drena)

$$\gamma_g = \alpha_g + j \cdot \beta_g \quad \gamma_d = \alpha_d + j \cdot \beta_d \quad \beta_g \cdot l_g = \beta_d \cdot l_d$$

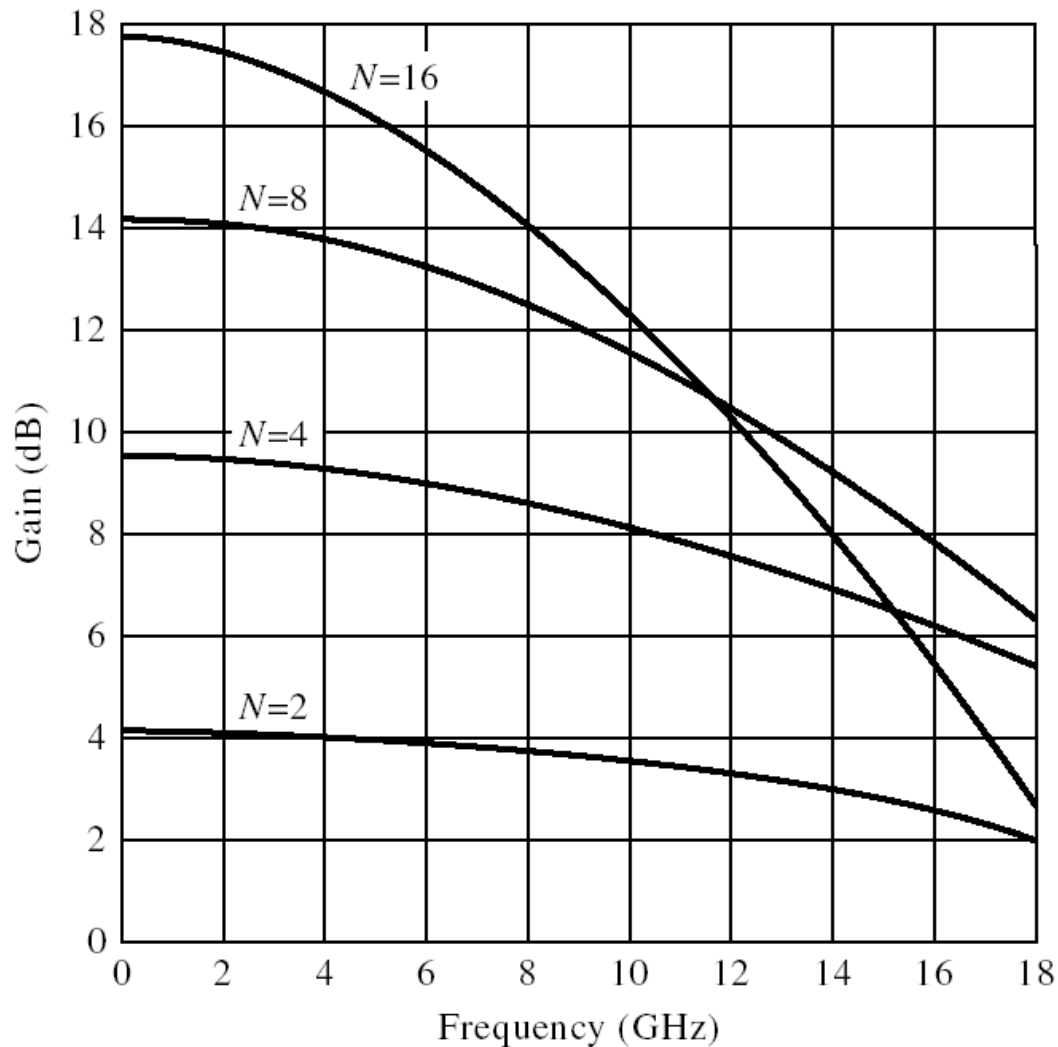
- Castigul de putere

$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g}{4} \cdot \frac{\left(e^{-N \cdot \alpha_g \cdot l_g} - e^{-N \cdot \alpha_d \cdot l_d} \right)^2}{\left(e^{-\alpha_g \cdot l_g} - e^{-\alpha_d \cdot l_d} \right)^2}$$

- Castigul de putere fara pierderi

$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g \cdot N^2}{4}$$

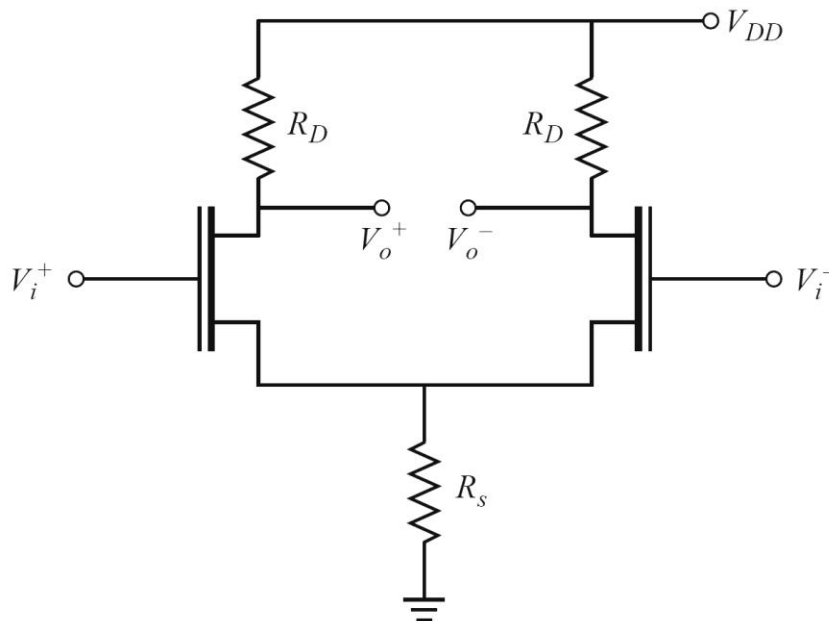
Amplificatoare distribuite



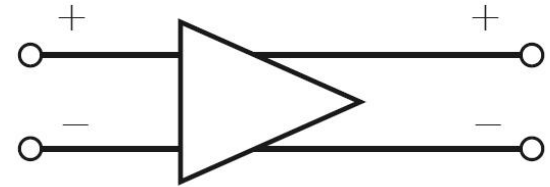
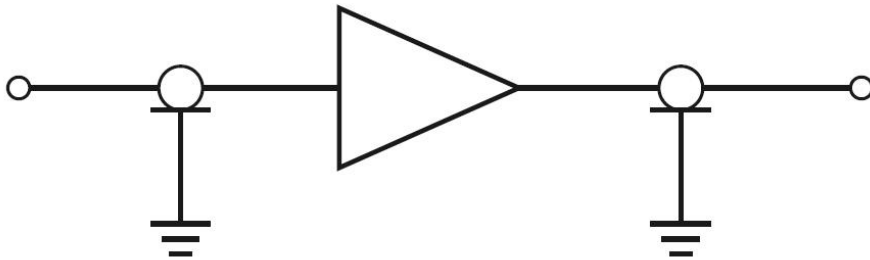
$$N_{opt} = \frac{\ln(\alpha_g \cdot l_g) - \ln(\alpha_d \cdot l_d)}{\alpha_g \cdot l_g - \alpha_d \cdot l_d}$$

Amplificatoare diferențiale

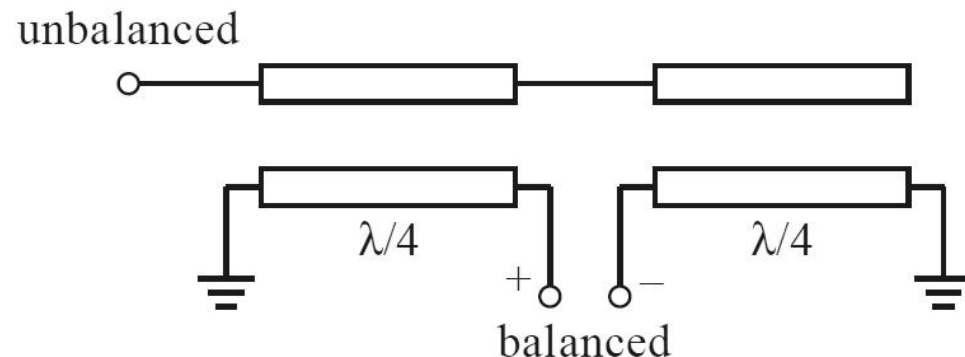
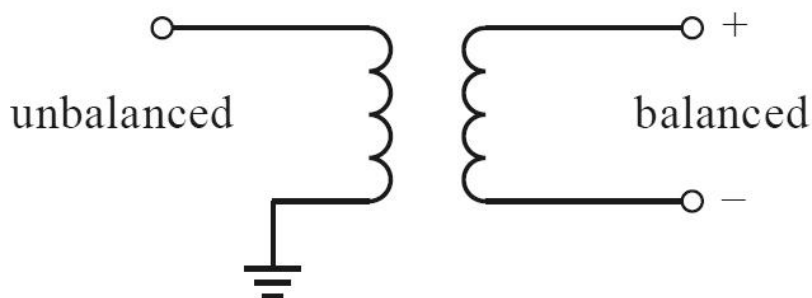
- Capacitățile de intrare în cele două tranzistoare în conexiune diferențială apar conectate în serie
- Se dublează astfel frecvența unitară



Amplificatoare diferențiale



- Se utilizeaza structuri de circuit care sa faca conversia de la dispozitivele unipolare la cele diferențiale
 - cuploare hibride 3dB / 180°
 - "balun" (balanced - unbalanced)



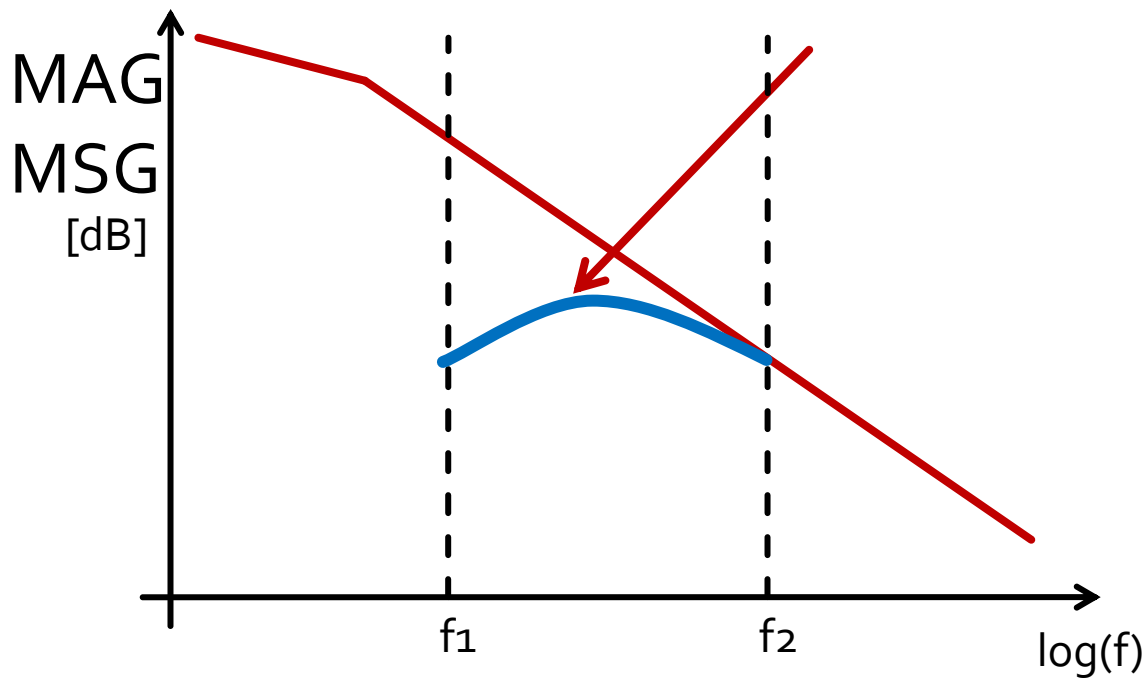
Amplificatoare de banda larga

- Se pot obtine prin un numar de tehnici de proiectare
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 2. Retele de adaptare rezistive
 3. Reactie negativa
 4. Amplificatoare echilibrate
 5. Amplificatoare distribuite
 6. Amplificatoare differentiale

Amplificatoare de banda larga

1. **Retele de adaptare care sa compenseze scaderea castigului cu frecventa**

- Metoda utilizata este de a repeta proiectarea la mai multe (macar 2) frecvente si impunerea unui castig egal la acestea



Filtre pentru microunde

Filtre pentru microunde

- In domeniul microundelor se utilizeaza doua strategii de implementare a filtrelor
 - structuri specifice microundelor (linii cuplate, rezonatori dielectrice, structuri periodice)
 - sinteza de filtre cu elemente concentrate urmate de implementare cu linii de transmisie
- prima strategie duce la obtinerea unor filtre mai eficiente dar e caracterizata de
 - generalitate mai mica
 - proiectare deseori dificila (lipsa relatiilor analitice)

Sinteza filtrelor

- Sinteza filtrelor cu elemente concentrate, urmata de implementarea acestora cu elemente distribuite (linii)
 - generala
 - relatii analitice usor de implementat pe calculator
 - eficienta
- Metoda preferata este metoda pierderilor de insertie

Metoda pierderilor de insertie

$$P_{LR} = \frac{P_S}{P_L} = \frac{1}{1 - |\Gamma(\omega)|^2}$$

- $|\Gamma(\omega)|^2$ este o functie para de ω

$$|\Gamma(\omega)|^2 = \frac{M(\omega^2)}{M(\omega^2) + N(\omega^2)}$$

$$P_{LR} = 1 + \frac{M(\omega^2)}{N(\omega^2)}$$

- Alegerea corespunzatoare a polinoamelor M si N determina comportarea filtrului

Metoda pierderilor de insertie

- Se aleg polinoamele pentru implementarea unui FTJ (prototip)
- Acest filtru poate fi convertit la alte functii, scalat in frecventa pentru a obtine alte tipuri de functii

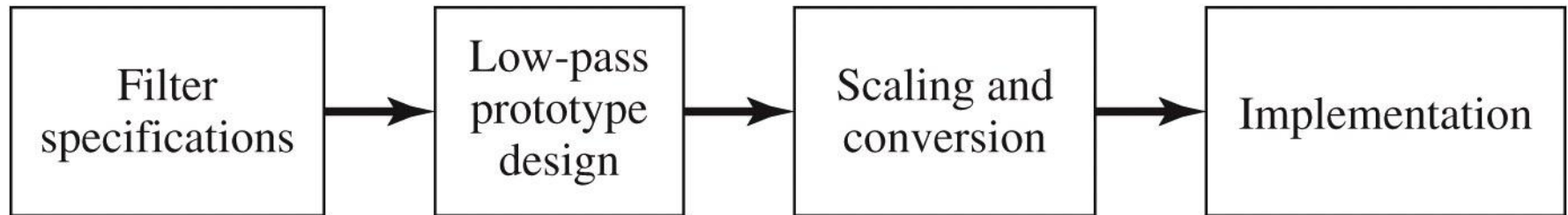


Figure 8.23

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Caracteristici de filtru trece jos prototip

- **Maxim plat** (Butterworth, binomial) ofera cea mai plata comportare in banda de trecere
- **Echiriplu** (Cebasev) ofera atenuare mai mare in banda de taiere cu dezavantajul existentei unor variatii (riplu) in banda de trecere
- **Filtre eliptice**, caracterizate de variatii (riplu) si in banda de taiere si in banda de trecere
- **Filtru cu raspuns liniar in faza**, ofera intarziere de grup de maxim plat, cu dezavantajul unei atenuari in putere mai mica, necesar in anumite aplicatii

FTJ prototip Maxim plat/Echiriplu

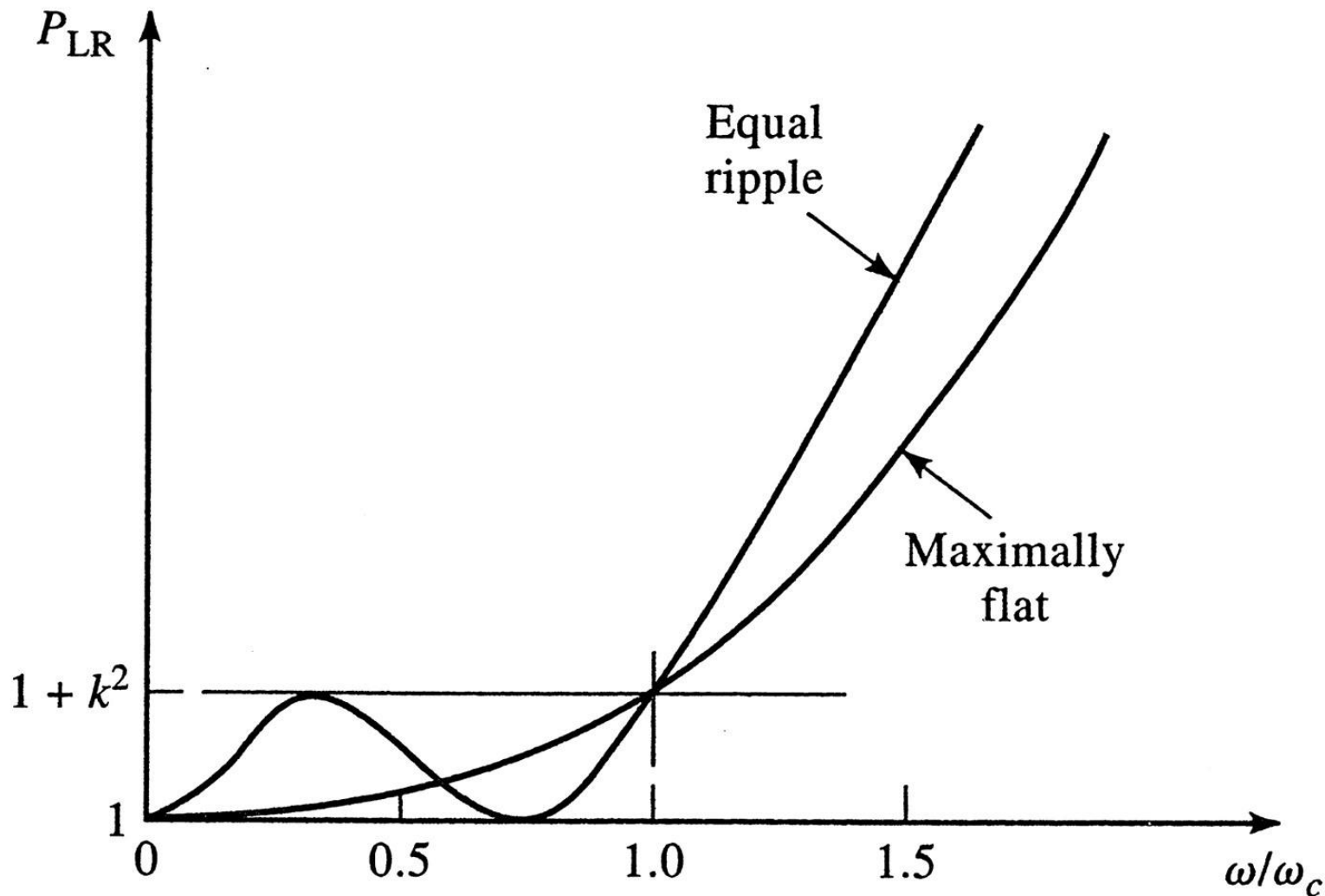


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FTJ elliptic prototip

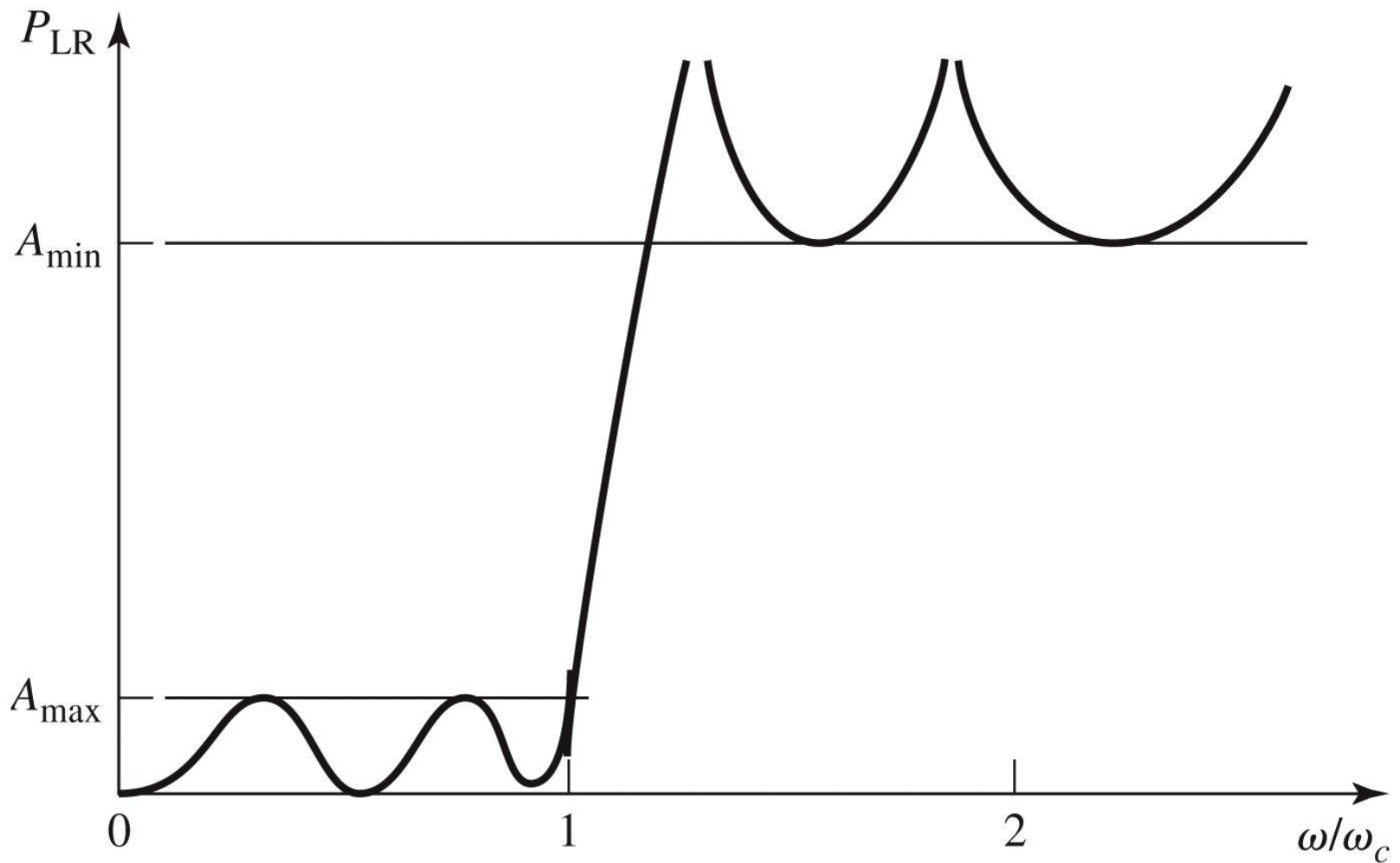


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FTJ de tip maxim plat

- Polinomul

$$P_{LR} = 1 + k^2 \cdot \left(\frac{\omega}{\omega_c} \right)^{2N}$$

- pentru $\omega \gg \omega_c$

$$P_{LR} \approx k^2 \cdot (\omega/\omega_c)^{2N}$$

- atenuarea creste cu 20N dB/decada

- k ofera atenuarea la limita benzii de trecere (3dB implica $k = 1$)

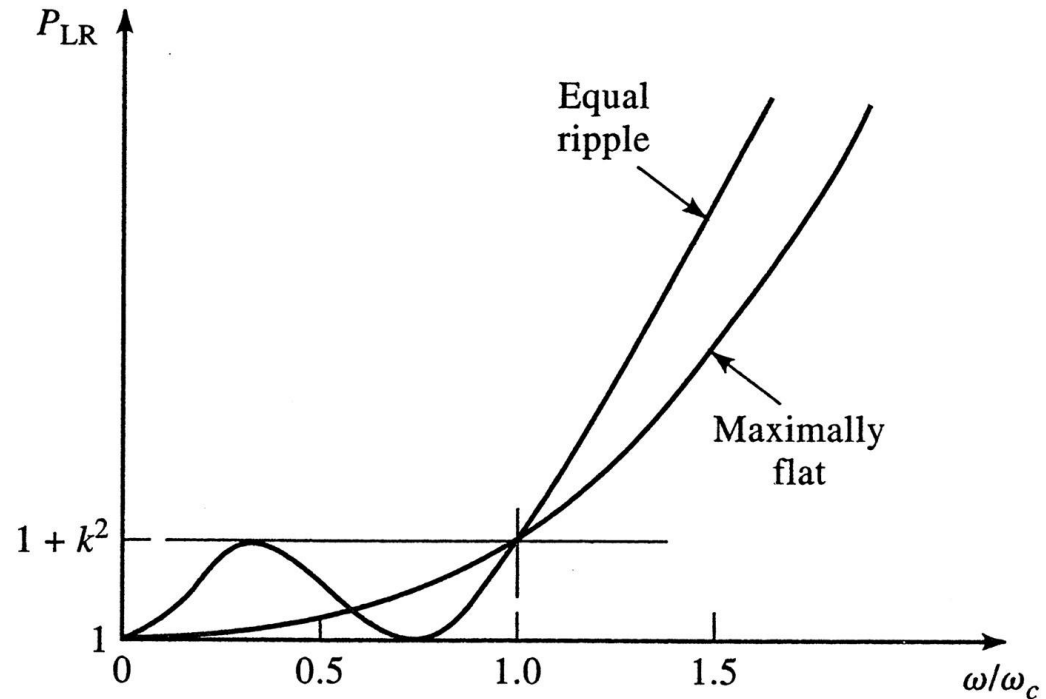


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FTJ de tip echiriplu

- Polinomul

$$P_{LR} = 1 + k^2 \cdot T_N^2 \left(\frac{\omega}{\omega_c} \right)$$

- pentru $\omega \gg \omega_c$

$$P_{LR} \approx \frac{k^2}{4} \cdot \left(\frac{2 \cdot \omega}{\omega_c} \right)^{2N}$$

- atenuarea crește cu $20N$ dB/decada

- atenuarea este mai mare de $(2^{2N})/4$ decat cea a filtrului binomial la frecventele $\omega \gg \omega_c$

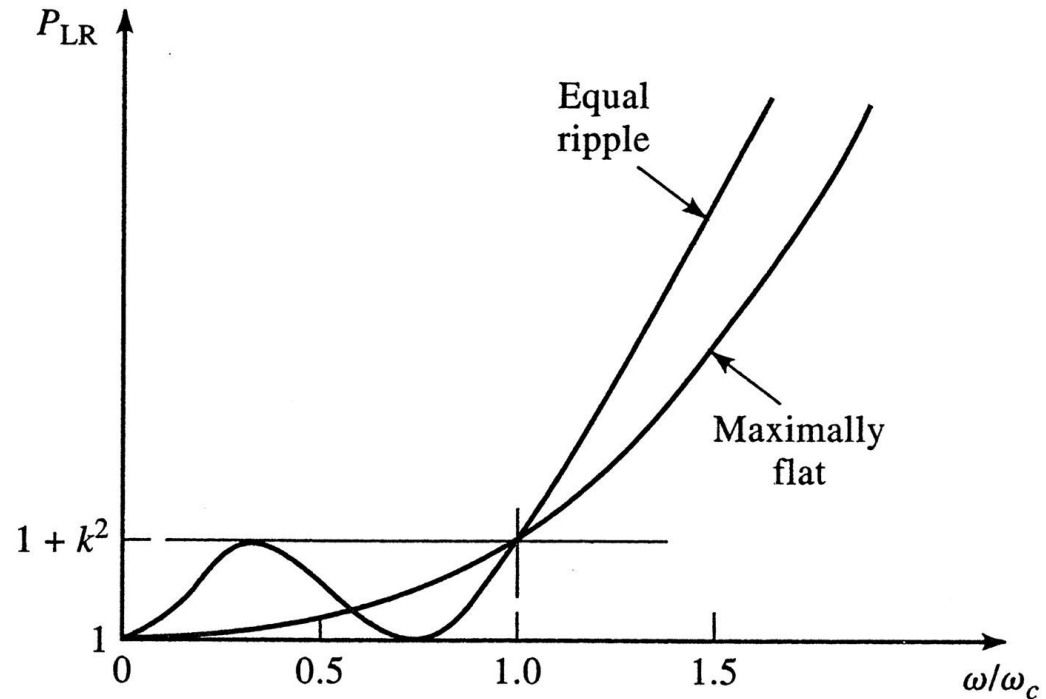


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